

Perfect Square Trinomials *

- three terms: the first and last are perfect squares.
- factors like this...

$$a^2 + 2ab + b^2 = (a + b)^2$$

OR

$$a^2 - 2ab + b^2 = (a - b)^2$$

- recognize them and you save yourself the decomposition steps!!!

EXAMPLES...

$$1) 25x^2 - 10x + 1$$
$$(5x - 1)^2$$

$$2) 9x^2 + 24x + 16$$
$$(3x + 4)^2$$

$$(5x-1)^2 \quad (2x+3)^2$$

$$(5x-1)(5x-1)$$

$$4x^2 + 12x + 9$$

$$25x^2 - 5x - 5x + 1$$

$$25x^2 - 10x + 1$$

$$\cancel{9x^2 - 24x + 16}$$

$$\begin{aligned} & \checkmark \\ & x^2 - 12x + \cancel{36} \\ & (x - 6)^2 \end{aligned}$$

$$\begin{aligned} & \checkmark \\ & x^2 + 8x + \cancel{16} \\ & (x + 4)^2 \end{aligned}$$

$$\begin{aligned} & \cancel{2x^2 + 12x + 18} \quad \begin{array}{l} x = 9 \\ - + = 6 \end{array} \\ & 2(x^2 + 6x + 9) \\ & 2(x+3)^2 \\ & 2(x+3)(x+3) \\ & 2(x+3) \end{aligned}$$

Factor using Perfect Squares Method

$$25x^2 - 120x + 144$$



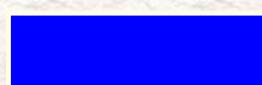
$$81x^2 - 180x + 100$$



$$49x^2 + 80x + 36$$



$$36x^2 + 132x + 121$$



Difference of Squares

1. GCF
(all)

- two terms that are perfect squares.
- must be a difference
- factor like this...

$$a^2 - b^2 = (a + b)(a - b)$$

- ximondy
- | |
|-----------------|
| 2. Simp Tri |
| 3. Hard Tri |
| 4. Perf sq. Tri |
| 5. DOS |

EXAMPLES...

1) $4x^2 - 49$ $\checkmark \checkmark \checkmark (2x+7)(2x-7)$

3) $81z^4 - 625$ $\underbrace{(9z^2+25)}_{(9z^2+25)} \underbrace{(9z^2-25)}_{(9z^2+25)} 49w^2 - 4s^2$

5) $32x^4 - 2$

$$2(16x^4 - 1)$$

$$2(4x^2 + 1)(4x^2 - 1)$$

$$2(4x^2 + 1) \boxed{(2x+1)(2x-1)}$$

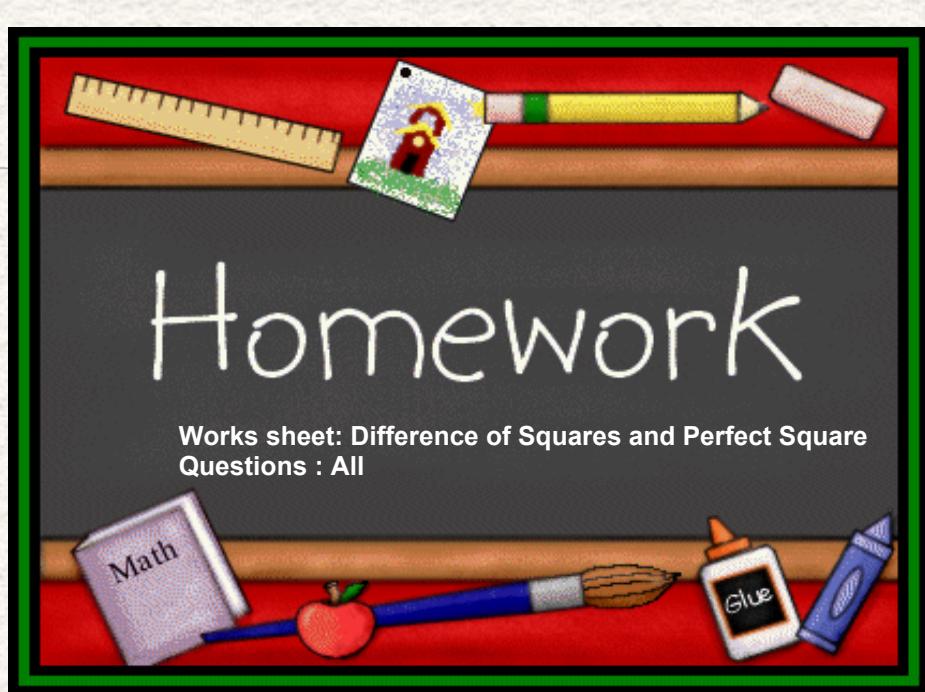
$$(2x+7)(2x-7)$$
$$4x^2 - \boxed{-14x + 14x} - 49$$
$$4x^2 - 49$$

Recognize binomial

Check for difference of squares

Double check!!

$$81z^4 - 625$$



Math 10

Name_____

Factoring: Difference of Squares and Perfect Squares

Date_____

Factor each completely.

1) $n^2 - 9$

2) $25a^2 - 9$

3) $k^2 - 4$

4) $16x^2 - 9$

5) $x^2 - 25$

6) $25x^2 - 16y^2$

7) $u^2 - 16v^2$

8) $u^2 - 9v^2$

9) $4x^2 - y^2$

10) $a^2 - 25b^2$

11) $9m^2 + 12m + 4$

12) $16r^2 + 8r + 1$

13) $25x^2 - 20x + 4$

14) $16n^2 + 40n + 25$

15) $9b^2 - 24b + 16$

16) $16m^2 - 24mn + 9n^2$

17) $9x^2 - 6xy + y^2$

18) $25x^2 + 10xy + y^2$

19) $x^2 - 8xy + 16y^2$

20) $9x^2 + 24xy + 16y^2$

Answers to Factoring: Difference of Squares and Perfect Squares (ID: 1)

- | | | | |
|-------------------|---------------------|-------------------|-------------------|
| 1) $(n+3)(n-3)$ | 2) $(5a+3)(5a-3)$ | 3) $(k+2)(k-2)$ | 4) $(4x+3)(4x-3)$ |
| 5) $(x+5)(x-5)$ | 6) $(5x+4y)(5x-4y)$ | 7) $(u+4v)(u-4v)$ | 8) $(u+3v)(u-3v)$ |
| 9) $(2x+y)(2x-y)$ | 10) $(a+5b)(a-5b)$ | 11) $(3m+2)^2$ | 12) $(4r+1)^2$ |
| 13) $(5x-2)^2$ | 14) $(4n+5)^2$ | 15) $(3b-4)^2$ | 16) $(4m-3n)^2$ |
| 17) $(3x-y)^2$ | 18) $(5x+y)^2$ | 19) $(x-4y)^2$ | 20) $(3x+4y)^2$ |

$$1) n^2 - 9$$
$$(n + 3)(n - 3)$$

$$2) 25a^2 - 9$$
$$(5a + 3)(5a - 3)$$

$$3) k^2 - 4$$
$$(k + 2)(k - 2)$$

$$4) 16x^2 - 9$$
$$(4x + 3)(4x - 3)$$

$$5) \ x^2 - 25$$

$$(x + 5)(x - 5)$$

$$6) \ 25x^2 - 16y^2$$

$$(5x + 4y)(5x - 4y)$$

$$7) \ u^2 - 16v^2$$

$$(u + 4v)(u - 4v)$$

$$8) \ u^2 - 9v^2$$

$$(u + 3v)(u - 3v)$$

$$9) \quad 4x^2 - y^2$$
$$(2x + y)(2x - y)$$

$$10) \quad a^2 - 25b^2$$
$$(a + 5b)(a - 5b)$$

$$11) \quad 9m^2 + 12m + 4$$
$$(3m + 2)^2$$

$$12) \quad 16r^2 + 8r + 1$$
$$(4r + 1)^2$$

$$13) \ 25x^2 - 20x + 4$$
$$(5x - 2)^2$$

$$14) \ 16n^2 + 40n + 25$$
$$(4n + 5)^2$$

$$15) \ 9b^2 - 24b + 16$$
$$(3b - 4)^2$$

$$16) \ 16m^2 - 24mn + 9n^2$$
$$(4m - 3n)^2$$

$$17) \quad 9x^2 - 6xy + y^2$$
$$(3x - y)^2$$

$$18) \quad 25x^2 + 10xy + y^2$$
$$(5x + y)^2$$

$$19) \quad x^2 - 8xy + 16y^2$$
$$(x - 4y)^2$$

$$20) \quad 9x^2 + 24xy + 16y^2$$
$$(3x + 4y)^2$$

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