

Quiz Tomorrow :

1) Classifying as Rational or Irrational

a) $\sqrt{72}$

\bar{Q}

b) $\sqrt{225}$

Q

c) $\sqrt[4]{81}$

Q

2) Use Power & Radical function on calculator...

ex. Order Least to Greatest

$\sqrt[2]{108}$

≈ 2.55

$\sqrt[4]{10}$

≈ 9.49

$\sqrt[3]{58}$

≈ 3.87

$(3.71)^{-0.38}$

≈ 0.61

3/ Simplifying Radicals...

ex.

$$\frac{\sqrt{75}}{\sqrt{25} \cdot \sqrt{3}}$$
$$5\sqrt{3}$$

$$\frac{\sqrt{300}}{\sqrt{100} \cdot \sqrt{3}}$$
$$10\sqrt{3}$$

$$4\sqrt{18}$$
$$4(\sqrt{9} \cdot \sqrt{2})$$
$$4(3\sqrt{2})$$
$$12\sqrt{2}$$

$$6\sqrt{108}$$
$$6(\sqrt{36} \cdot \sqrt{3})$$
$$6(6\sqrt{3})$$
$$36\sqrt{3}$$

$$\sqrt[3]{54}$$
$$\sqrt[3]{27} \cdot \sqrt[3]{2}$$
$$3\sqrt[3]{2}$$

$$2\sqrt[5]{96}$$

$2^5 = 32$

$$2(\sqrt[5]{32} \cdot \sqrt[5]{3})$$
$$2(2\sqrt[5]{3})$$
$$= 4\sqrt[5]{3}$$

4/ Express as Entire Radicals...

$$\begin{aligned} \underline{\text{ex}} \text{ ① } & 3\sqrt{2} \\ &= \sqrt{3^2 \cdot 2} \\ &= \sqrt{18} \end{aligned}$$

$$\begin{aligned} \text{② } & 5\sqrt{8} \\ &= \sqrt{5^2 \cdot 8} = \sqrt{200} \end{aligned}$$

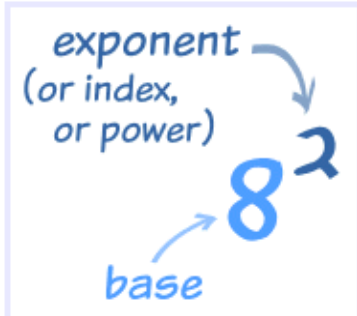
$$\text{③ } 4\sqrt[3]{2}$$

$$\begin{aligned} & \sqrt[3]{4^3 \cdot 2} \\ & \sqrt[3]{128} \end{aligned}$$

$$\text{④ } -3\sqrt[6]{5} \quad 3 \times 3 \times 3 \times 3$$

$$\begin{aligned} &= -\sqrt[6]{3^6 \cdot 5} \\ &= -\sqrt[6]{3645} \end{aligned}$$

Laws of Exponents



The exponent of a number says **how many times to multiply** the number.

In this example: $8^2 = 8 \times 8 = 64$

- In words: 8^2 could be called "8 to the second power", "8 to the power 2" or simply "8 squared"

Product Law:

The law that $x^m \cdot x^n = x^{m+n}$

With $x^m x^n$, how many times will you end up multiplying "x"? *Answer:* first "m" times, then **by another** "n" times, for a total of "m+n" times.

Example: $x^2 x^3 = (xx) \times (xxx) = xxxxx = x^5$

So, $x^2 x^3 = x^{(2+3)} = x^5$

The multiplication law states that when multiplying two powers with the same base we add the exponents.

$$(y^3)(y^2) = y^5$$

These have the same base.

$$(y^3)(y^2) = y^5$$

The five comes from the addition of three and two... ($2 + 3 = 5$)

Why Add?

ex. 1) $w^7 \cdot w^8 = w^{15}$

2) $1x^2 \cdot 1x^1 \cdot \underline{3x^8} = 3x^{11}$

3) $7^2 \cdot 7^{15} = 7^{17}$

4) $(-2a^3b^6)(5a^4b^9) = -10a^7b^{15}$

Quotient Law:

The law that $x^m/x^n = x^{m-n}$ OR $\frac{x^m}{x^n}$ OR $x^m \div x^n$

Like the previous example, how many times will you end up multiplying "x"? Answer: "m" times, then **reduce that** by "n" times (because you are dividing), for a total of "m-n" times.

Example: $x^{4-2} = x^4/x^2 = (xxxx) / (xx) = xx = x^2$

$$\frac{\cancel{xx}\cancel{xx}}{\cancel{xx}} = x^2$$

(Remember that $x/x = 1$, so every time you see an x "above the line" and one "below the line" you can cancel them out.)

The division law states that when dividing powers with the same base we subtract the exponents.

$$\frac{y^{12}}{y^3} = y^9$$

Division $\frac{y^4}{y^3} = y^1$

Same Base

Subtract
 $4 - 3 = 1$

Why does this work?

2. Simplify each of the following using the division law.

$$\text{a. } \frac{x^8}{x^5}$$

$$= x^3$$

$$\text{b. } \frac{y^7}{y^9}$$

$$= y^{-2}$$

$$\text{c. } \frac{15x^5}{3x^2}$$

$$= 5x^3$$

$$\text{d. } \frac{100x^{13}}{25x^7}$$

$$= 4x^6$$

What about these?

$$\frac{15m^9}{4m^3}$$

$$= \frac{15}{4} m^6$$

$$\frac{(4x^3)(3x^4)}{4x^2}$$

$$= \frac{12x^7}{4x^2}$$

$$= 3x^5$$

$$\frac{24a^{10}b^6}{4a^2b^{12}}$$

$$= 6a^8b^{-6}$$

$$10^6 \times 10^{22} \div 10^3 \cdot 10^4$$

$$= 10^{28} \div 10^3 \cdot 10^4$$

$$= 10^{25} \cdot 10^4$$

$$= 10^{29}$$

Attachments

applications of sequences.doc