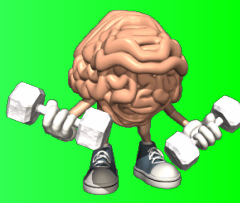


**Warm Up**



1)  $20 - 32a + 40a^3$

2)  $x^2 + 4x + 3$

3)  $-42k + 36k^2 + 30k^3$

4)  $5x^2 - 45x + 70$

5)  $4n^2 + 21n - 18$

6)  $10n^2 - n - 24$

7)  $49x^4 - 4$

8)  $x^2 + 100$

# Prime Numbers

## Prime Numbers

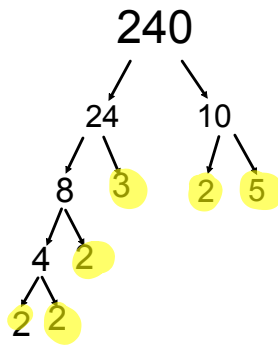
A Prime Number can be divided evenly **only** by 1 & itself.  
 And it must be a whole number greater than 1.

The first few prime numbers are 2, 3, 5, 7, 11, 13, 17 etc.....

**Determining the Prime Factors  
of a Whole Number**

Write the prime factorization of 240

Draw a Factor  
Tree !!



The Prime Factorization of 240 is:

$2 \times 2 \times 2 \times 3 \times 5 \times 2$  or  $2^4 \times 3 \times 5$

The Prime Factors of 240 are:

2, 3, & 5

240



# Warm Up



What is the greatest common factor of 144 and 216 ?

What is the least common multiple of 45 and 30 ?

**Distributing Factor**

## 3.7 Multiplying Polynomials

# Expand & Simplify



**Rainbow**



$$4x(2x + 1) - 2x(3x - 3)$$

$$8x^2 + 4x - 6x^2 + 6x$$

$$2x^2 + 10x$$

$$(x + 4)(x - 3)$$

$$\begin{array}{r} x^2 + 4x - 3x - 12 \\ \hline x^2 + x - 12 \end{array}$$

$x$	$x^2$	$+4x$
$-3$	$-3x$	$-12$

$$\begin{array}{l}
 (x+2)^2 \\
 \cancel{x^2 + 4} \\
 (x+2)(x+2) \\
 x^2 + 2x + 2x + 4 \\
 x^2 + 4x + 4
 \end{array}$$

Expand and collect like terms.

$$2x(5x+3) - 7x(6x-5)$$

$$(x + 4)(x - 3)$$

	x	+4
x	$x^2$	+ 4x
-3	-3x	-12

5)  $(10x^5 + 3)(-2x^2 - 11x + 2)$

$x^5 \cdot x^2 = x^7$  (with a crossed-out  $x^5$  term)

	$-2x^2$	$-11x$	$+2$
$\cdot 10x^5$	$-20x^7$	$-110x^6$	$+20x^5$
$+3$	$-6x^2$	$-33x$	$+6$

Expand and simplify

$$(x - 1)^2 + (x + 4)^2$$

Expand and simplify

$$6 \cdot (3)(2)$$

$$18 \cdot 2 = 36$$

$$\frac{(x-3)(x-1)(x-5)}{(x^2 - 4x + 3)} \cdot (x-5)$$

$x^2 + 3x - x + 3$



*Factoring* Simple  $1a^2 + a + \dots$   
 hard.  $4a^2 + \dots$

There are 5 different kinds of Factoring:

- Greatest common factor (GCF) *any # of terms*
- Simple Trinomials (Factor by Inspection) *3*
- Hard Trinomials (Factor by Decomposition) *3*
- Special Factors
  - \* Difference of Squares *2*  $a^2 - 4 = (a+2)(a-2)$
  - Perfect Square Trinomials *3*  $4a^2 + 20a + 25 = (2a+5)^2$

$$x^2 + 5x - 6$$

$$8x^2 - 26x - 24$$

## *Difference of Squares*

- two terms that are perfect squares.
- must be a difference
- factor like this...

$$a^2 - b^2 = (a + b)(a - b)$$

### EXAMPLES...

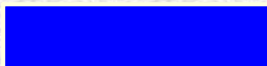
1)  $4x^2 - 49$



2)  $16x^2 - 9y^2$



3)  $81z^4 - 625$



4)  $49w^2 - 4s^2$



## Perfect Square Trinomials

- three terms: the first and last are perfect squares.
- factors like this...

$$a^2 + 2ab + b^2 = (a + b)^2$$

OR

$$a^2 - 2ab + b^2 = (a - b)^2$$

- recognize them and you save yourself the decomposition steps!!!

### EXAMPLES...

1)  $25x^2 - 10x + 1$



2)  $9x^2 + 24x + 16$



Math 10

Name \_\_\_\_\_

Factoring: Difference of Squares and Perfect Squares

Date \_\_\_\_\_

Factor each completely.

1)  $n^2 - 9$

2)  $25a^2 - 9$

3)  $k^2 - 4$

4)  $16x^2 - 9$

5)  $x^2 - 25$

6)  $25x^2 - 16y^2$

7)  $u^2 - 16v^2$

8)  $u^2 - 9v^2$

9)  $4x^2 - y^2$

10)  $a^2 - 25b^2$

11)  $9m^2 + 12m + 4$

12)  $16r^2 + 8r + 1$

13)  $25x^2 - 20x + 4$

14)  $16n^2 + 40n + 25$

15)  $9b^2 - 24b + 16$

16)  $16m^2 - 24mn + 9n^2$

17)  $9x^2 - 6xy + y^2$

18)  $25x^2 + 10xy + y^2$

19)  $x^2 - 8xy + 16y^2$

20)  $9x^2 + 24xy + 16y^2$

## Review Questions

1.  $9x^2 - y^2$

2.  $2x^2 - x - 15$

3.  $3a^2b^2 + 27a^4b^7 - 12a^6b^5$

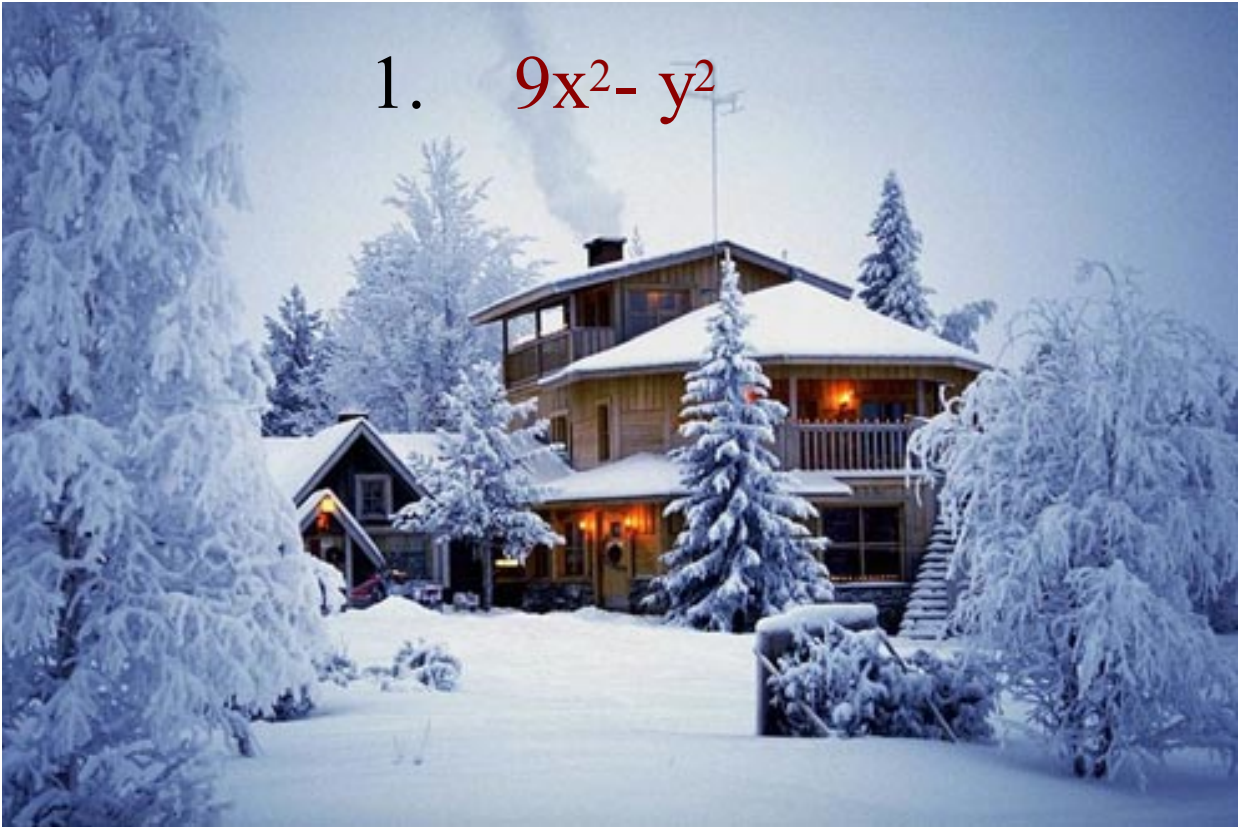
4.  $3x^2 - 27x + 42$

5.  $24x^4 + 10x^2 + 4$

**Tricky**

6.  $(x+1)^2 - (x+5)^2$

1.  $9x^2 - y^2$



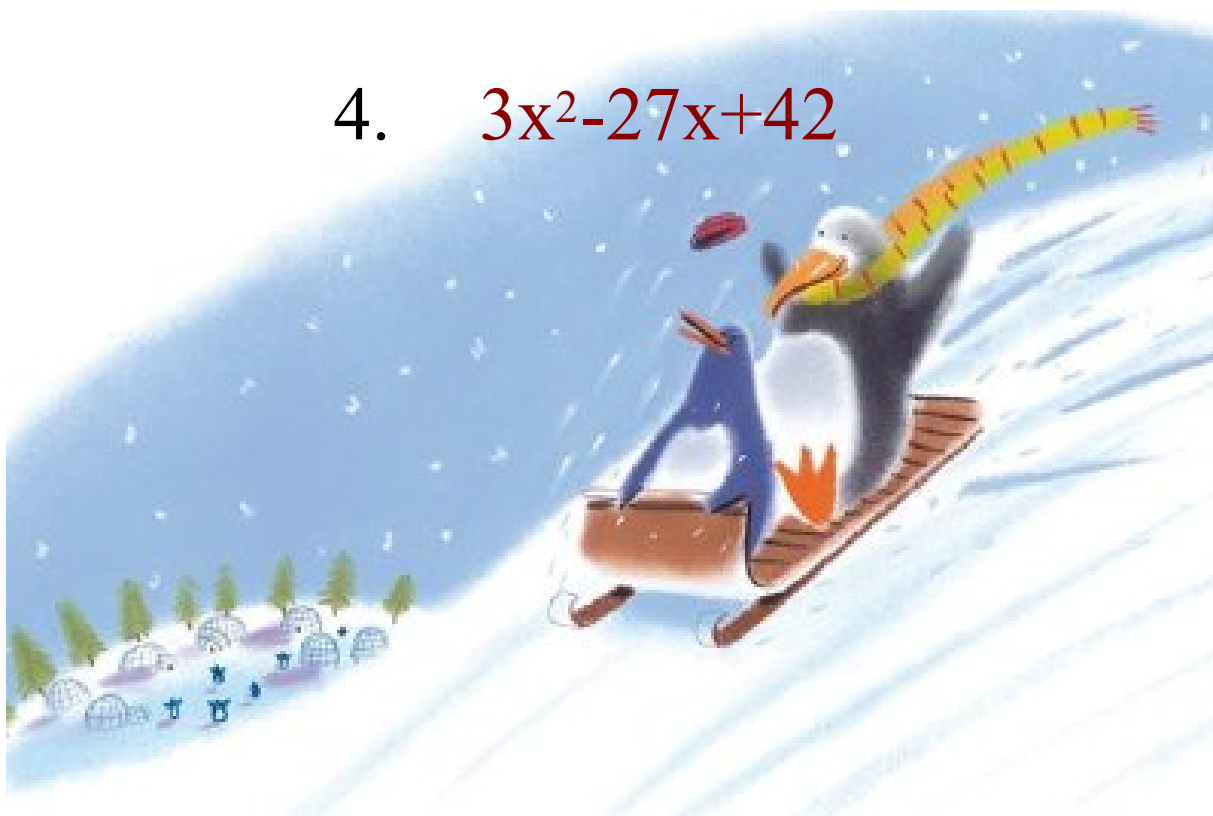
2.  $2x^2 - x - 15$



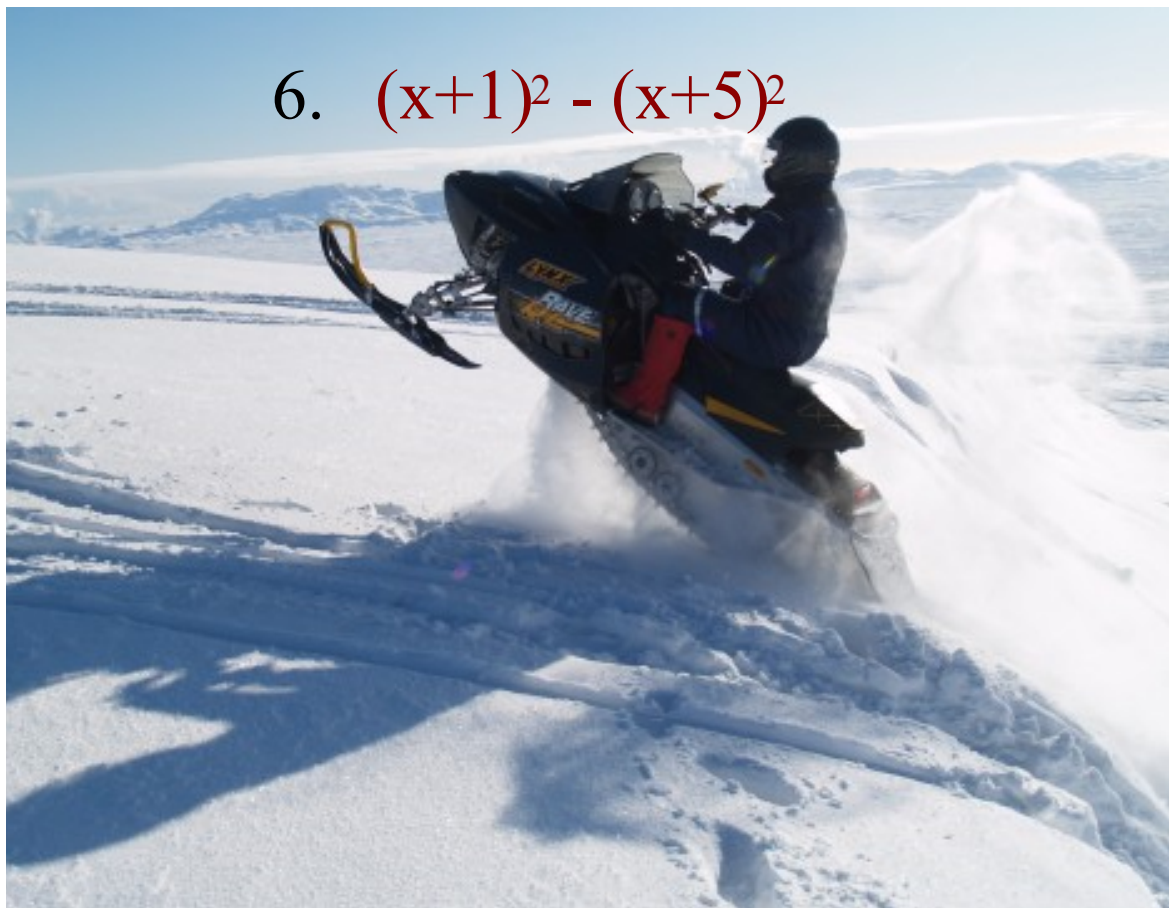
3.  $3a^2b^2+27a^4b^7-12a^6b^5$



4.  $3x^2-27x+42$



6.  $(x+1)^2 - (x+5)^2$



7.  $(x-2)^2 - 9(x+1)^2$



Factoring Review  
Math 10B

Factor each completely. :

- |                           |                               |
|---------------------------|-------------------------------|
| 1) $6b^2a^2 - 24b^2$      | 2) $3x^2 + x - 10$            |
| 3) $x^2 - 4y^2$           | 4) $m^2 - 10m - 11$           |
| 5) $25x^2 - 30x + 9$      | 6) $2n^2 - 9n + 9$            |
| 7) $15x^2 - 12y^2$        | 8) $2a^2 - 7a^2 - 20a + 70$   |
| 9) $4x^2 + 10xy + 625y^2$ | 10) $36n^2 - 32$              |
| 11) $a^2 - 9a - 36$       | 12) $6v^3 - 48v - 2v^2 + 16$  |
| 13) $-56x^3 + 80$         | 14) $9m^4 + 30m^2n^2 + 25n^4$ |
| 15) $5v^2 - 26v - 63$     | 16) $64x^2 - 36y^2$           |
| 17) $2x^2 - 2x - 40$      | 18) $4x^2 - 25$               |
| 19) $3x^2 - 17xy + 10y^2$ | 20) $40x^3 - 5x^2 - 32x + 4$  |
| 21) $25r^2 - 49$          | 22) $p^2 - 5p - 84$           |

