

Let's try a couple more examples using monomial denominators
require finding a common denominator...

$$\frac{5a}{2b} - \frac{1}{2b}$$

$$\frac{(a+4)(5a^2) + (2a-1)(3a)}{15a^3} + \frac{(2a-1)(3a)}{15a^3}$$

$$\frac{5a^3 + 20a^2 + 6a^2 - 3a}{15a^3}$$

$$\frac{5a^3 + 26a^2 - 3a}{15a^3}$$

$$\cancel{a} \frac{(5a^2 + 26a - 3)}{15a^3}$$

$$\frac{a+4}{3a} + \frac{2a-1}{5a^2}$$

$$\frac{(a+4)(5a) + (2a-1)(3)}{15a^2} + \frac{(2a-1)(3)}{15a^2}$$

$$\frac{5a^2 + 20a + 6a - 3}{15a^2} + \frac{6a - 3}{15a^2}$$

$$\frac{5a^2 + 26a - 3}{15a^2}$$

$$\frac{a(3a^3)}{a^3 b}$$

$$\frac{a}{b}$$

$$\frac{2}{3} + \frac{5}{12}$$

$$\frac{8}{12} + \frac{5}{12}$$

$$\frac{13}{12}$$

$$\frac{24}{36} + \frac{15}{36}$$

$$\frac{39}{36}$$

$$\frac{13}{12}$$

Adding/Subtracting Rational Expressions

$$\frac{2}{7} + \frac{3}{4}$$

$$\frac{2(4)}{(7)(4)} + \frac{3(7)}{(7)(4)}$$

$$\frac{3}{5} - \frac{4}{25}$$
~~$$\frac{15}{25} - \frac{4}{25}$$

$$\frac{11}{25}$$~~

$$\frac{3}{5} - \frac{4}{(5)(5)}$$

$$\frac{3(5) - 4}{(5)(5)}$$

$$\frac{15 - 4}{25}$$

$$\frac{11}{25}$$

$$\frac{1}{3} + \frac{1}{12}$$

$$\frac{4}{12} + \frac{1}{12}$$

$$\frac{5}{12}$$

3, 6, 9, (12)

$$\frac{12}{36} + \frac{3}{36}$$

$$\frac{15}{36}$$

$$\frac{5}{12}$$

Fractions \rightarrow Add/Subtract.

$$\frac{3}{4} + \frac{2}{7}$$

$$\frac{21}{28} + \frac{8}{28}$$

$$\frac{29}{28}$$

$$\frac{3}{4} + \frac{2}{7}$$

$$\frac{3(7)}{(4)(7)} + \frac{2(4)}{(4)(7)}$$

WARM UP PASS IN

Do on your own paper

$$\frac{1}{3} \quad \textcircled{1} \quad \frac{6x^3}{-x^2} \cdot \frac{x^5}{18x} \div \frac{8}{6x^6}$$

$$\frac{1}{4} \quad \textcircled{2} \quad \frac{x^2+7x}{x^2-1} \cdot \frac{x^2+3x+2}{x^2+14x+49}$$

$$\frac{1}{6} \quad \textcircled{3} \quad \frac{x^2-4}{2x^2+11x+5} \cdot \frac{2x+3}{x^2-x-6} \cdot \frac{x^2+2x-15}{20x^3+30x^2}$$

5d)

$$\frac{\frac{4z}{xy} - \frac{9x}{yz}}{xyz} = \frac{\frac{4z^2}{xy^2z} - \frac{9x^2}{y^2xz}}{xyz} = \frac{4z^2 - 9x^2}{xy^2z}$$

$x \neq 0$
 $y \neq 0$
 $z \neq 0$

$$\frac{(2z-3)(2z+3)}{xy^2z}$$

5b)

$$\frac{3}{2x} + \frac{1}{6} = \frac{9}{6x} + \frac{1x}{6x} = \frac{9+x}{6x}$$

$x \neq 0$

5f)

$$\frac{6xy}{a^2b} - \frac{2x}{ab^2y} + \frac{1}{a^2b^2y}$$

$$\frac{6xy^2b}{a^2b^2y} - \frac{2xa}{a^2b^2y} + \frac{a^2b^2y}{a^2b^2y}$$

$$\frac{6xy^2b - 2xa + a^2b^2y}{a^2b^2y}$$

P 327
#10

$n-2$

$$\frac{n^2-4}{n+1} \div n-2$$

$$\frac{(n-2)(n+2)}{n+1} \cdot \frac{1}{n-2}$$

$\frac{n+2}{n+1}$ ← thickness

$$\frac{2}{(x+3)} + \frac{4}{(x-5)}$$
$$\frac{2(x-5) + 4(x+3)}{(x+3)(x-5)}$$
$$\frac{2x-10+4x+12}{(x+3)(x-5)}$$
$$\frac{6x+2}{(x+3)(x-5)}$$
$$\frac{2(x+1)}{(x+3)(x-5)}$$

4

11c length = $2x-3$
 width = $x+1$
 height = ?
 Volume = x^2+2x+1

$V = lwh$
 $\frac{V}{lw} = h$

$$\frac{x^2+2x+1}{(2x-3)(x+1)}$$

$$\frac{\cancel{(x+1)}\cancel{(x+1)}}{(2x-3)\cancel{(x+1)}} \quad h = \frac{x+1}{2x-3}$$

What if the denominators are not monomials???

$$\frac{2}{x-2} - \frac{5}{x+8}$$

$\frac{2(x+8)}{(x-2)(x+8)} - \frac{5(x-2)}{(x-2)(x+8)}$

$$\frac{2x+16 - 5x+10}{(x-2)(x+8)}$$

$$\frac{-3x+26}{(x-2)(x+8)}$$

$\frac{4}{x^2-16} + \frac{3}{x^2+8x+16}$

$$\frac{4}{x^2-16} + \frac{3}{x^2+8x+16}$$

$\frac{3}{20} + \frac{3}{25}$

$$\frac{4}{(x-4)(x+4)} + \frac{3}{(x+4)(x+4)}$$

$$\frac{4(x+4) + 3(x-4)}{(x-4)(x+4)(x+4)}$$

$$\frac{4x+16+3x-12}{(x-4)(x+4)^2} = \frac{7x+4}{(x-4)(x+4)^2}$$

Try

$$\frac{7}{x^2+6x+8} - \frac{4}{x^2+7x+12}$$

$$\frac{7}{(x+2)(x+4)} - \frac{4}{(x+3)(x+4)}$$

$$\frac{7(x+3) - 4(x+2)}{(x+2)(x+4)(x+3)}$$

$$\frac{7x+21-4x-8}{(x+2)(x+4)(x+3)}$$

$$\frac{3x+13}{(x+2)(x+4)(x+3)}$$

$$\frac{3}{20} + \frac{3}{25} \rightarrow 100$$

$$\frac{3}{(4)(5)} + \frac{3}{(5)(4)}$$

$$(4)(5)(5)$$

$$\frac{1}{12} + \frac{1}{15}$$

$$\frac{\cancel{3}}{(3)(4)} + \frac{\cancel{3}}{(3)(5)}$$

$$\frac{\quad}{(3)(4)(5)}$$

$$\frac{1}{x^2+7x+12} + \frac{1}{x^2+6x+8}$$

$$\frac{1}{(x+3)(x+4)} + \frac{1}{(x+4)(x+2)} \quad x \neq -3, -4, -2$$

$$\frac{1(x+2) + 1(x+3)}{(x+3)(x+4)(x+2)}$$

$$\frac{x+2+x+3}{(x+3)(x+4)(x+2)}$$

$$\frac{2x+5}{(x+3)(x+4)(x+2)}$$

$$\frac{1}{8} + \frac{1}{15} = \frac{\quad}{120}$$

$$\frac{1}{(2)(4)} + \frac{1}{(3)(5)}$$

$$\frac{1}{3} + \frac{1}{12} = \frac{\quad}{12}$$

$$\frac{1}{(3)} + \frac{1}{(3)(4)}$$

~~(2)(2)~~
~~(3)(4)~~

$$(3)(4)$$

$$\frac{1}{12} - \frac{2}{15}$$

$$\frac{1}{(4)(3)} - \frac{2}{(3)(5)}$$

$$\overline{60}$$

$$\overline{(4)(3)(5)}$$

$$\frac{2}{7} + \frac{3}{4}$$

$$\frac{2(4)}{(7)(4)} + \frac{3(7)}{(7)(4)}$$

Page 334 #1, 5, 6

Remember to ALWAYS factor everywhere possible FIRST!!!

$$\frac{\frac{2}{w} - \frac{3}{w-1} + \frac{2}{w+2}}{\frac{2}{w(w-1)(w+2)} - \frac{3w}{w(w-1)(w+2)} + \frac{2w}{w(w-1)(w+2)}}$$

$$\frac{2w^2 + 2w - 4 - 3w^2 - 6w + 2w^2 - 2w}{w(w-1)(w+2)}$$

$$\frac{w^2 - 6w - 4}{w(w-1)(w+2)}$$

$$\frac{4}{y^2 - 4} - \frac{2}{y + 2}$$

$$\frac{4}{(y-2)(y+2)} - \frac{2}{y+2}$$

$$\frac{4 - 2(y-2)}{(y-2)(y+2)}$$

$$\frac{4 - 2y + 4}{(y-2)(y+2)}$$

$$\frac{-2y + 8}{(y-2)(y+2)}$$

$$\frac{-2(y-4)}{(y-2)(y+2)}$$

Try these examples...Remember to **FACTOR** first!

$$\frac{x+2}{x^2-6x+5} - \frac{5}{x^2+2x-35}$$

$$\frac{2x}{x^2+4x-12} + \frac{3}{5x^4-20x^2}$$

Do you really understand?? ...Let's find out...

$\frac{2x-3}{3x^2} + \frac{3x+3}{3x^2}$

$\frac{3x^2}{3x^2} + \frac{9x}{3x^2} + \frac{3(x+1)}{3x^2}$

$\frac{3x^2}{3x^2} + \frac{3x^2}{3x^2} + \frac{3x^2}{3x^2} + \frac{3x^2}{3x^2} + \frac{3x^2}{3x^2} + \frac{3x^2}{3x^2} + \frac{3x^2}{3x^2} + \frac{3x^2}{3x^2}$

$\frac{4y}{y^2-1} - \frac{2}{y} - \frac{y+1}{y+1}$

Factor $\frac{4y}{(y-1)(y+1)} - \frac{2}{y} - \frac{y+1}{y+1}$

$\frac{4y(y)}{y(y-1)(y+1)} - \frac{2(y)(y)}{y(y-1)(y+1)} - \frac{2(y)(y+1)}{y(y-1)(y+1)}$

$\frac{4y^2}{y(y-1)(y+1)} - \frac{2y^2}{y(y-1)(y+1)} - \frac{2y^2+2y}{y(y-1)(y+1)}$

$\frac{4y^2-2y^2-2y^2-2y}{y(y-1)(y+1)}$

$\frac{-2y^2-2y}{y(y-1)(y+1)}$

$\frac{-2y(y+1)}{y(y-1)(y+1)}$

$\frac{-2}{y-1}$

$\frac{2x}{(x-2)(x+2)} + \frac{3x}{(x+1)} - \frac{3}{(x-1)(x+1)}$

Factor $\frac{(2x-1)(2x+1)}{(x-1)(x+1)} - \frac{3x-3}{(x-1)(x+1)}$

$\frac{2x^2-5x-3}{(x-1)(x+1)} - \frac{(x-3)(x+1)}{(x-1)(x+1)}$

$\frac{2x^2-5x-3-(x^2-2x-3)}{(x-1)(x+1)}$

$\frac{x^2-3x}{(x-1)(x+1)}$

$\frac{x(x-3)}{(x-1)(x+1)}$

$\frac{2x}{(x-2)(x+2)} - \frac{1}{x^2} + \frac{x^2+1}{x^2(x-2)^2}$

$\frac{2x(x^2-1)(x+2)}{x^2(x-2)^2} - \frac{1(x-2)(x+2)}{x^2(x-2)^2} + \frac{(x^2+1)(x-2)}{x^2(x-2)^2}$

$\frac{2x(x^2-1)(x+2) - (x-2)(x+2) + (x^2+1)(x-2)}{x^2(x-2)^2}$

$\frac{2x^3-2x(x^2-1)(x+2) - (x-2)(x+2) + (x^2+1)(x-2)}{x^2(x-2)^2}$

$\frac{2x^3-2x^3+2x(x+2) - (x-2)(x+2) + (x^2+1)(x-2)}{x^2(x-2)^2}$

$\frac{2x^2+4x-4 - (x^2-4) + (x^2-x-2)}{x^2(x-2)^2}$

$\frac{2x^2+4x-4-x^2+4+x^2-x-2}{x^2(x-2)^2}$

$\frac{3x^2+3x-2}{x^2(x-2)^2}$

$\frac{(x+2)(3x-1)}{x^2(x-2)^2}$

easier

harder → common denominator

Bedmas

brackets
ponents
ide
ultiply
dd
ubtract

$$\frac{-1}{2} = -\frac{1}{2} = \frac{1}{-2}$$

Practice Problems...

Page 336 - 339

#1, 3, 5, 6, 7, 8,

Attachments

Mathematical Pathways Description.docx

Pre-Calculus 110 - Fall 2012.doc