

Example #2: After experimentation, it was found that the safe stopping distance, d , (in metres) for a heavy aircraft that taxis at a speed, v , (in km/h) is given by...

$$d = 0.003(6v^2 + 400v + 50\,000)$$

- a) What is the safe stopping distance of the aircraft taxiing at 100 km/h? 450m
- b) Determine the speed at which the aircraft is taxiing to take 200 m to stop safely. \approx

$$\begin{aligned} \text{a) } d &= 0.003(6(100)^2 + 400(100) + 50\,000) \\ d &= \underline{450\text{m}} \end{aligned}$$

$$\begin{aligned} \text{b) } \frac{200}{0.003} &= \frac{0.003(6v^2 + 400v + 50\,000)}{0.003} \\ 66\,666.\bar{6} &= 6v^2 + 400v + 50\,000 \end{aligned}$$

$$0 = 6v^2 + 400v - 16\,666.\bar{6}$$

$$V = \frac{-400 \pm \sqrt{(400)^2 - 4(6)(-16\,666.\bar{6})}}{2(6)}$$

400²-4(6)(-16666.666)
= 559999.984
√(Ans) = 748.3314667

$$V = \frac{-400 \pm 748.331}{12}$$

$$V = \frac{-400 + 748.331}{12} \quad \text{or} \quad V = \frac{-400 - 748.331}{12}$$

$$V = \underline{29.03 \text{ km/h}}$$

can't Be (-)

Warm Up

A frustrated Math student opens his second floor bedroom window and throws his textbook up into the air and it lands on the lawn below the window. The height h (metres) of the textbook at any time t (seconds) as it falls toward the ground is represented by the equation $h = -4.9t^2 + 39.2t + 8$

- (a) What is the **maximum height** reached by the textbook? [3]
 (b) How high is the student's bedroom window above the ground? [1]
 (c) When will the textbook hit the lawn? [2]

$$\begin{aligned} \text{a) } h &= -4.9(t^2 - 8t + 16) + 8 + 78.4 \\ h &= -4.9(t-4)^2 + 86.4 \end{aligned}$$

$$V(4, 86.4)$$

(t, h)

$$= 86.4 \text{ m}$$

(b) Sub. $t=0$:

$$\begin{aligned} h &= 0 + 0 + 8 \\ h &= 8 \text{ m} \end{aligned}$$

(c) $0 = -4.9(t-4)^2 + 86.4$

$$\frac{-86.4}{-4.9} = (t-4)^2$$

$$\pm \sqrt{\frac{86.4}{4.9}} = t-4$$

$$t = 4 \pm \sqrt{\frac{86.4}{4.9}}$$

$$t = 8.199 \text{ or } -0.199$$

Quad. Formula:

$$0 = -4.9t^2 + 39.2t + 8$$

$$t = \frac{-39.2 \pm \sqrt{(39.2)^2 - 4(-4.9)(8)}}{2(-4.9)}$$

$$t = \frac{-39.2 \pm 41.15}{-9.8}$$

$39.2^2 + 4 \cdot 4.9 \cdot 8$
1693.44
√(Ans) = 41.15142768

$$t = \frac{-39.2 - 41.15}{-9.8} \text{ or } t = \frac{-39.2 + 41.15}{-9.8}$$

$$t = 8.199 \text{ sec} \quad t = -0.199$$

$$(-39.2 - 41.15) \div -9.8$$

Homework...

Practice Sheet

* Quiz coming up on Thursday