

Pg. 188

#2/ Minimize Sum } x - 1st #
 y \rightarrow 2nd #

$$S = x + 2y$$

$$xy = 200$$

$$S(x) = x + 2\left(\frac{200}{x}\right)$$

$$y = \frac{200}{x}$$

$$S(x) = x + 400x^{-1}$$

$$S'(x) = 1 - 400x^{-2}$$

$$0 = 1 - \frac{400}{x^2}$$

$$0 = x^2 - 400 \implies \sqrt{400} = \sqrt{x^2}$$

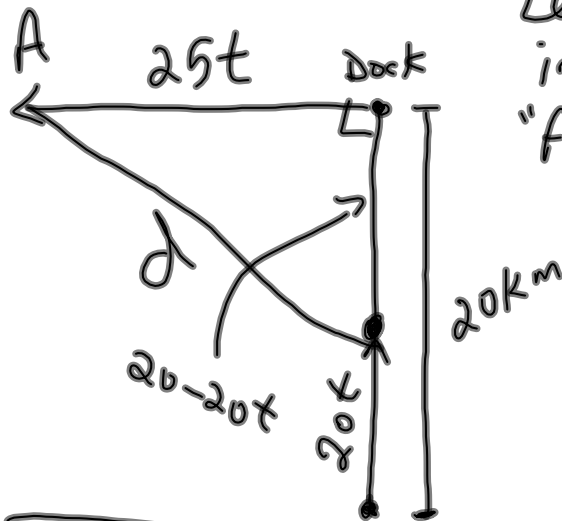
$$0 = (x-20)(x+20) \quad \pm 20 = x$$

$$x = \pm 20$$

2 Positives $\therefore x \neq -20$

$$\left. \begin{array}{l} x = 20 \\ y = \frac{200}{20} = 10 \end{array} \right\} 20 \text{ ; } 10$$

17/



Let "t" be time
in hours after
"A" leaves the dock

$$d = st$$

$$d = \sqrt{(25t)^2 + (20-20t)^2}$$

$$d' = \frac{1}{2} \left[625t^2 + (20-20t)^2 \right]^{-\frac{1}{2}} \left[1250t + 2(20-20t)(-20) \right]$$

$$0 = \frac{625t - 20(20-20t)}{\sqrt{625t^2 + (20-20t)^2}}$$

$$0 = 625t - 400 + 400t$$

$$400 = 1025t$$

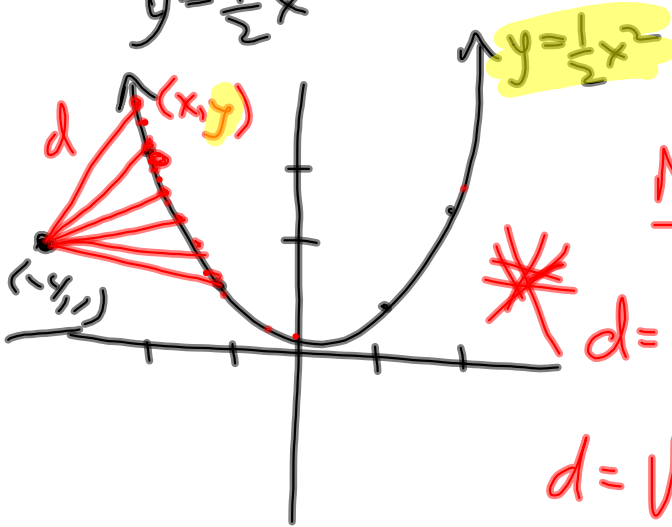
$$\frac{400}{1025} = t$$

$$t = 0.39 \text{ hours} \times \frac{60 \text{ min}}{1 \text{ hr.}}$$

$$\approx \underline{23 \text{ minutes}}$$

\therefore Closest @ 12:23 PM

11. $2y = x^2$ $(-4, 1)$
 $y = \frac{1}{2}x^2$



Minimize Distance

~~$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$~~

$d = \sqrt{(x+4)^2 + (y-1)^2}$

$d = \sqrt{(x+4)^2 + \left(\frac{1}{2}x^2 - 1\right)^2}$

$d' = \frac{1}{2} \left[\cancel{(x+4)^2} + \left(\frac{1}{2}x^2 - 1\right)^2 \right]^{-1/2} \left[\cancel{2(x+4)} + \cancel{2} \left(\frac{1}{2}x^2 - 1\right)'(x) \right]$

$0 = (x+4) + x \left(\frac{1}{2}x^2 - 1\right)$

$0 = \cancel{x} + 4 + \frac{1}{2}x^3 - \cancel{x}$

$0 = 8 + x^3$

$-8 = x^3$

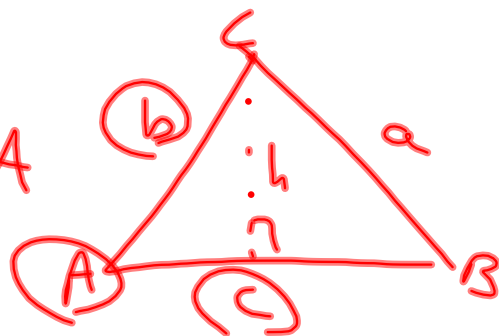
$-2 = x$

$y = \frac{1}{2}(-2)^2 = 2$

$\therefore (-2, 2)$ is closest to $(-4, 1)$

Law of Cosines

$$a^2 = b^2 + c^2 - 2bc \cos A$$



Law of Sines

$$\frac{a}{\sin A} = \frac{b}{\sin B}$$

Area of triangle

$$A = \frac{1}{2}bh$$

OR

$$A = \frac{1}{2}ab \sin C$$

