

Pg. 319

$$\#15) \quad d = rt$$

$$t = \frac{d}{r}$$

$$(a) \quad t = \frac{2n^2 + 11n + 12}{2n^2 - 32}$$

$$\begin{aligned} & 2n^2 + 8n + 3n + 12 \\ & 2n(n+4) + 3(n+4) \\ & (n+4)(2n+3) \end{aligned}$$

$$t = \frac{(n+4)(2n+3)}{2(n-4)(n+4)}$$

$$(b) \quad \frac{2(n-4)(n+4)}{2(n-4)}$$

$$t = \frac{2n+3}{2(n-4)}$$

$$n \neq \pm 4$$

$$\begin{aligned} & 2(n^2 - 16) \\ & 2(n-4)(n+4) \end{aligned}$$

$$26.b) \frac{\sqrt{4(x^2-9)}^2 - (x+3)^2}{x^2 + 6x + 9} \rightarrow \frac{4w^2 - y^2}{(2w-y)(2w+y)}$$

$$\frac{[2(x^2-9) - (x+3)][2(x^2-9) + (x+3)]}{(x+3)^2}$$

$$\frac{(2x^2-x-21)(2x^2+x-15)}{(x+3)^2}$$

$$2x^2-7x+6x-21$$

$$x(2x-7)+3(2x-7)$$

$$(2x-7)(x+3)$$

$$2x^2+6x-5x-15$$

$$2x(x+3)-5(x+3)$$

$$(x+3)(2x-5)$$

$$\frac{(2x-7)(x+3)(x+3)(x-5)}{(x+3)^2}$$

$$= (2x-7)(2x-5)$$

## Check-Up Time...

**UNDEFINED VALUES** For what values of the variable is the rational expression undefined?

**SIMPLIFYING EXPRESSIONS** Simplify the expression if possible.

$$\frac{-18x^2}{12x}$$

$$= -\frac{3x}{2}, x \neq 0$$

$$\frac{12 - 5x}{10x^2 - 24x}$$

~~$5x - 12 = 0$~~   
 ~~$5x = 12$~~   
 ~~$x = \frac{12}{5}$~~

$$= \frac{-12 - 5x}{2x(5x - 12)}$$

$$= \frac{-1}{2x}, x \neq 0, \frac{12}{5}$$

$$\cancel{x} \frac{x^3 - x}{x^3 + 5x^2 - 6x}$$

$$\frac{x(x^2 - 1)}{x(x^2 + 5x - 6)}$$

$$\frac{x(x-1)(x+1)}{x(x+6)(x-1)}$$

$$= \frac{x+1}{x+6}, x \neq 0, -6, 1$$

$$\frac{5 - x}{x^2 - 8x + 15}$$

$$= \frac{\cancel{5-x}^{-1}}{(x-\cancel{5})(x-3)}$$

$$= \frac{-1}{x-3}, x \neq 5, 3$$

$$\frac{x^3 + 9x^2 + 14x}{x^2 - 4}$$

$$\frac{x(x^2 + 9x + 14)}{(x-2)(x+2)}$$

$$\frac{x(x+7)(x+2)}{(x-2)(x+2)}$$

$$= \frac{x(x+7)}{x-2}, x \neq 2, -2$$

$$\frac{2x^2 + 11x - 6}{x+6} \rightarrow -12$$

$$\begin{aligned} & 2x^2 + 12x - x - 6 \\ & 2x(x+6) + (x+6) \\ & \cancel{(x+6)}(2x-1) \\ & \cancel{x+6} \end{aligned}$$

$$= 2x-1, x \neq -6$$

# Multiplying and Dividing Rational Expressions

## Focus on...

- comparing operations on rational expressions to the same operations on rational numbers
- identifying non-permissible values when performing operations on rational expressions
- determining the product or quotient of rational expressions in simplest form

**Objective:** Multiply and divide rational expressions.

Multiplying and dividing rational expressions is very similar to the process we use to multiply and divide fractions.

Let's recall how to multiply and divide rational numbers...

### Example

Calculate  $\frac{2}{3} \times \frac{3}{10} = \frac{18}{30} = \frac{3}{5}$

$$\frac{3}{4} \div \frac{2}{3} = \frac{3}{4} \cdot \frac{3}{2} = \frac{9}{8}$$
$$= \frac{3}{5}$$

The method for multiplying and dividing fractions also works with rational expressions. Remember that to multiply two fractions, you multiply the numerators and multiply the denominators. To divide two fractions, you multiply by the multiplicative inverse, or the reciprocal, of the divisor.

### Multiplication

$$\frac{2}{9} \cdot \frac{15}{4} = \frac{\cancel{2}^1 \cdot \cancel{3}^1 \cdot 5}{\cancel{3}^1 \cdot 3 \cdot \cancel{2}^1 \cdot 2} = \frac{5}{3 \cdot 2} = \frac{5}{6}$$

### Division

$$\frac{3}{5} \div \frac{6}{35} = \frac{3}{5} \cdot \frac{35}{6} = \frac{\cancel{3}^1 \cdot \cancel{5}^1 \cdot 7}{\cancel{5}^1 \cdot 2 \cdot \cancel{3}^1} = \frac{7}{2}$$

State any restrictions on the following rational expression and simplify:

$$\left( \frac{2x^3 + 10x^2 + 12x}{2x^2 + 14x} \right) \left( \frac{x+7}{x^2 - 9} \right)$$

① FACTOR where Possible !!

$$\frac{2x(x^2 + 5x + 6)}{2x(x+7)} \cdot \frac{x+7}{(x-3)(x+3)}$$

$$\frac{2x(x+3)(x+2)}{2x(x+7)} \cdot \frac{x+7}{(x-3)(x+3)}$$

$$= \frac{x+2}{x-3}, x \neq 0, -7, 3, -3$$

Where is the best place  
to look when identifying  
non-permissible values  
in products of rational  
expressions?

↓  
factored  
Version  
of denominator

State any restrictions on the following rational expression and simplify:

$$\frac{x+7}{x^2-9} \div \frac{x^2+9x+14}{3x^2-9x}$$

$$\begin{aligned} & \frac{x+7}{(x-3)(x+3)} \cdot \frac{3x(x-3)}{(x+7)(x+2)} \\ &= \frac{3x}{(x+3)(x+2)} \end{aligned}$$

must consider factors  
of rational expression that  
was flipped

Simplify the following rational expressions:

$$\frac{25x^2}{3y^4} \cdot \frac{24y^4}{55x^5} = \frac{40}{33x^5y^4}$$

$$= \frac{600x^2y^4}{495x^5y^8}$$

$$= \frac{40}{33x^5y^4}$$

$$\frac{a^4b^2}{a} \div \frac{b^4}{4}$$

$$= \frac{a^4b^2 \cdot 4}{b^4}$$

$$= \frac{4a^3}{b^2}$$

Multiply:  $\frac{3x^2 + 6x}{x^2 - 4x} \cdot \frac{x - 4}{x^2 + 9x + 14}$

$$\frac{3x(x+2)}{x(x-4)} \cdot \frac{(x-4)}{(x+7)(x+2)}$$

$$= \frac{3}{x+7}$$

$$\frac{x-3}{xy^2} \cdot \frac{4x^2y^3}{x^2 + x - 12}$$

$$\frac{(x-3)(4x^2y^3)}{(xy^2)(x+4)(x-3)}$$

$$= \frac{4xy}{x+4}$$