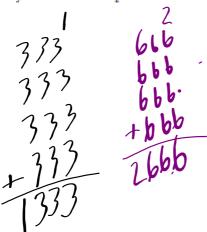
HOMEWORK...

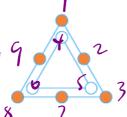


2000

- Substitute numbers for the letters to create an addition problem with a correct answer.
 - b) How many solutions are possible?



 Copy this diagram. Nace the digit through 9 in the circles so that the sum of the numbers on the outside triangle is double the sum of the numbers on the inside triangle. Explain whether more than one solution is possible.



APPLY the Math D. 28

Using deductive reasoning to generalize a conjecture EXAMPLE 2

In Lesson 1.3, page 19, Luke found more support for Steffan's conjecture from Lesson 1.1, page 9—that the difference between consecutive perfect squares is always an odd number.

4-1=3 25-16=9 100-91=19

Determine the general case to prove Steffan's conjecture.

Gord's Solution

Back to previous lesson...

The difference between consecutive perfect

squares is always an odd number.

Steffan's conjecture has worked for consecutive perfect squares with sides of 1 to 7 units.



1 unit

$$26^2 - 25^2 = 2(25) + 1$$

 $26^2 - 25^2 = 51$

Let x be any natural number. Let D be the difference between consecutive perfect squares.

$$D = (x + 1)^2 - x^2$$

$$D = x^{2} + x + x + 1 - x^{2}$$

$$D = x^{2} + 2x + 1 - x^{2}$$

$$D = 2x + 1$$

Steffan's conjecture, that the difference of consecutive perfect squares is always an odd number, has been proved for all natural numbers.

I tried a sample using even greater squares: 26² and 252.

The difference is the two sets of 25 unit tiles, plus a single unit tile.

Since the conjecture has been supported with specific examples, I decided to express the conjecture as a general statement. I chose x to be the length of the smaller square's sides. The larger square's sides would then be x + 1.

I expanded and simplified my expression. Since x represents any natural number, 2x is an even number, and 2x + 1 is an odd number.

Prove: The difference between sonsecutive perfect squares will a lways be odd Preusoning will a lways be the first #

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Algebra
$$0 \left(2x+5\right)^{2}$$

$$4x^{2}+d0x+d5$$

p. 30

EXAMPLE 5 Communicating reasoning about a divisibility rule

The following rule can be used to determine whether a number is divisible by 3:

Add the digits, and determine if the sum is divisible by 3. If the sum is divisible by 3, then the original number is divisible by 3.

Use deductive reasoning to prove that the divisibility rule for 3 is valid for two-digit numbers.

Lee's Solution

Expanded Number Forms		
	Expanded Form	Expanded Form
Number	(Words)	(Numbers)
9	9 ones	9(1)
27	2 tens and 7 ones	2(10) + 7(1)
729	7 hundreds and 2 tens and 9 ones	7(100) + 2(10) + 9(1)
ab	a tens and b ones	a(10) + b(1)

3 digit# 100a+10b+C

Let ab represent any two-digit number.

$$ab = 10a + b$$

$$ab = (9a + 1a) \pm b$$

$$ab = 9a + (a + b)$$

$$\vdots$$

The number ab is divisible by 3 only when (a + b) is divisible by 3.

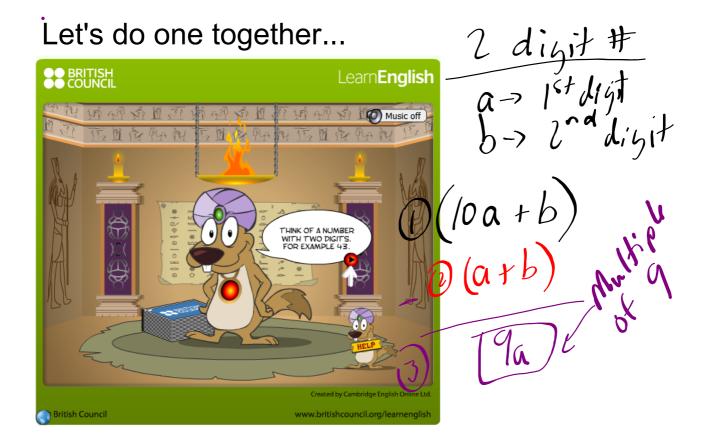
The divisibility rule has been proved for two-digit numbers.

I let ab represent any two-digit number.

Since any number can be written in expanded form, I wrote *ab* in expanded form.

I decomposed 10a into an equivalent sum. I used 9a because I knew that 9a is divisible by 3, since 3 is a factor of 9.

From this equivalent expression, I concluded that ab is divisible by 3 only when both 9a and (a + b) are divisible by 3. I knew that 9a is always divisible by 3, so I concluded that ab is divisible by 3 only when (a + b) is divisible by 3.



In Summary p. 31

Key Idea

 Deductive reasoning involves starting with general assumptions that are known to be true and, through logical reasoning, arriving at a specific conclusion.

Need to Know

- A conjecture has been proved only when it has been shown to be true for every possible case or example. This is accomplished by creating a proof that involves general cases.
- When you apply the principles of deductive reasoning correctly, you can be sure that the conclusion you draw is valid.
- The transitive property is often useful in deductive reasoning. It can be stated as follows: Things that are equal to the same thing are equal to each other. If a = b and b = c, then a = c.
- A demonstration using an example is not a proof.

HOMEWORK...

p. 31: #1, 2 #4, 5 #7, 8 #10, 11 #15, 17