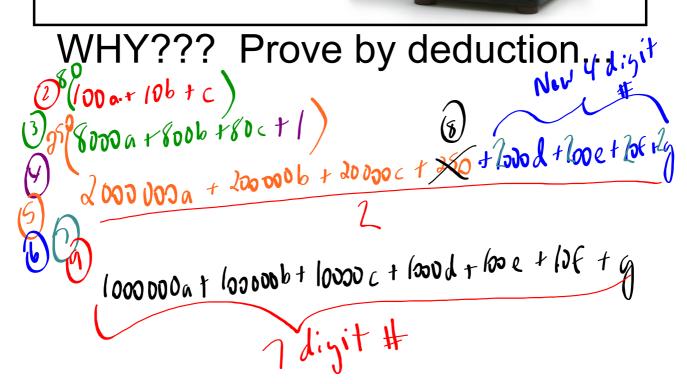
WARM-UP...

- 1. Grab a calculator. (you won't be able to do this one in your head)
- 2. Key in the first three digits of your phone number (NOT the area code)
- 3. Multiply by 80
- 4. Add 1
- 5. Multiply by 250
- 6. Add the last 4 digits of your phone number
- 7. Add the last 4 digits of your phone number again.
- 8. Subtract 250
- 9. Divide number by 2

Do you recognize the answer?





In Summary p. 31

Key Idea

 Deductive reasoning involves starting with general assumptions that are known to be true and, through logical reasoning, arriving at a specific conclusion.

Need to Know

- A conjecture has been proved only when it has been shown to be true for every possible case or example. This is accomplished by creating a proof that involves general cases.
- When you apply the principles of deductive reasoning correctly, you can be sure that the conclusion you draw is valid.
- The transitive property is often useful in deductive reasoning. It can be stated as follows: Things that are equal to the same thing are equal to each other. If a = b and b = c, then a = c.
- · A demonstration using an example is not a proof.

Questions?

HOMEWORK...

p. 31: #1, 2 #4,5 #7, 8 #10, 11 #15, 17

5. Prove that the product of an even integer and an odd integer is always even.

$$12 \times 15 = 180$$

inductively

Peductively

Even # > 2xOld # > 2x + /x 2x(2x+1) $4x^2 + 2x \Rightarrow 2(2x+x)$ even + even \Rightarrow even

7. Drew creates this step-by tep number trick:

• Choose any number.

• Multiply by 4.

• Add 10.

• Divide by 2.

• Subtract 5.

- Subtract 5.
 Divide by 2.
 Add 3.
 a) Show inductively, using three examples, that the result is always 3 more than the chosen number.
- **b)** Prove deductively that the result is always 3 more than the chosen number.

b)
$$x = 0$$
 | 8 2
 $\frac{4x}{4x+10}$ | $\frac{54}{27}$ | $\frac{2}{27}$ | $\frac{2}$

10. Prove that whenever you square an <u>odd integer</u>, the result is odd.

17. Simon made the following conjecture: When you add three consecutive numbers, your answer is always a multiple of 3. Joan, Garnet, and Jamie took turns presenting their work to prove Simon's conjecture. Which student had the strongest proof? Explain.

| Joan's Work | | Garnet's Work | Jamie's Work | |
|------------------------------|------------------|--|---|-------|
| 1 + 2 + 3 = 6 | $3 \cdot 2 = 6$ | 3 + 4 + 5 | Let the numbers be $n, n + 1$, | |
| 2 + 3 + 4 = 9 | $3 \cdot 3 = 9$ | = " | and <i>n</i> + 2. | |
| 3 + 4 + 5 = 12 | $3 \cdot 4 = 12$ | The two outside numbers | n + n + 1 + n + 2 = 3n + 3 | |
| 4 + 5 + 6 = 15 | $3 \cdot 5 = 15$ | (3 and 5) add to give twice the middle number (4). All three | n + n + 1 + n + 2 = 3(n + 1) | 11:04 |
| 5 + 6 + 7 = 18 | $3 \cdot 6 = 18$ | numbers add to give 3 times the middle number. | M. 1 | Mr. 3 |
| and so on | | | , , , , , , , , , , , , , , , , , , , | 9% |
| Simon's conjecture is valid. | | Simon's conjecture is valid. | Simon's conjecture is valid. | |
| Inductive | | | deductive | |

Squaring A Binomial

Distribute 2x+1/2 3 Step (1st)² $3(2^{nd})^{2}$ (2x+1)(2x+1) $4x^{2}+3x+2x+1$ $4x^{2}+4x+1$ $4x^{2}+4x+1$ $4x^{2}+4x+1$ $4x^{2}-30x+25$

APPLY the Math p. 28

EXAMPLE 2 Using deductive reasoning to generalize a conjecture

In Lesson 1.3, page 19, Luke found more support for Steffan's conjecture from Lesson 1.1, page 9—that the difference between consecutive perfect squares is always an odd number.

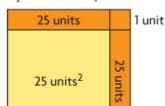
Determine the general case to prove Steffan's conjecture.

Gord's Solution

Back to previous lesson...

The difference between consecutive perfect squares is always an odd number.

Steffan's conjecture has worked for consecutive perfect squares with sides of 1 to 7 units.



$$26^2 - 25^2 = 2(25) + 1$$

 $26^2 - 25^2 = 51$

I tried a sample using even greater squares: 26^2 and 25^2 .

The difference is the two sets of 25 unit tiles, plus a single unit tile.

Let *x* be any natural number. Let *D* be the difference between consecutive perfect squares.

$$D = (x + 1)^2 - x^2$$

$$D = x^{2} + x + x + 1 - x^{2}$$

$$D = x^{2} + 2x + 1 - x^{2}$$

$$D = 2x + 1$$

Steffan's conjecture, that the difference of consecutive perfect squares is always an odd number, has been proved for all natural numbers. Since the conjecture has been supported with specific examples, I decided to express the conjecture as a general statement. I chose x to be the length of the smaller square's sides. The larger square's sides would then be x+1.

I expanded and simplified my expression. Since x represents any natural number, 2x is an even number, and 2x + 1 is an odd number.

In Lesson 1.3, page 19, Luke found more support for Steffan's conjecture from Lesson 1.1, page 9—that the difference between consecutive perfect squares is always an odd number.

Inductive

| 52-42 | 9 |
|--------------|-----|
| 112-102 | 21 |
| 812-8ø2 ■ | 161 |

HOMEWORK