## Warm Up

1. During a recent home renovation Abby finds an old financial statement that belonged to her grandfather. The document has faded and some of the dates are difficult to read. She can see that her grandfather deposited \$10000 on June 30, 1944. The balance of the investment at the time of this statement is \$107651.63, however, the date has been smudged out. If this money was invested at 8%/a and compounded quarterly, what must have been the date on this statement?

2. "Lenny the loan shark" gives out a \$500 loan to a client. Lenny lends the money at 32%/a simple interest, and demands that he is repaid in 30 days...OR ELSE!!! How much must be paid to "Lenny the loan shark" 30 days later?

$$I = Prt$$

$$I = S00(0.32)(\frac{30}{365})$$

$$I = $13.15$$

$$Owe: $513.15$$



1+2+3+4+5+---+100 5050

# **Series**

#### **Summation Notation:**

The capital Greek letter sigma  $\sum$  is used to provide a shorthand notation for a summation.

In summation notation, the sum of the terms of the sequence  $\{a_1, a_2, a_3, ..., a_n\}$ 

is denoted 
$$\sum_{k=1}^{n} a_k = \alpha_1 + \alpha_2 + \alpha_3 + \cdots + \alpha_n$$

which is read "the sum of  $a_k$  from k = 1 to n"

Sigma notation is actually more widely used than the above definition suggests.

See if you can evaluate each of the following summations:

## **Arithmetic Series:**

• The summation of the terms of an arithmetic sequence

Formula 
$$S_n = \frac{n}{2} [2a + (n-1)d]$$

Let's derive this formula that can be used to determine the sum of "n" terms in any arithmetic series...

$$S = a + (a+d) + (a+2d) + (a+3d) + \dots + [a+(n-2)d] + [a+(n-1)d]$$

$$S = a + (n-1)d + a + (n-2)d + \dots + a + d + a$$

$$S = \frac{1}{2} \left( \frac{1}{2} \left( \frac{1}{2} + \frac{1}{2} \left( \frac{1}{2} + \frac{1}{2} \right) \right) \right)$$

### Example:

Evaluate the following summation:

$$-2+7+16+25+34+...+1420 =$$
Arithmetic 2<sup>nd</sup>

$$S_{n} = \frac{n}{2} \left[ 2a+(n-1)d \right]$$

$$S_{159} = \frac{159}{2} \left[ 2(-2)+(158)(9) \right]$$

$$\frac{1420}{9} = n-1$$

$$= \frac{1}{2} \left[ 2(3) + (158)(9) \right]$$

$$n = \frac{1422}{9} = n-1$$

$$= \frac{1}{2} \left[ 2(3) + (158)(9) \right]$$

$$n = \frac{1422}{9} + 1 = \frac{159}{9}$$

## Example:

A corner section of a stadium has 8 seats along the front row. Each successive row has two more seats than the row preceding it. If the top row has 24 seats, how many seats are in the entire section?

$$\frac{1}{9} = 0$$

$$\frac{1}{9} + 1 =$$