

Review Questions:

Practice Test...

#4) $S(\theta) = \sqrt{2} \cos \theta + \theta$, $0 \leq \theta \leq 2\pi$

$S'(\theta) = 0$ ← horizontal

$S'(\theta) = -\sqrt{2} \sin \theta + 1$

$0 = -\sqrt{2} \sin \theta + 1$

$-\frac{1}{\sqrt{2}} = \sin \theta$

$\sin \theta = \frac{1}{\sqrt{2}}$

(Ref $\frac{\pi}{4}$, Q1,2)

$180 - \theta$	θ
S	A
$180 + \theta$	$360 - \theta$

$\theta = \frac{\pi}{4}, \frac{1}{-1} - \frac{\pi}{4}$
 $= \frac{3\pi}{4}$



$S\left(\frac{\pi}{4}\right) = \sqrt{2} \cos \frac{\pi}{4} + \frac{\pi}{4}$
 $= \sqrt{2} \left(\frac{1}{\sqrt{2}}\right) + \frac{\pi}{4}$
 $= 1 + \frac{\pi}{4}$

$\left(\frac{\pi}{4}, 1 + \frac{\pi}{4}\right)$

$S\left(\frac{3\pi}{4}\right) = \sqrt{2} \cos \frac{3\pi}{4} + \frac{3\pi}{4}$

$= \sqrt{2} \left(-\frac{1}{\sqrt{2}}\right) + \frac{3\pi}{4}$

$= -1 + \frac{3\pi}{4}$

$\left(\frac{3\pi}{4}, -1 + \frac{3\pi}{4}\right)$

$$1. a) \sec(\cot x^3)$$

$$\sec(\cot x^3) \tan(\cot x^3) \left[-\csc^2 x^3 (3x^2) \right]$$

$$2. b) x^3 + y^3 = 6xy \quad @ (3, 3)$$

$$3x^2 + 3y^2 \frac{dy}{dx} = 6y + 6x \frac{dy}{dx}$$

$$\frac{dy}{dx} = \frac{6y - 3x^2}{3y^2 - 6x}$$

$$\text{at } (3, 3) \quad m = ?$$

$$m = \frac{6(3) - 3(3)^2}{3(3)^2 - 6(3)}$$

$$m = -1$$

$$y - 3 = -1(x - 3)$$

$$y - 3 = -x + 3$$

$$y = -x + 6$$

$$\text{OR } \underline{x + y - 6 = 0}$$

$$6. s(t) = t^3 - 15t^2 + 72t - 5$$

$$a) s'(t) = 3t^2 - 30t + 72$$

$$s''(t) = 6t - 30$$

$$12 = 6t - 30$$

$$\frac{42}{6} = \frac{6t}{6}$$

$$7 = t$$

$$\underline{7 \text{ sec} = \text{time}} \implies s'(7) = 3(7)^2 - 30(7) + 72 = \underline{9 \text{ m/s}}$$

$$b) \text{Velocity} < 0$$

$$\frac{3t^2 - 30t + 72}{3} < \frac{0}{3}$$

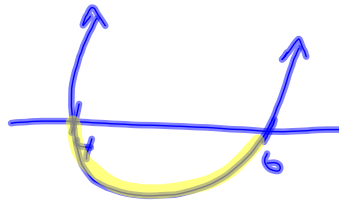
$$\oplus t^2 - 10t + 24 < 0$$

$$(t-6)(t-4) < 0$$

x-Intercepts

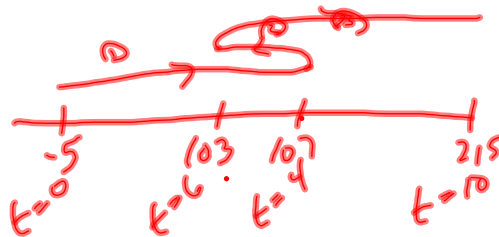
$$t = 6, 4$$

opens up



$$\{4 < t < 6\}$$

time	Position
0	-5
4	107
6	103
10	215



$$\text{distance} = 112 + 4 + 112 = \underline{228 \text{ m}}$$

$$7. f(x) = x^2 + x \quad \text{at } x = 5 \quad \& \quad x = -1$$

$$f'(x) = 2x + 1$$

$$\text{at } x = 5$$

$$f'(5) = 2(5) + 1$$

$$\underline{m = 11}$$

$$f(5) = (5)^2 + 5$$

$$= 30$$

$$(5, 30) \quad m = 11$$

$$y - 30 = 11(x - 5)$$

$$y - 30 = 11x - 55$$

$$\underline{y = 11x - 25}$$

$$\text{at } x = -1$$

$$m = 2(-1) + 1$$

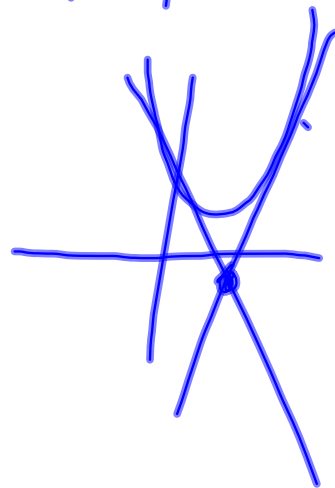
$$= -1$$

$$f(-1) = (-1)^2 + (-1) = 0$$

$$(-1, 0) \quad m = -1$$

$$y - 0 = -1(x + 1)$$

$$y = -x - 1$$



$$11x - 25 = -x - 1$$

$$\frac{12x}{12} = \frac{24}{12}$$

$$x = 2 \implies y = -2 - 1$$

$$y = -3$$

$$(2, -3)$$

pg. 126

$$s = 450 + 10t - 5t^2$$

#9 a) $s' = 0$
 $s' = 10 - 10t$
 $0 = 10 - 10t$
 $10t = 10$
 $t = \underline{1 \text{ sec}}$



b) $0 = \frac{450}{5} + \frac{10t}{5} - \frac{5t^2}{5}$
 $0 = 90 + 2t - t^2$ (c)

$$t = \frac{-2 \pm \sqrt{4 - 4(-1)(90)}}{2(-1)}$$

$t = -$
 $\hat{=} \underline{\underline{10.5 \text{ sec}}}$

Practice Test

$$\# 5 f(x) = (x^2 - 2)(x - 2)^{-1}$$

$$f'(x) = (2x)(x - 2)^{-1} + (x^2 - 2) \left[-1(x - 2)^{-2} (1) \right]$$

$$\underline{h} \quad m = -1$$

$$\frac{2x(x - 2)^{-1} + (x^2 - 2)(-1(x - 2)^{-2})}{(x - 2)^2} = -1$$

$$\frac{2x}{x - 2} - \frac{x^2 - 2}{(x - 2)^2} = -1(x - 2)^2$$

$$(x - 2)(2x) - x^2 + 2 = -1(x - 2)^2$$

Pg. 111 $y'' = ??$

#7 a) $x^4 + y^4 = 1$

$$4x^3 + 4y^3 \frac{dy}{dx} = 0$$

$$\frac{dy}{dx} = \frac{-4x^3}{4y^3}$$

$$\frac{dy}{dx} = -\frac{x^3}{y^3}$$

$$\frac{d^2y}{dx^2} = \frac{-3x^2y^3 + x^3(3y^2 \frac{dy}{dx})}{y^6}$$

$$\frac{d^2y}{dx^2} = \frac{-3x^2y^3 + 3x^3y^2 \left(\frac{-x^3}{y^3} \right)}{y^6}$$

Related Rates

Must understand the process of implicit differentiation...

Interpret the notation $\frac{dy}{dx}$

What about $\frac{dV}{dt}$, given that "V" is volume and "t" is time.

$$\textcircled{1} \frac{dP}{dw} = 2 \frac{dl}{dw} + 2(1)$$

$$\textcircled{2} 1 = 2 \frac{dl}{dP} + 2 \frac{dw}{dP}$$

Example:

Given the formula $P = 2l + 2w$

- ① • differentiate with respect to w
- differentiate with respect to P
- differentiate with respect to time (use t)

$$\frac{dP}{dt} = 2 \frac{dl}{dt} + 2 \frac{dw}{dt}$$

Differentiate each of the following with respect to time:

$$A = \pi r^2$$

$$a^2 + b^2 = c^2$$

$$\frac{dA}{dt} = \pi(2r) \frac{dr}{dt}$$

$$2a \frac{da}{dt} + 2b \frac{db}{dt} = 2c \frac{dc}{dt}$$

$$V = \frac{1}{3} \pi r^2 h$$

$$\frac{dV}{dt} = \frac{1}{3} \pi \left(2r \frac{dr}{dt} h + r^2 \frac{dh}{dt} \right)$$

Attachments

Integration Tables.pdf