



Sir Isaac Newton

Welcome to ... Advanced Mathematics with Calculus 120



Gottfried Leibniz

Housework to get done today...

- Attendance
- Introductions
- Classroom Rules...
 1. Must be on time and prepared with all necessary supplies.
 2. No food or drink during class other than water and a light snack before class.
 3. Must be respectful of all others in the classroom. Someone speaking or intercom in use means EVERYONE else is listening.
- Review emergency evacuation procedures and "code black".
- Course Outline

Fundamental Skills Review

Radicals:

Simplify each of the following... $(6\sqrt{2})(5\sqrt{3})$

$$\begin{array}{l}
 3\sqrt{72} \\
 3(6\sqrt{2}) \\
 = 18\sqrt{2}
 \end{array}
 \quad
 \begin{array}{l}
 3(3\sqrt{8}) \\
 9\sqrt{8} \\
 9(2\sqrt{2}) \\
 18\sqrt{2}
 \end{array}
 \left\{
 \begin{array}{l}
 (3\sqrt{8})(5\sqrt{3}) \\
 15\sqrt{24} \\
 15(2\sqrt{6}) \\
 30\sqrt{6}
 \end{array}
 \right.
 \quad
 \left.
 \begin{array}{l}
 \left(\frac{\sqrt{3}}{2}\right)^2 \\
 \left(\frac{3}{4}\right) \\
 \left(\sqrt{3}\right)^2 \\
 3
 \end{array}
 \right.$$

$$\begin{array}{l}
 3\sqrt{98} - 2\sqrt{32} \\
 21\sqrt{2} - 8\sqrt{2} \\
 = \underline{13\sqrt{2}}
 \end{array}$$

1 Rationalize the denominator...

$$\frac{6}{5\sqrt{2}} \left(\frac{\sqrt{2}}{\sqrt{2}} \right)$$
$$= \frac{6\sqrt{2}}{10}$$
$$= \frac{3\sqrt{2}}{5}$$

$$\sqrt{\frac{4}{5}}$$

$$= \frac{\sqrt{4}}{\sqrt{5}}$$
$$= \frac{2}{\sqrt{5}} \left(\frac{\sqrt{5}}{\sqrt{5}} \right)$$
$$= \frac{2\sqrt{5}}{5}$$

$$(a-b)(a+b)$$

$$\frac{2}{3+\sqrt{6}} \left(\frac{3-\sqrt{6}}{3-\sqrt{6}} \right)$$

$$\frac{6-2\sqrt{6}}{9-6}$$
$$= \frac{6-2\sqrt{6}}{3}$$
$$= 2 - \frac{2\sqrt{6}}{3}$$

Algebraic Processes:

Factor each of the following...

$$3x^2 - 10x + 8$$

$$3x^2 - 6x - 4x + 8$$

$$3x(x-2) - 4(x-2)$$

$$(x-2)(3x-4)$$

$$27m^{27} + v^{12}$$

$$(3m^9 + v^4)(9m^{18} - 3m^9v^4 + v^8)$$

$\pm 1, \pm 2, \pm 4, \pm 8$

$a=1$: $3a^3 - a^2 - 10a + 8$

$$3 - 1 - 10 + 8 = 0$$

$\therefore a=1$ is a Root

$\therefore (a-1)$ is a factor

$$\begin{array}{r|rrrr}
 -1 & 3 & -1 & -10 & 8 \\
 \hline
 & \downarrow & -3 & -2 & 8 \\
 \hline
 & 3 & 2 & -8 & 0
 \end{array}$$

$$(a-1)(3a^2 + 2a - 8)$$

$$3a^2 - 4a + 6a - 8$$

$$a(3a-4) + 2(3a-4)$$

$$(a-1)(3a-4)(a+2)$$

Common factor
 Trinomials
 Diff. of Squares
 Sum & Diff. of cubes
 Factor theorem

$$m^2 - 6m + 8 = (m-8)(m+8)$$

$$(x^4 - 1)^2 - 64$$

$$[(x^4 - 1) - 8][(x^4 - 1) + 8]$$

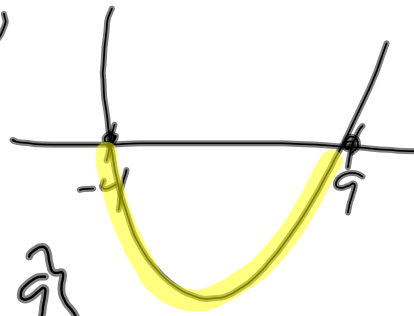
$$(x^4 - 9)(x^4 + 7)$$

$$(x^2 - 3)(x^2 + 3)(x^4 + 7)$$

Solve the following...

$$m^2 - 5m < 36$$

Below

$$\textcircled{+} m^2 - 5m - 36 < 0$$
$$(m - 9)(m + 4) < 0$$
$$m = 9 \text{ \& } -4$$
$$\{-4 < x < 9\}$$


Locate the vertex of the following quadratic function...

$$f(x) = -2x^2 + 12x - 6$$