

Composite Objects Assignment

- ① Find surface area of all objects
- ② Locate and Calculate Overlap
- ③ Determine Total Surface Area

1. Small rectangular prism

Front/Back $A = L \times w$ $= 8 \times 10$ $= 80$ <hr/> $160$	Side/Side $A = L \times w$ $= 5 \times 8$ $= 40$ <hr/> $80$	Top/Bottom $A = L \times w$ $= 5 \times 10$ $= 50$ <hr/> $100$	$SA = 160 + 80 + 100$ $= 340 \text{ cm}^2$
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Large rectangular Prism

Front/Back $A = L \times w$ $= 20 \times 15$ $= 300$ <hr/> $600$	Side/Side $A = L \times w$ $= 12 \times 15$ $= 180$ <hr/> $360$	Top/Bottom $A = L \times w$ $= 20 \times 12$ $= 240$ <hr/> $480$	$SA = 600 + 360 + 480$ $= 1440 \text{ cm}^2$
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Overlap

$$A = L \times w$$

$$= 10 \times 5$$

$$= 50$$


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$$100$$

Total Surface Area

$$= \text{Small} + \text{Large} - \text{overlap}$$

$$340 + 1440 - 100$$


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$$1680 \text{ cm}^2$$

2. Cylinder

$$SA = 2\pi r^2 + 2\pi r h$$

$$= 2(3.14)(6)^2 + 2(3.14)(6)(10)$$

$$= 2(3.14)(36) + 376.8$$

$$= 226.08 + 376.8$$

$$= 602.88 \text{ mi}^2$$

Rectangular Prism

Front/Back $A = L \times w$ $= 15 \times 4$ $= 60$ <hr/> $120$	Side/Side $A = L \times w$ $= 12 \times 4$ $= 48$ <hr/> $96$	Top/Bottom $A = L \times w$ $= 15 \times 12$ $= 180$ <hr/> $360$	$SA = 120$ $96$ $+ 360$ <hr/> $576 \text{ mi}^2$
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Overlap

$$A = \pi r^2$$

$$= (3.14)(6)^2$$

$$= (3.14)(36)$$

$$= 113.04$$


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$$226.08 \text{ mi}^2$$

Total Surface Area = Cylinder + Rectangular Prism - Overlap

$$= 602.88 + 576 - 226.08$$

$$= 952.8 \text{ mi}^2$$

3. Small Cylinder

$$\begin{aligned}
 SA &= 2\pi r^2 + 2\pi r h \\
 &= 2(3.14)(3)^2 + 2(3.14)(3)(8) \\
 &= 2(3.14)(9) + 150.72 \\
 &= 56.52 + 150.72 \\
 &= 207.24 \text{ Km}^2
 \end{aligned}$$

Large Cylinder

$$\begin{aligned}
 SA &= 2\pi r^2 + 2\pi r h \\
 &= 2(3.14)(11)^2 + 2(3.14)(11)(6) \\
 &= 2(3.14)(121) + 414.48 \\
 &= 759.88 + 414.48 \\
 &= 1174.36 \text{ Km}^2
 \end{aligned}$$

Overlap

$$\begin{aligned}
 A &= \pi r^2 \\
 &= (3.14)(3)^2 \\
 &= (3.14)(9) \\
 &= 28.26 \\
 &\quad \times 2 \\
 &= 56.52 \text{ Km}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Total Surface Area} &= \text{Small Cylinder} + \text{Large} - \text{Overlap} \\
 &= 207.24 + 1174.36 - 56.52 \\
 &= 1325.08 \text{ Km}^2
 \end{aligned}$$

4. Top Rec. Prism

Front/Back	Side/Side	Top/Bottom	
$A = L \times w$	$A = L \times w$	$A = L \times w$	$SA = 400 + 100 + 32$ $= 532 \text{ Km}^2$
$= 8 \times 25$	$= 2 \times 25$	$= 8 \times 2$	
$= 200$	$= 50$	$= 16$	
$\quad \times 2$	$\quad \times 2$	$\quad \times 2$	
$400$	$100$	$32$	

Middle Rec. Prism

Front/Back	Side/Side	Top/Bottom	
$A = L \times w$	$A = L \times w$	$A = L \times w$	$SA = 440 + 220 + 400$ $= 1060 \text{ Km}^2$
$= 20 \times 11$	$= 10 \times 11$	$= 20 \times 10$	
$= 220$	$= 110$	$= 200$	
$\quad \times 2$	$\quad \times 2$	$\quad \times 2$	
$440$	$220$	$400$	

Bottom Rec. Prism

Front/Back	Side/Side	Top/Bottom	
$A = L \times w$	$A = L \times w$	$A = L \times w$	$SA = 140 + 60 + 42$ $= 242 \text{ Km}^2$
$= 10 \times 7$	$= 10 \times 3$	$= 7 \times 3$	
$= 70$	$= 30$	$= 21$	
$\quad \times 2$	$\quad \times 2$	$\quad \times 2$	
$140$	$60$	$42$	

Overlap  $(32 + 42 = 74)$  } Total Surface Area

$A = L \times w$ $= 8 \times 2$ $= 16$ $\quad \times 2$ $32 \text{ Km}^2$	$A = L \times w$ $= 7 \times 3$ $= 21$ $\quad \times 2$ $42 \text{ Km}^2$	$\text{Top} + \text{Middle} + \text{Bottom} - \text{Overlap}$ $532 + 1060 + 242 - 74$ $1760 \text{ Km}^2$
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5. Top Rec. Prism

Front/Back $A = L \times w$ $= 6 \times 2$ $= 12$ $\frac{\times 2}{32}$	Side/Side $A = L \times w$ $= 2 \times 3$ $= 6$ $\frac{\times 2}{12}$	Top/Bottom $A = L \times w$ $= 3 \times 8$ $= 24$ $\frac{\times 2}{48}$	$SA = 32 + 12 + 48$ $= 92 \text{ cm}^2$
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Middle Cylinder

$$SA = 2\pi r^2 + 2\pi r h$$

$$= 2(3.14)(12)^2 + 2(3.14)(12)(5)$$

$$= 2(3.14)(144) + 376.8$$

$$= 904.32 + 376.8$$

$$= 1281.12 \text{ cm}^2$$

Bottom Cylinder

$$SA = 2\pi r^2 + 2\pi r h$$

$$= 2(3.14)(6)^2 + 2(3.14)(6)(20)$$

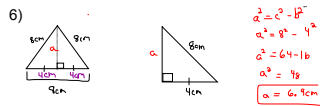
$$= 2(3.14)(36) + 753.6$$

$$= 226.08 + 753.6$$

$$= 979.68 \text{ cm}^2$$

Overlap ( $48 + 226.08 = 274.08$ )

$A = L \times w$ $= 6 \times 3$ $= 24$ $\frac{\times 2}{48 \text{ cm}^2}$	$A = \pi r^2$ $= (3.14)(6)^2$ $= (3.14)(36)$ $= 113.04$ $\frac{\times 2}{226.08 \text{ cm}^2}$	Total Surface Area Top Rec. Prism + Middle Cylinder + Bottom - Overlap $92 + 1281.12 + 979.68 - 274.08$ $= 2078.72 \text{ cm}^2$
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Prisms:

$A = \frac{b \times h}{2}$ $A = \frac{3 \times 4}{2}$ $A = \frac{12}{2}$ $A = 6 \text{ cm}^2$ $2A = 12 \text{ cm}^2$	$A = bh$ $A = 5 \times 3$ $A = 15 \text{ cm}^2$ $3A = 45 \text{ cm}^2$	$SA = 2A + 3A$ $= 12 + 45$ $= 57 \text{ cm}^2$
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There are 2 triangle prism so  
 $2SA = 114 \text{ cm}^2$

Cylinder:

$$SA = 2\pi r^2 + 2\pi r h$$

$$= 2(3.14)(3)^2 + 2(3.14)(3)(12)$$

$$= 2(3.14)(9) + 2(3.14)(36)$$

$$= 56.52 + 226.08$$

$$= 282.6 \text{ cm}^2$$

Overlap (circles)

$$A_c = \pi r^2$$

$$A_c = (3.14)(3^2)$$

$$A_c = 3.14(9)$$

$$A_c = 28.26 \text{ cm}^2$$

$$4A_c = 113.04 \text{ cm}^2$$

$$TSA = 2 \text{ Triangle prisms} + \text{Cylinder} - \text{overlap}$$

$$= 114 \text{ cm}^2 + 282.6 \text{ cm}^2 - 113.04 \text{ cm}^2$$

$$= 283.56 \text{ cm}^2$$