

Warm Up

Determine the common ratio for each of the following:

X	Y ₁
-1	-2
-2	-4.5
-3	-6.75
-4	-10.13

X	Y ₁
1	.6
2	.12
3	.024
4	.0048

Determine an equation that would define each of the above sets of data:

(Hint: Look around your TI-83 for some help!!)

Transformations of the Exponential Function

$$y = a(b)^x$$

initial value \swarrow a \nwarrow base b

check with...



Properties:

If $b > 1$, then the graph will be **GROWTH**

If $0 < b < 1$, then the graph will be **DECAY**

y - intercept: happens when $x = 0$, so...

$$y\text{-int} = a$$

Transformations of the Exponential Function

$(y\text{-Int})$ $y = a(b)^x + d$ check with...

initial value base vertical translation



Properties:

If $b > 1$, then the graph will be **GROWTH**

If $0 < b < 1$, then the graph will be **DECAY**

y - intercept: happens when $x = 0$, so... $y\text{-int} = a + d$

Horizontal Asymptote - a horizontal line that a graph approaches but never intersects.

Equation of Horizontal Asymptote will be... $y = d$

Domain - describes all possible x -values

Range - describes all possible y -values

Thus, for exponential functions... Domain: $\{x \in \mathbb{R}\}$

Range: $\{y > d\}$

Horizontal Asymptote

Exercise: Complete the following table...

Equation	Growth/Decay	y-intercept	Eq'n for Horizontal Asymptote
$y = 3(5)^x - 4$	G	-1	$y = -4$
$y = 4\left(\frac{2}{5}\right)^x + 1$	D	5	$y = 1$
$y = 2^x - 2$	G	-2	$y = -2$
$y = \frac{3}{4}\left(\frac{1}{2}\right)^x$	D	$\frac{3}{4}$	$y = 0$
$y = 5(3)^x$	G	5	$y = 0$

Homework...

p. 129 #9 - 12

p. 140 #43 (without technology)
#44
#46

Solutions

- p. 129 9. b. This graph has a horizontal asymptote at $y = 0$.
c. The y intercept is at $(0, 2)$.
e. The graph is a decay curve, since $0 < b < 1$.

10.

Question	Function	y-intercept	Growth or decay	Reason
a	$y = 4(3.2)^x$	$(0, 4)$	growth	$b = 3.2 > 1$
b	$y = 2.1(0.8)^x$	$(0, 2.1)$	decay	$b = 0.8 < 1$
c	$y = 0.3(1.1)^x$	$(0, 0.3)$	growth	$b = 1.1 > 1$
d	$y = 0.7(0.85)^x$	$(0, 0.7)$	decay	$b = 0.85 < 1$

11. All three functions have $a = 1$, since they all cross the y axis at $y = 1$. The function f has a b that is greater than 0 but less than 1, since it is a decay curve. The functions g and h both have a b that is greater than 1, since they are both growth curves. The b in the equation for g will be greater than the b in the equation for h, since the curve for the function g rises at a faster rate than the curve for the function h.
12. a. f has $a = 1$, g has $a = 2$ and h has $a = 3$. We can see this by looking at the y intercepts of each of the graphs. For all three graphs, the ratio of successive y terms is 1.5, so the b for all three is equal to 1.5
b. The equations would be $f(x) = 1.5^x$, $g(x) = 2(1.5)^x$ and $h(x) = 3(1.5)^x$.

p. 140 #43. b)

Equation	Eq'n for Horizontal Asymptote
$y = 2^x$	$Y = 0$
$y = 2^x - 1$	$Y = -1$
$y = 2^x + 3$	$Y = 3$

#44. a) ii b) iv c) v d) vi e) i f) iii

#46.

Equation	Growth/Decay	y-intercept	Eq'n for Horizontal Asymptote
$y = 2^x - 3$	Growth	$(0, -2)$	$Y = -3$
$y = 2(3)^x + 1$	Growth	$(0, 3)$	$Y = 1$
$y = 20(0.8)^x - 2.4$	Decay	$(0, 17.6)$	$Y = -2.4$
$y = 1.7(1.25)^x$	Growth	$(0, 1.7)$	$Y = 0$