

Warm Up

Prove the following identity:

$$\frac{\sin x}{1 - \cos x} - \frac{\sin x \cos x}{1 + \cos x} = \underline{\csc x} \underline{(1 + \cos^2 x)}$$

LS

$$\frac{\sin x (1 + \cos x) - \sin x \cos x (1 - \cos x)}{(1 - \cos x)(1 + \cos x)}$$

$$\frac{\sin x + \cancel{\sin x \cos x} - \cancel{\sin x \cos x} + \sin x \cos^2 x}{1 - \cos^2 x}$$

$$\frac{\cancel{\sin x} (1 + \cos^2 x)}{\sin x}$$

$$\csc x (1 + \cos^2 x)$$

LS = RS

Prove the following identities:

#1. $\frac{1}{\sin^2 x} + \frac{1}{\cos^2 x} = \frac{1}{\sin^2 x \cos^2 x}$

LS

$$\frac{\cos^2 x + \sin^2 x}{\sin^2 x \cos^2 x}$$

$$\frac{1}{\sin^2 x \cos^2 x} \quad \underline{LS=RS}$$

#2. $\frac{\csc \theta}{\cot^2 \theta} = \tan \theta \sec \theta$

LS

$$\frac{\left(\frac{1}{\sin \theta}\right)}{\left(\frac{\cos^2 \theta}{\sin^2 \theta}\right)}$$

RS

$$\left(\frac{\sin \theta}{\cos \theta}\right) \left(\frac{1}{\cos \theta}\right)$$

$$\frac{\sin \theta}{\cos^2 \theta}$$

LS

$$\left(\frac{1}{\sin \theta}\right) \cdot \left(\frac{\sin^2 \theta}{\cos^2 \theta}\right)$$

$$\frac{\sin \theta}{\cos^2 \theta}$$

RS

$$\left(\frac{\sin \theta}{\cos \theta}\right) \frac{1}{\cos \theta}$$

and sec θ

#3. $\tan^2 \theta + \sin^2 \theta = (\sec \theta + \cos \theta)(\sec \theta - \cos \theta)$

LS

$$(\sec^2 \theta - 1) + (1 - \cos^2 \theta)$$

$$\sec^2 \theta - 1 + 1 - \cos^2 \theta$$

$$\sec^2 \theta - \cos^2 \theta$$

LS=RS

RS

$$\sec^2 \theta - \cos^2 \theta$$

$1 + \tan^2 \theta = \sec^2 \theta$
 $\tan^2 \theta = \sec^2 \theta - 1$
 $\sin^2 \theta + \cos^2 \theta = 1$
 $\sin^2 \theta = 1 - \cos^2 \theta$

Warm Up

Prove the following identities...

#1. $\tan \alpha + \cot \alpha = \sec \alpha \csc \alpha$

$$\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta} \quad \left(\frac{1}{\cos \theta} \right) \left(\frac{1}{\sin \theta} \right)$$

$$\frac{\sin^2 \theta + \cos^2 \theta}{\cos \theta \sin \theta} \quad \frac{1}{\cos \theta \sin \theta}$$

$$\frac{1}{\cos \theta \sin \theta}$$

$\text{RHS} = \text{LHS}$

#2. $\tan \theta + \tan^3 \theta = \frac{1}{\cot \theta \cos^2 \theta}$

$$\tan \theta (1 + \tan^2 \theta) \quad \text{OR} \quad \frac{\text{RS}}{\text{LS}}$$

$$\tan \theta \sec^2 \theta \quad \tan \theta \sec^2 \theta$$

$$\left(\frac{1}{\cos \theta} \right) \left(\frac{1}{\cos^2 \theta} \right) \quad \tan \theta (1 + \tan^2 \theta)$$

$$\frac{1}{\cos \theta \cos^2 \theta} \quad \tan \theta + \tan^3 \theta$$

$\sin \theta (1 - \sin^2 \theta)$

#3. $\frac{1}{\sec^2 \theta \cot \theta} = \frac{\sin \theta - \sin^3 \theta}{\cos \theta}$

LS

$$\cos^2 \theta \tan \theta$$

$$\frac{\cos^2 \theta \sin \theta}{\cos \theta}$$

$$(\cos \theta \sin \theta)$$

LS = RS

RS

$$\frac{\sin \theta (1 - \sin^2 \theta)}{\cos \theta}$$

$$\frac{\sin \theta \cos^2 \theta}{\cos \theta}$$

$$\sin \theta \cos \theta$$

$(\sec \theta \cos \theta) \sec \theta$

HOMework...

Worksheet - Trig Identities #1.doc



Do questions #2 - 27

Attachments

Worksheet - Trig Identities #1.doc