

D) Determine the LCM & GCF for  
320 and 4828

$$\begin{array}{c}
 320 \\
 | \\
 2 \quad 160 \\
 | \quad | \\
 2 \quad 80 \\
 | \quad | \\
 2 \quad 40 \\
 | \quad | \\
 2 \quad 20 \\
 | \quad | \\
 2 \quad 10 \\
 | \quad | \\
 2 \quad 5 \\
 | \\
 5
 \end{array}
 = 2^6 \cdot 5$$

$$\begin{array}{c}
 4828 \\
 | \\
 4 \\
 | \\
 2 \quad 1207 \\
 | \quad | \\
 2 \quad 17 \\
 | \quad | \\
 17 \quad 71
 \end{array}
 = 2^2 \cdot 17 \cdot 71$$

$$\frac{\text{Greatest Common Factor:} \ ( \text{Lowest common power of prime factor} )}{= 2^2 = 4}$$

Least Common Multiple

$$\begin{aligned}
 &= 2^6 \cdot 5 \cdot 17 \cdot 71 \\
 &= \underline{386240}
 \end{aligned}$$

## 3.3 Common Factors of a Polynomial



### LESSON FOCUS

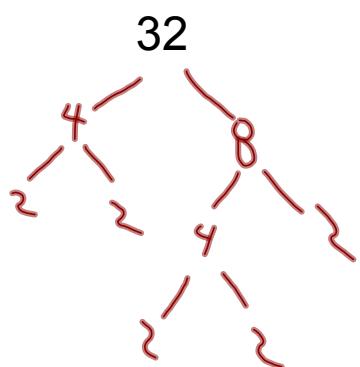
Model and record factoring a polynomial.

Compare multiplying and factoring in arithmetic and algebra.

In Arithmetic	In Algebra
<i>Multiply</i> factors to form a product. $(4)(7) = 28$	<i>Expand</i> an expression to form a product. $3(2 - 5a) = 6 - 15a$
<i>Factor</i> a number by writing it as a product of factors. $28 = (4)(7)$	<i>Factor</i> a polynomial by writing it as a product of factors. $6 - 15a = 3(2 - 5a)$

Factoring is the same as the process of PRIME FACTORIZATION...  
Only it is done using algebra skills!!

Determine the prime factorization for each of the following...



$$\begin{aligned}
 & 12a^2 - 30a^6 \\
 & \cancel{2} \quad \cancel{2} \\
 & \quad 6a^2 - 15a^6 \\
 & \quad \cancel{3} \quad \cancel{5} \\
 & \quad 2a^2 - a^6 \\
 & \quad \cancel{a^2} \quad \cancel{a^6} \\
 & = 6a^2(2 - 5a^4) \\
 & = 12a^2 - 30a^6
 \end{aligned}$$

Factoring: The process of expressing a polynomial as the product of its factors.

We will now examine a variety of factoring techniques

## I. Greatest Common Factor

Factor each binomial.

$$\text{a) } \frac{6n}{3} + \frac{9}{3}$$
$$3(2n+3)$$

$$\text{b) } \frac{6c}{2c} + \frac{4c^2}{2c}$$
$$= 2c(3+2c)$$

## Example 2 Factoring Trinomials

Factor the trinomial  $\frac{5}{s} - \frac{10z}{s} - \frac{5z^2}{s}$ .

$$= 5(1 - 2z - z^2)$$

OR

$$= -5(-1 + 2z + z^2)$$

## Example 3 Factoring Polynomials in More than One Variable

Factor the trinomial. Verify that the factors are correct.

$$\frac{-12x^3y}{4xy} - \frac{20xy^2}{4xy} - \frac{16x^2y}{4xy}$$

$$4xy(-3x^2 - 5y - 4xy)$$

Factor each of the following:

$$\frac{9m^4n^2 - 6m^3n^3}{3m^2n^2}$$
$$3m^3n^2(3m - 2n)$$

~~$3m(3m^3n^2 - 2m^2n^3)$~~

Not GCF

$$42s^3t^2 - 14s^2t - 77s^4$$
$$= 7s^2(6st^2 - 2t - 11s^2)$$

Get the idea....let's make things a little more interesting...

$$\frac{w^2}{w} = w^1 \quad \frac{(a+3)^4}{(a+3)} = (a+3)^1$$

Factor each of the following:

$$30w^5 - 24w^3 \rightarrow \frac{14x(a-7)}{2(a-7)} - \frac{2(a-7)}{2(a-7)}$$
$$6w^3 \oplus (5w^2 - 4)$$
$$2(a-7)(7x-1)$$

Let  $\tilde{x} = x - 3$

$$3x^2(x-3) + 24y(x-3) - 15(x-3)$$

$$3x^2 \tilde{x} + 24y \tilde{x} - 15 \tilde{x}$$

$$3 \tilde{x} (x^2 + 8y - 5)$$

$$\frac{5w^3(2w-1)^3 - (2w-1)^5}{(2w-1)^3}$$
$$(2w-1)^3 [5w^3 - (2w-1)^5]$$

**Checkpoint...do you really understand??**

Completely factor each of the following polynomials:

$$9 + 8b^2$$

$$-32n^9 + 32n^6 + 40n^5$$

$$-10y^7 + 6y^{10} - 4y^{10}x - 8y^8x$$

$$30y^4z^3x^5 + 50y^4z^5 - 10y^4z^3x$$

$$3a(2a + 5b) - 7b(2a + 5b)$$

$$6w^3(5a - 3)^2 + 4w(5a - 3)^6$$

## Practice Problems:

Pg. 155

# 9, 10, 12, 14, 15b, 16, 19