

- Without the aid of a calculator arrange the following radicals in descending order:

$$\begin{array}{cccccc}
 & \xrightarrow{=} 4 & & \text{Between} & & \\
 & & & 2 \& 3 & & \\
 \rightarrow & \sqrt[3]{13} & , & \sqrt{18} & , & \sqrt{9} & , & \sqrt[4]{27} & , & \sqrt[3]{-5} \\
 \text{Between} & & & = 3 & & & & & & \leftarrow \text{some} \\
 2 \& 3 & & & & & & & & (-) \text{ Number}
 \end{array}$$

- What strategies were used?

$$\begin{array}{cccccc}
 & & \approx 2.3 & & \approx 2.2 & & \\
 \sqrt{18} & , & \sqrt{9} & , & \sqrt[3]{13} & , & \sqrt[4]{27} & , & \sqrt[3]{-5} \\
 & & 2.35 & & 2.28 & & & &
 \end{array}$$

Pre-requisite skill...

Solve this inequation:

$$4x + 5 > 9x - 10$$

$$\frac{-5x}{-5} > \frac{-15}{-5}$$

$$3 > x$$

$$x < 3$$

Let's revisit restrictions...

State any restrictions on the following radicals:

$$\sqrt{3x+5}$$

$$3x+5 \geq 0$$
$$\frac{3x}{3} \geq \frac{-5}{3}$$
$$x \geq -\frac{5}{3}$$

$$\sqrt[5]{4-x}$$

None

$$\sqrt[12]{5-3x}$$

$$5-3x \geq 0$$

$$\frac{-3x}{-3} \geq \frac{-5}{-3}$$

$$x \leq \frac{5}{3}$$

$$\sqrt[6]{4x^8}$$

None

Always (+)

- Simplifying Radicals

Required prior knowledge:

- Expressing radicals as exponents

$$\sqrt{x} \rightarrow x^{\frac{1}{2}}$$

$$16^{\frac{1}{2}} = \sqrt{16} \\ = 4$$

$$\sqrt[7]{x} \rightarrow x^{\frac{1}{7}}$$

$$\sqrt[5]{x^9} = x^{\frac{9}{5}} = \left(\sqrt[5]{x}\right)^9$$

ex. $8^{\frac{5}{3}} = 32$

↑

$\left(\sqrt[3]{8}\right)^5$

$\frac{x^4}{x^9}$

$$16^{-\frac{3}{4}} = \frac{1}{16^{\frac{3}{4}}} \\ = \frac{1}{8}$$

$$\omega^0 = 1$$

$$3\omega^0 = 3(1)$$

$$(3\omega)^0 = 1$$

- Converting radicals between forms (Mixed \leftrightarrow Entire)

$$9\sqrt{50}$$

$$9(\sqrt{25 \cdot 2})$$

$$9(5\sqrt{2})$$

$$45\sqrt{2}$$

$$\sqrt[3]{40}$$

$$\sqrt[3]{8 \cdot 5}$$

$$= 2\sqrt[3]{5}$$

$$\sqrt{12} \quad (\sqrt{4 \cdot 3})$$

$$2\sqrt{3} \quad \sqrt{50}$$

$$= 5\sqrt{2}$$

$$\sqrt{27} = \sqrt{9 \cdot 3}$$

$$3\sqrt{3} = \sqrt{9 \cdot 3}$$

$$\sqrt{8} = 2\sqrt{2} \quad 3\sqrt{3}$$

$$\sqrt{72} = 6\sqrt{2}$$

$$\sqrt{9 \cdot 8}$$

$$3\sqrt{8}$$

$$2\sqrt[5]{96}$$

$$2\sqrt[5]{32 \cdot 3}$$

$$2(2\sqrt[5]{3})$$

$$4\sqrt[5]{3}$$

$$5\sqrt{2}$$

$$= \sqrt{5^2 \cdot 2}$$

$$= \sqrt{50}$$

$$3\sqrt{5}$$

$$= \sqrt{4 \cdot 5}$$

$$2\sqrt[3]{5}$$

$$\sqrt[3]{2^3 \cdot 5}$$

$$= \sqrt[3]{40}$$

Simplifying radicals involving variables:

$$\sqrt{x^{16}} = (x^{16})^{\frac{1}{2}} = x^8$$

$$\sqrt[3]{w^{27}} = (w^{27})^{\frac{1}{3}} = w^9$$

$$\sqrt[5]{32y^{10}} = (y^{10})^{\frac{1}{5}} = 2y^2$$

What if things do not work out as nicely??

Pg. 273 #1-6

$$\sqrt{x^{11}} = \sqrt{x^{10} \cdot x^1} = x^5 \sqrt{x}$$

$$\sqrt{27x^6y^5} = \sqrt{9 \cdot 3 \cdot x^6 \cdot y^4 \cdot y^1} = 3x^3y^2\sqrt{3y}$$

$$\sqrt[4]{16a^5b^{18}}$$

$$\sqrt[3]{8} = 2$$

$$\sqrt[3]{-8} = -2$$

$$\sqrt[3]{w^{17}}$$

$$\sqrt[3]{w^{15} \cdot w^2}$$

$$w^5 \sqrt[3]{w^2}$$

Homework:

Page 278

#1 - 6