

$$(2x^3 - y^4)^{17}$$

What is numerical  
coefficient when  
variable part is  
 $x^{18} y^{44}$ ?

$$\binom{17}{6} (2x^3)^6 (-y^4)^{11}$$

$$(12376) \times 64 \times -1$$

$$\underline{-792064}$$

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#8 b)  $-4x^3 - 7x^2 + 16x + 16$

$$-4(x^3 + x^2 - 4x - 4)$$

$x = -1$   $-1 + 1 + 4 - 4 = 0$

$\therefore (x+1)$  is factor

$$\begin{array}{r|rrrr} 1 & 1 & 1 & -4 & -4 \\ & & 1 & 0 & -4 \\ \hline & 1 & 0 & -4 & 0 \end{array}$$

$$-4(x+1)(x^2-4)$$

$$-4(x+1)(x-2)(x+2)$$

Pg. 548

$$\#15) \left(y - \frac{2}{y^2}\right)^5$$

$$\begin{aligned} &= {}_5C_0 (y)^5 \left(-\frac{2}{y^2}\right)^0 + {}_5C_1 (y)^4 \left(-\frac{2}{y^2}\right)^1 + {}_5C_2 (y)^3 \left(-\frac{2}{y^2}\right)^2 \\ &+ {}_5C_3 (y)^2 \left(-\frac{2}{y^2}\right)^3 + {}_5C_4 (y)^1 \left(-\frac{2}{y^2}\right)^4 + {}_5C_5 (y)^0 \left(-\frac{2}{y^2}\right)^5 \\ &= 1y^5 - 10y^2 + 40y^{-1} - 80y^{-4} + 80y^{-7} - 32y^{-10} \end{aligned}$$

## Warm Up

1. Simplify:  $\frac{\left(\frac{1}{x^2} - \frac{1}{9}\right)}{x-3} \div \frac{1}{x-3}$

$$= \frac{\left(\frac{1}{x^2} - \frac{1}{9}\right) \cdot \frac{1}{x-3}}{\frac{1}{x-3}}$$

$$= \frac{\left(\frac{9-x^2}{9x^2}\right) \cdot \frac{1}{x-3}}{\frac{1}{x-3}}$$

$$= \frac{\cancel{9} \cdot \cancel{x} \cdot (3+x)}{9x^2} \cdot \frac{1}{\cancel{x-3}} = \frac{-1(3+x)}{9x^2} = \frac{-3-x}{9x^2}$$

2. Factor each of the following:

$x^{27} - 1$        $(x^2+1)^{\frac{1}{2}} + 3(x^2+1)^{\frac{1}{2}}$

$$(x^9-1)(x^18+x^9+1)$$

$$(x^3-1)(x^6+x^3+1)(x^{18}+x^9+1)$$

$$(x-1)(x^2+x+1)(x^6+x^3+1)(x^{18}+x^9+1)$$

$3 \approx 3^7 + 12 \approx 9$   
 $3 \approx 3^7 + 12 \approx 9$   
 $(1 + 4 \approx 2)$

$\frac{(x^2+1)^{\frac{1}{2}} + 3(x^2+1)^{\frac{1}{2}}}{(x^2+1)^{\frac{1}{2}}}$        $\frac{(x^2+1)^{\frac{1}{2}}}{(x^2+1)^{\frac{1}{2}}}$

$$(x^2+1)^{-\frac{1}{2}} [(x^2+1)^1 + 3(1)]$$

$$(x^2+1)^{-\frac{1}{2}} (x^2+4)$$

$\frac{m^{\frac{1}{2}}}{m^{\frac{1}{2}}} = m^0 = 1$

$\frac{(a+b)(a-b)}{a^2-b^2}$  Rationalize the denominator:  $\frac{x+2}{\sqrt{x-4}-\sqrt{x-6}}$

$$\frac{x+2}{\sqrt{x-4}-\sqrt{x-6}} \cdot \frac{\sqrt{x-4}+\sqrt{x-6}}{\sqrt{x-4}+\sqrt{x-6}}$$

$$= \frac{(x+2)(\sqrt{x-4}+\sqrt{x-6})}{(x-4) - (x-6)}$$

$$= \frac{(x+2)(\sqrt{x-4}+\sqrt{x-6})}{2}$$

conjugate

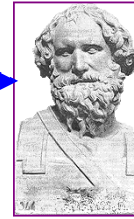
# Limits

## What is meant by a limit in Mathematics?

Let's explore and find out!

I bet he knows something about limits

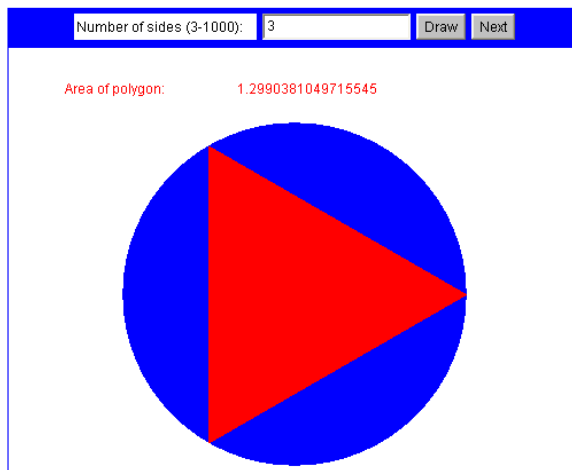
Archimedes



Have a look at these two scenarios:

### Determining the area of a circle using polygons

Approximating the area of a unit circle with regular polygons



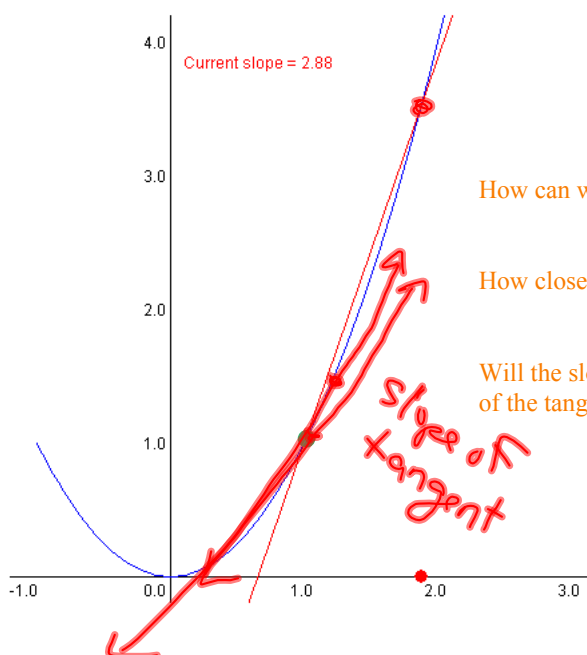
What should the area actually equal?

Will it ever equal this value?

What is the limit of the area of the polygon?

### Determining the slope of a tangent to a curve

Secant line approximations to the tangent line



How can we find the slope of a secant?

How close to the point  $x = 1$  should we choose?

Will the slope of the secant ever equal the exact slope of the tangent?