

Introduction to Trigonometric Equations

trigonometric equation

- an equation involving trigonometric ratios

Focus on...

- algebraically solving first-degree and second-degree trigonometric equations in radians and in degrees
- verifying that a specific value is a solution to a trigonometric equation
- identifying exact and approximate solutions of a trigonometric equation in a restricted domain
- determining the general solution of a trigonometric equation

Did You Know?

In equations, mathematicians often use the notation $\cos^2 \theta$. This means the same as $(\cos \theta)^2$.

Let's start with basic LINEAR trigonometric equations...

Solve: $\sin \theta = 0.9659$, $-360^\circ < \theta < 720^\circ$

...Pre-Calculus 110

- Reference angle?
- Which quadrants?
- Any co-terminal angles acceptable?

- If the domain is in degrees, give solutions in degrees.
- If the domain is in radians, give solutions in radians.

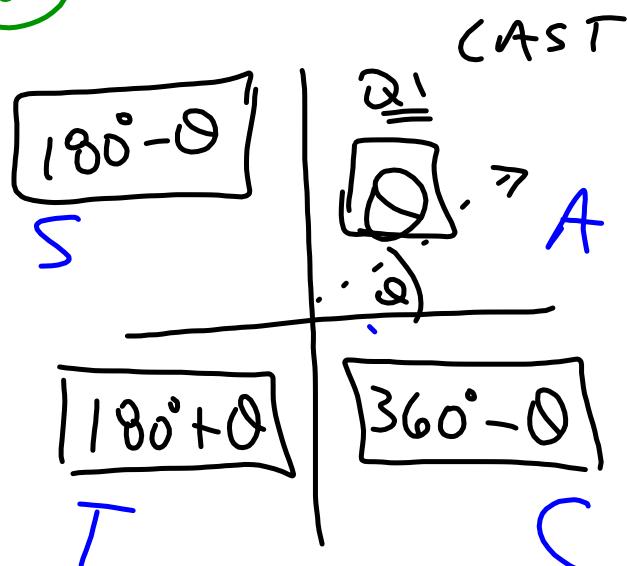
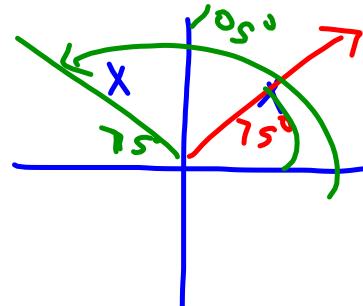
$\theta = 75^\circ$

$+360^\circ$ -360°

$+360^\circ$ $+360^\circ$

$= 435^\circ$ $= 105^\circ$

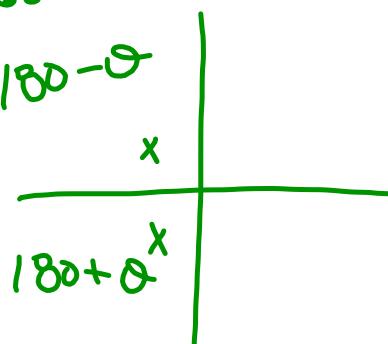
$= -285^\circ$ $= -255^\circ$



Solve: $\sec \theta = -1.3054, -2\pi \leq \theta \leq 2\pi$

(Ref $\triangle 40^\circ$, Q2, 3)

* Ignore Negative
When finding Reference
Angle!!!



$$\theta = 140^\circ, 220^\circ, -220^\circ, -140^\circ$$

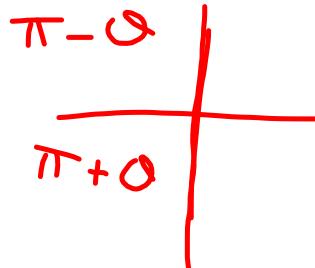
$$\theta = \frac{140\pi}{180}, \frac{220\pi}{180}, -\frac{220\pi}{180}, -\frac{140\pi}{180}$$

$$\theta = \pm \frac{7\pi}{9}, \pm \frac{11\pi}{9}$$

Solution)

$$\sec \theta = -1.3054, -2\pi \leq \theta \leq 2\pi$$

(Ref $\triangle 0.698$, Q2, 3)



$$Q2 \Rightarrow 2.444 (\pi - 0.698)$$

$$Q3 \Rightarrow 3.840 (\pi + 0.698)$$

$$\dots \text{other 2} (-2\pi)$$

$$\theta = -3.843$$

$$\theta = -2.44$$

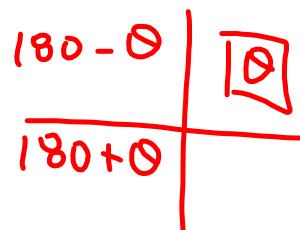
Ex. $\sqrt{2} \cos \theta + 1 = 0, -360^\circ \leq \theta \leq 720^\circ$

$$\frac{\sqrt{2} \cos \theta}{\sqrt{2}} = -\frac{1}{\sqrt{2}}$$

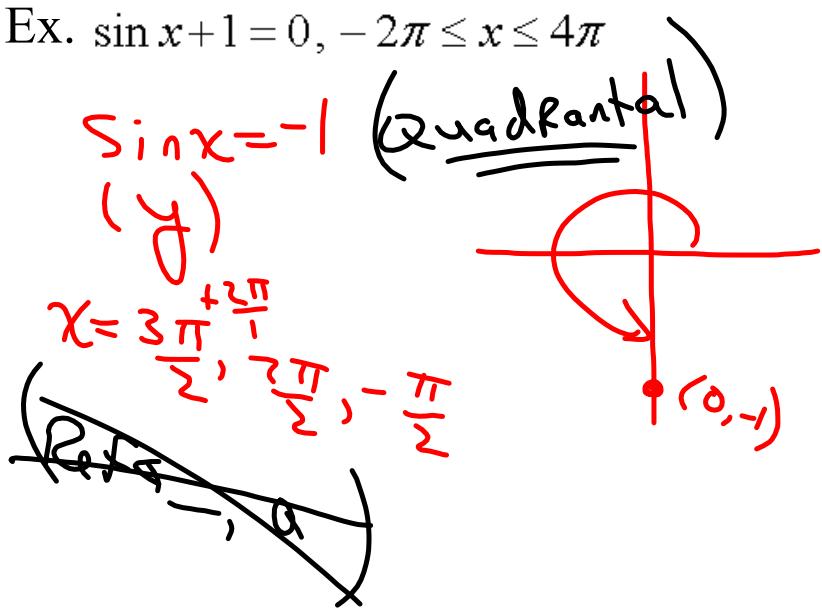
$$\cos \theta = -\frac{1}{\sqrt{2}}$$

(Ref & 45° , Q2,3)

$$\theta = 435^\circ, 225^\circ, 495^\circ, 585^\circ$$



$$\text{Ex. } \sin x + 1 = 0, -2\pi \leq x \leq 4\pi$$



Your Turn

Solve each trigonometric equation in the specified domain.

a) $3 \cos \theta - 1 = \cos \theta + 1, -2\pi \leq \theta \leq 2\pi$

b) $4 \sec x + 8 = 0, 0^\circ \leq x < 360^\circ$

$$\text{a)} 3 \cos \theta - 1 = \cos \theta + 1 \Rightarrow 3m - 1 = m + 1$$

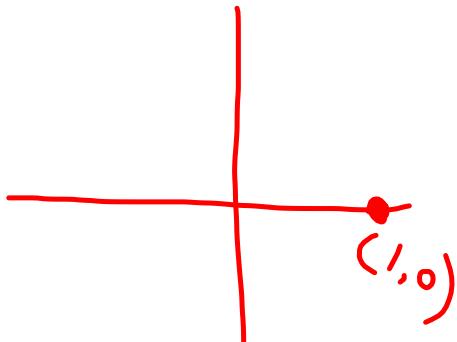
$$3 \cos \theta - \cos \theta = 1 + 1$$

$$\frac{2 \cos \theta}{2} = 2$$

$$\cos \theta = 1$$

$$(x \Rightarrow 1)$$

$$\theta = 0^\circ, 2\pi$$



b) $4 \sec x + 8 = 0, 0^\circ \leq x < 360^\circ$

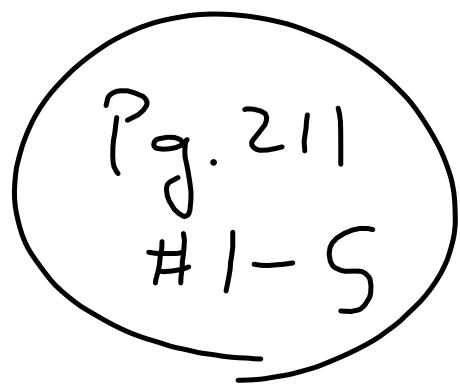
$$\frac{4 \sec x}{4} = -\frac{8}{4}$$

$$\sec x = -2$$

$$\cos x = -\frac{1}{2}$$

$$\left(\text{Ref } \cancel{\frac{60^\circ}{2}}, Q_2, 3\right)$$

$$\underline{\theta = 120^\circ, 240^\circ}$$



Attachments

Worksheet - Sketching Angles in Radians.doc

Warm-Up - Intro to Limits.docx