

Check-Up problem...

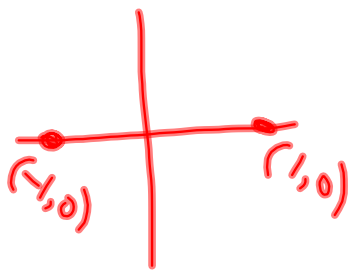
Solve:

$$\sin x \sec x + 2 \sin x = 0, x \in \mathbb{R} \quad (x \text{ is measured in radians})$$

$$\sin x (\sec x + 2) = 0$$

(y)
 $\sin x = 0$

Quadrantal

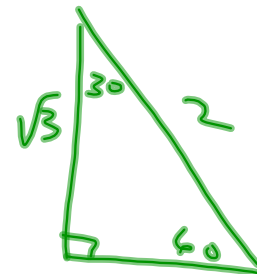


$$\begin{aligned} \mathcal{Q}_1 &= 0 + 2\pi k, k \in \mathbb{I} \\ \mathcal{Q}_2 &= \pi + 2\pi k, k \in \mathbb{I} \end{aligned}$$

$\mathcal{Q} = \mathcal{Q}_1 \cup \mathcal{Q}_2$

$$\mathcal{Q} = 0 + \pi k, k \in \mathbb{I}$$

$$\sec x = -2$$



$$\cos x = -\frac{1}{2}$$

(Ref $\frac{\pi}{3}$, Q2,3)

$$\begin{aligned} \pi - \frac{\pi}{3} \\ \pi + \frac{\pi}{3} \end{aligned}$$

$$\mathcal{Q} = \frac{2\pi}{3} + 2\pi k, k \in \mathbb{I}$$

$$\mathcal{Q} = \frac{4\pi}{3} + 2\pi k, k \in \mathbb{I}$$

What topics have we covered??

1) Converting: Degrees ↔ Radians

$$180^\circ = \pi \text{ Rad}$$

2)  In Radians ONLY!!!

$$\theta = \frac{a}{r}$$

$C = 2\pi r$
 $A = \pi r^2$ } Circles

3) Angular Velocity:

$$V_A = \frac{\theta_{\text{Rotation}}}{\text{time}}$$

4) Rotation Angles

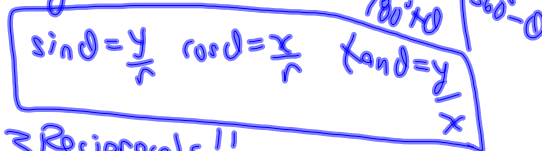
⇒ Positive & Negative Rotations
 (ccw) (cw)

⇒ Co-terminal Angles

⇒ Principal Angle

5) Reference Triangles

⇒ Trig. Ratios...



3 Reciprocals!!

* Unit Circle

⇒ Special Angles

30°, 60°, 45°, Quadrants
 Ref. & ⇒ Unit Circle

Trigonometric Equations...

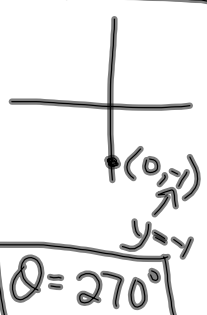
⇒ Linear } - Specific Domain
 ⇒ Quadratic } - General Solutions

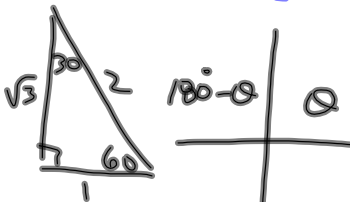
Review...

- c4 a) Determine all solutions for the equation $2 \sin^2 \theta = 1 - \sin \theta$ in the domain $0^\circ \leq \theta < 360^\circ$.

$$\begin{aligned} 2 \sin^2 \theta + \sin \theta - 1 &= 0 \\ 2m^2 + m - 1 &= 0 \\ 2m^2 + 2m - m - 1 &= 0 \\ 2m(m+1) - 1(m+1) &= 0 \\ (m+1)(2m-1) &= 0 \\ m &= -1 \quad m = \frac{1}{2} \end{aligned}$$

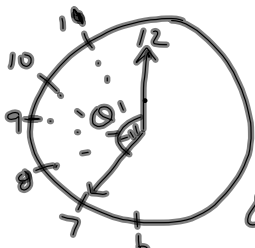
- b) Are your solutions exact or approximate? Why?
 c) Show how you can check one of your solutions to verify its correctness.

$\sin \theta = -1$
 Quadrantal


$\sin \theta = \frac{1}{2}$ ←
 (Ref $\& 30^\circ$, Q1, 2)
 $\theta = 30^\circ, 150^\circ$


b) Exact ... No Rounding.
 c) $2(\sin 30^\circ)^2 = 1 - \sin 30^\circ$
 $2\left(\frac{1}{2}\right)^2 = 1 - \frac{1}{2}$
 $2\left(\frac{1}{4}\right) = \frac{1}{2} = \frac{1}{2}$
 CS = RS

A grandfather clock shows a time of 7 o'clock. What is the exact radian measure of the angle between the hour hand and the minute hand?



$\frac{2\pi \text{ Rad}}{12}$
 $\pi \text{ Rad Between #'s}$
 $\theta = 5\left(\frac{\pi}{6}\right) = \frac{5\pi}{6}$

Determine the angular velocity of the minute hand on a clock. (Rad/sec)

1 Rotation every hour

$$V_{\text{min}} = \frac{2\pi \text{ Rad}}{60 \text{ min}} \times \frac{1 \text{ min}}{60 \text{ sec}}$$

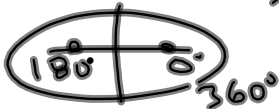
$$V_{\text{min}} = \frac{2\pi}{3600} \text{ Rad/sec}$$

$$V_{\text{min}} = \frac{\pi}{1800} \text{ Rad/sec}$$

Solve: $6 \sin^2 \theta - 3 \sin \theta = 0$, $0 \leq \theta \leq 360^\circ$

[A] $0^\circ, 30^\circ, 180^\circ, 330^\circ, 360^\circ$ $3 \sin \theta (2 \sin \theta - 1) = 0$ [B] $0^\circ, 30^\circ, 180^\circ, 150^\circ, 360^\circ$

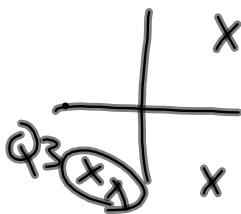
[C] $30^\circ, 90^\circ, 120^\circ, 270^\circ$ $3 \sin \theta = 0$ $\sin \theta = 0$ [D] $0^\circ, 180^\circ, 210^\circ, 330^\circ, 360^\circ$



$\sin \theta = \frac{1}{2}$
Ref: 30, 150
30, 150

If $\csc \theta < 0$ and $\tan \theta > 0$, then which of the following could be a possible measure of angle θ ?

[A] $\frac{11\pi}{6}$



[B] $\frac{4\pi}{3}$

[C] $\frac{3\pi}{4}$

[D] $\frac{\pi}{2}$

What is the principal angle of $-\frac{25\pi}{4}$?

[A] $\frac{3\pi}{4}$

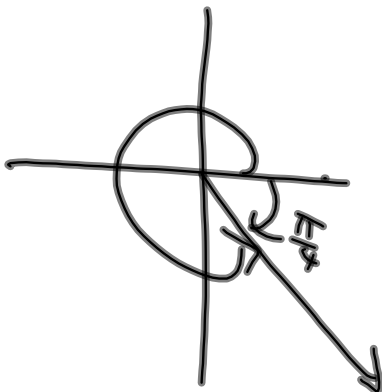
[B] $\frac{\pi}{4}$

[C] $-\frac{\pi}{4}$

[D] $\frac{7\pi}{4}$

$-\frac{24\pi}{4} - \frac{\pi}{4}$

$-\frac{6\pi}{\text{even}} - \frac{\pi}{4}$



Pg. 215-217

1-6

Textbook
Review

12, 13, 14, 15, 16, 18, 20, 21, 23