

Questions...

p. 252: #1 - 3

p. 259: #1 - 4

3. Meg is building a bookshelf to display her cookbooks and novels.
- She has no more than 50 cookbooks and no more than 200 novels.
 - She wants to display at least 2 novels for every cookbook.
 - The cookbook spines are about half an inch wide, and the novel spines are about a quarter of an inch wide.
- Meg wants to know how long to make the bookshelf.

The following model represents this situation.

Let c represent the number of cookbooks.

Let n represent the number of novels.

Let W represent the width of the bookshelf.

Restrictions:

$$c \in \mathbb{W}, n \in \mathbb{W}$$

Constraints:

$$c \geq 0$$

$$n \geq 0$$

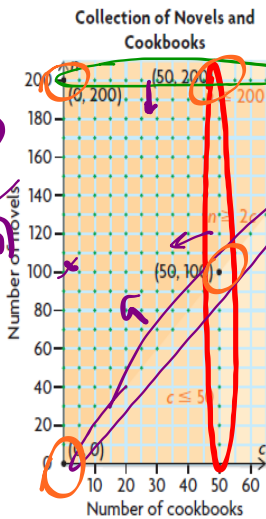
$$c \leq 50$$

$$n \leq 200$$

$$n \geq 2c$$

Objective function:

$$W = 0.5c + 0.25n$$



vertex $W = 0.5c + 0.25n$

$(0, 0)$	0
$(0, 200)$	$.5(0) + .25(200) = 50$
$(50, 100)$	$.5(50) + .25(100) = 50$
$(50, 200)$	$.5(50) + .25(200) = 75$

- Which point in the feasible region represents the greatest number of books (both cookbooks and novels) that Meg could have? Explain how you know.
- Can she display the same number of cookbooks as novels? Explain.
- What point represents the most cookbooks and the fewest novels?
- What point represents the number of cookbooks that would require the longest shelf? How long would the shelf have to be?
- What point represents the number of cookbooks that would require the shortest shelf?

$(50, 200)$ ✓
 $(50, 100)$ ✓
 No... need 2x the novels
 $(50, 200) \Rightarrow W = 75$ inches

- the other two points have a positive difference.
- $(50, 200)$; e.g., farthest point from both axes
 - No. These points are not in the feasible region.
 - $(50, 100)$
 - $(50, 200)$; 75 in.
 - $(0, 0)$ would require no shelving

2. The following model represents an optimization problem.
Determine the maximum solution.

Optimization Model

Restrictions:

$x \in \mathbb{R}$ and $y \in \mathbb{R}$

Constraints:

$x \geq 0$

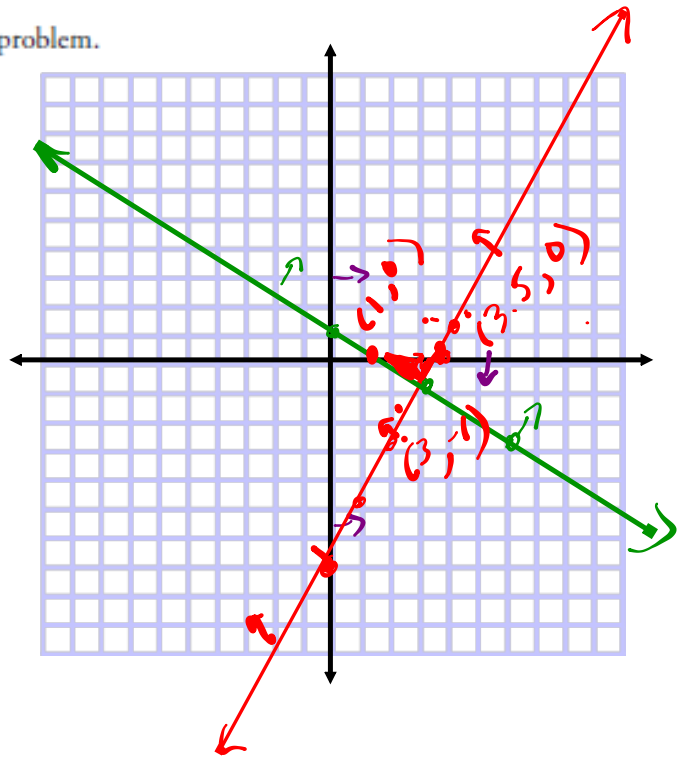
$y \leq 0$

$3y \geq -2x + 3$

$y \geq 2x - 7$

Objective function:

$D = -5x + 3y$



CS > PS

$$\begin{array}{r|l} 3(6) & -2(0) + 3 \\ 0 & 3 \\ \hline & \text{No} \end{array}$$

$$\frac{3y}{3} = \frac{-2x + 3}{3}$$

$$y = -\frac{2}{3}x + 1$$

Vertex	$D = -5x + 3y$
$(1, 0)$	$-5(1) + 3(0) = -5$
$(3.5, 0)$	$-5(3.5) + 3(0) = -17.5$
$(3, -1)$	$-5(3) + 3(-1) = -18$

MAX

ONE MORE...

Malia and Lainey are baking cupcakes and banana mini-loaves to sell at a school fundraiser...

- No more than 60 cupcakes and 35 mini-loaves can be made each day.
- Malia and Lainey can make no more than 80 baked goods in total, each day.
- It costs \$0.50 to make a cupcake and \$0.75 to make a mini-loaf.

Determine the maximum cost to produce the baked goods.

$C = 0.50x + 0.75y$

$x \rightarrow$ # of cupcakes

$x \in \mathbb{N}$

$y \rightarrow$ # of loaves

$y \in \mathbb{N}$

$x \leq 60$

$x = 60$

$y \leq 35$
 $y = 35$

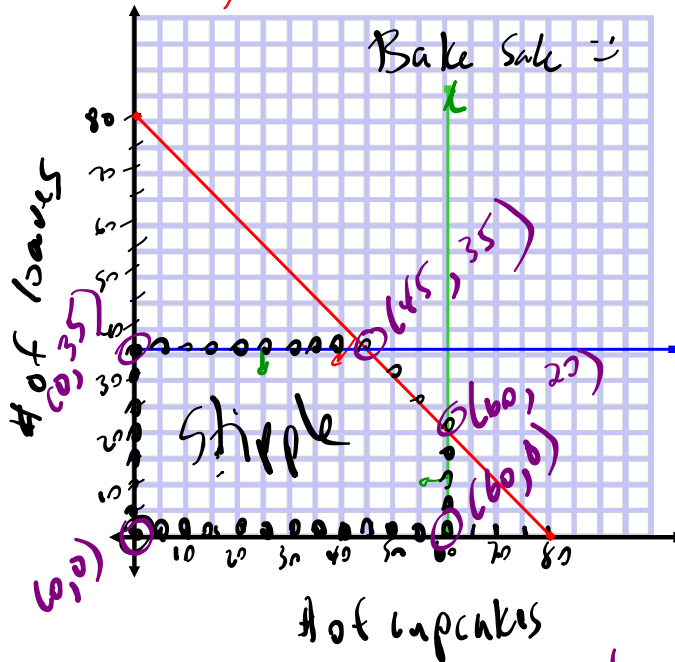
$x + y \leq 80$

Graphed

$x + y = 80$

x-int (80, 0)

y-int (0, 80)



vertex | $C = 0.5x + 0.75y$

(45, 35)

(60, 20)

$0.5(45) + .75(35)$	48.75
$.5(60) + .75(20)$	45

Max Cost

HOMEWORK: p. 259 #5, 7, 8, 11, 13

Test ⇒
THURSDAY

Multiple Choice ⇒ 10-15

Open Response ⇒ 25-40

→ #1 → 2 inequalities - graph
→ #2 → Word problem

→ #3 → Optimization
(constraints given)
→ #4 → Word problem