

Warm-up: Find t_{125} for each of the following...

$$t_n = a + (n-1)d$$

a) $t_1 = 5$
 $d = -6$

b) $t_1 = 10$
 $t_{20} = 67$

linear patterns

$$t_{125} = 5 + (125-1)(-6)$$

$$t_{125} = 5 + (-744)$$

$$t_{125} = \underline{-739}$$

b) $t_{125} = 10 + (124)d$

$$67 = 10 + (20-1)d$$

$$67 = 10 + 19d$$

$$\frac{57}{19} = \frac{19d}{19}$$

$$3 = d$$

$$t_{125} = 10 + (124)(3)$$

$$= \underline{382}$$

$$\begin{aligned} \text{c) } t_{10} &= 16 \\ d &= 3 \end{aligned}$$

$$t_n = t_1 + d(n-1)$$

$$16 = t_1 + (3)(10-1)$$

$$16 = t_1 + 27$$

$$-11 = t_1$$

$$t_{125} = -11 + (3)(125-1)$$

$$= -11 + 372$$

$$= 361$$

$$\begin{aligned} \text{d) } t_{11} &= -48 \\ t_{27} &= -128 \end{aligned}$$

$$\begin{aligned} t_{11} &\Rightarrow -48 = a + (11-1)d \\ -48 &= a + 10d \end{aligned}$$

$$\begin{aligned} t_{27} &\Rightarrow -128 = a + (27-1)d \\ -128 &= a + 26d \end{aligned}$$

$$\begin{array}{r} -128 = a + 26d \\ \text{Subtract} \left\{ \begin{array}{l} -48 = a + 10d \\ \hline -80 = 16d \\ 16 \quad 16 \\ -5 = d \end{array} \right. \end{array}$$

$$\text{Sub: } -48 = a + 10(-5)$$

$$-48 + 50 = a$$

$$2 = a$$

$$\begin{aligned} t_{125} &= 2 + (125)(-5) \\ &= -618 \end{aligned}$$

WARM - UP

1, 1, 2, 3, 5, 8, 13, 21, 34, 55, . . .

Finish the above number sequence!!!

1202



Leonardo Pisano Fibonacci

Born 1170 in (probably) Pisa

Died 1250 in (possibly) Pisa

His Book:

Liber abaci

The Book of the Abacus

His work introduces the arithmetic and algebra he learned in the Middle East.

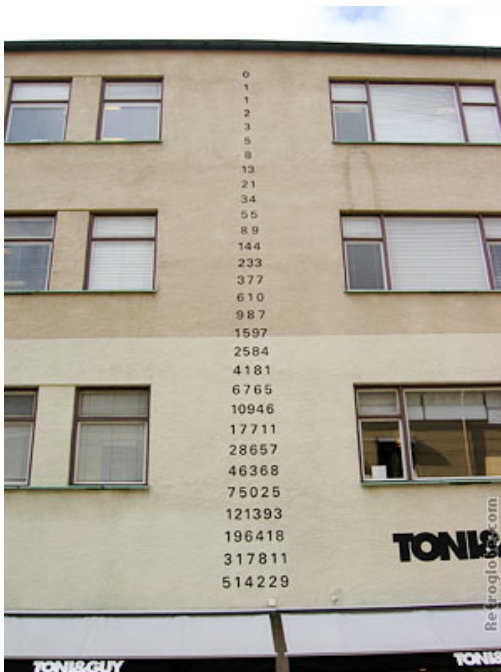
Fibonacci introduces the
Fibonacci Sequence

Illustration of Fibonacci by a French artist, 1873
© 1873, 1874

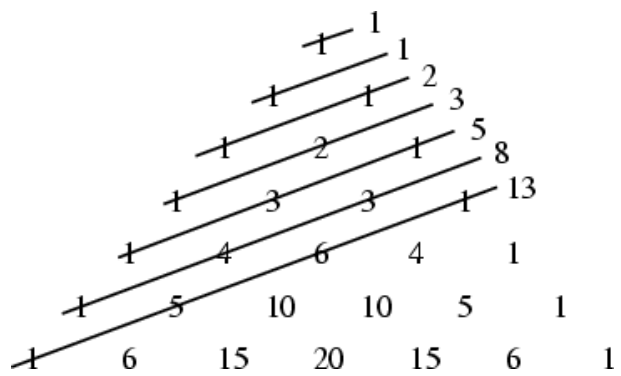
The Fibonacci Sequence

- Important numerical sequence over 800 years old that was originally developed to predict how many pairs of rabbits there will be if one assumes that each month, each pair produces a new pair of baby rabbits, that then bear again two months later...
- The sequence begins with 1, and each successive number is the sum of the previous two numbers.
- 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144 ...

0+1 1+1 1+2 2+3 3+5 5+8...



Building in Goteborg, Sweden



Levels of Differences

The results of subtracting consecutive terms in a sequence are referred to as Levels of Difference.

- If the **First-level Differences (D_1)** result in a common number, the relation is **LINEAR**

ex: -25, -20, -15, -10, -5, ...

$$t_n = a + (n-1)d$$

D_1 : 5, 5, 5, 5, ...
 ⇒ constants at first level

- If the **Second-Level Differences (D_2)** result in a common number, the relation is **QUADRATIC**

ex: 2, 9, 22, 41, 66, ...

D_1 : 7, 13, 19, 25, ... $t_n = 3n^2 - 2n + 1$
 D_2 : 6, 6, 6, ...

QuadReg
 $y = ax^2 + bx + c$
 $a = 3$
 $b = -2$
 $c = 1$
 $R^2 = 1$

- If the **Third-Level Differences (D_3)** result in a common number, the relation is **CUBIC**

ex: -4, 7, 40, 107, 220, ...

D_1 : 11, 33, 67, 113
 D_2 : 22, 34, 46
 D_3 : 12, 12, ...

$$t_n = n^3 + \dots$$

- If the **Fourth-Level Differences (D_4)** result in a common number, the relation is **QUARTIC**

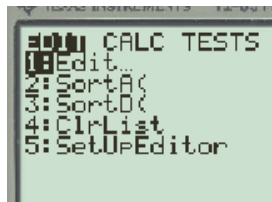
ex: 1, 16, 81, 256, 625, 1296, ...

D_1 : 15, 65, 175, 369, 671
 D_2 : 50, 110, 194, 302
 D_3 : 60, 84, 108
 D_4 : 24, 24

Creating Equations with the TI-83

1. Determine if the sequence is linear, quadratic, cubic or quartic.
 (Using Levels of Difference-on your own paper)

2. Enter the data into Lists: $n \Rightarrow L_1$ $t_n \Rightarrow L_2$

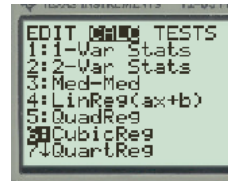
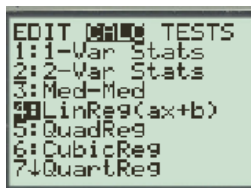


3. Then "Calculate" the regression for the type of function determined by the level of differences.



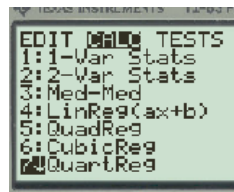
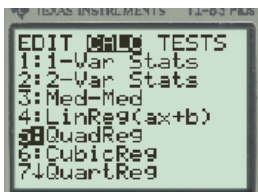
Linear $y = ax + b$

Cubic $y = ax^3 + bx^2 + cx + d$



Quadratic $y = ax^2 + bx + c$

Quartic $y = ax^4 + bx^3 + cx^2 + dx + e$



Can you come up with the general term for each of these??

X	Y ₁	
1	1	
2	5	
3	11	
4	17	
5	23	
6	29	
7	35	

X=1

X	Y ₁	
1	3	
2	11	
3	23	
4	37	
5	53	
6	71	
7	91	

X=1