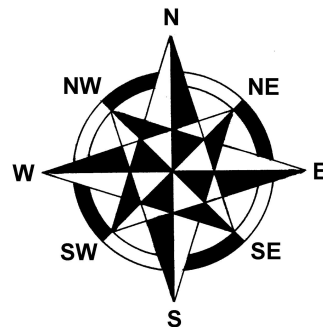
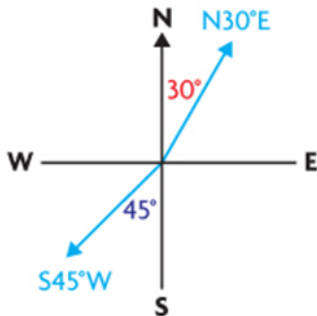


MORE APPLICATIONS... Bearings

NOTE:

Communication | Tip

Directions are often stated in terms of north and south on a compass. For example, $N30^\circ E$ means travelling in a direction 30° east of north. $S45^\circ W$ means travelling in a direction 45° west of south.

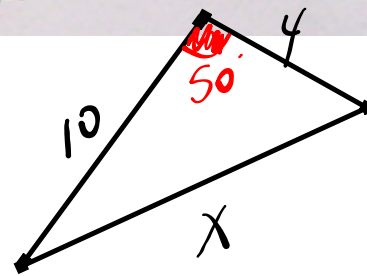
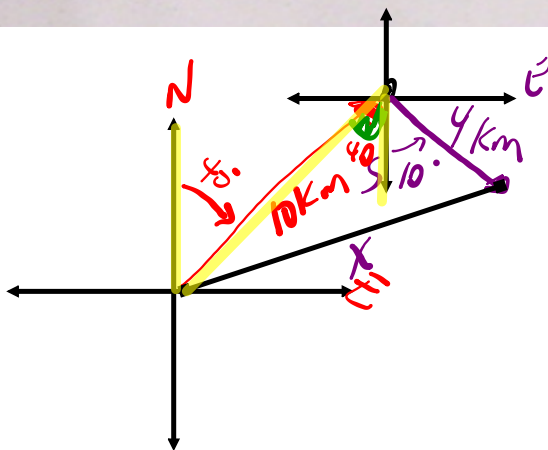


Booklet Questions... 10.12: #11, 12

QUESTIONS???

"40° East of North"

11 Jean is a cross-country skier and skis 10 km in a direction $N40^\circ E$ of the ski lodge. At this point she turns and skis $S10^\circ E$ for 4 km and arrives at a chalet. How far is Jean from the lodge?

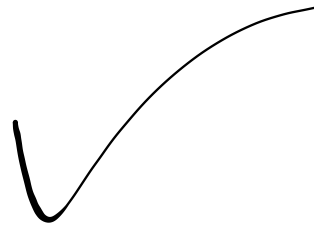


$$x^2 = 10^2 + 4^2 - 2(10)(4)\cos 50^\circ$$

$$x^2 = \begin{matrix} 10^2 + 4^2 - 2 * 10 * 4 * \cos(50) \\ 64.57699123 \\ \sqrt{\text{Ans}} \\ 8.035981037 \end{matrix}$$

$$x = \boxed{X = 8.0 \text{ km}}$$

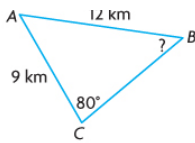
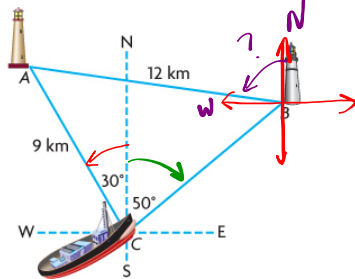
Practice & Problems #7-9



Applications: Bearings

Ex #1:(p. 122) Using reasoning to determine the measure of an angle

The captain of a small boat is delivering supplies to two lighthouses, as shown. His compass indicates that the lighthouse to his left is located at $N30^\circ W$ and the lighthouse to his right is located at $N50^\circ E$. Determine the compass direction he must follow when he leaves lighthouse B for lighthouse A .



$$\frac{\sin B}{AC} = \frac{\sin C}{AB}$$

I drew a diagram. I labelled the sides of the triangle I knew and the angle I wanted to determine.

I knew AC , AB , and $\angle C$, and I wanted to determine $\angle B$. So I used the sine law that includes these four quantities.

I used the proportion with $\sin B$ and $\sin C$ in the numerators so the unknown would be in the numerator.

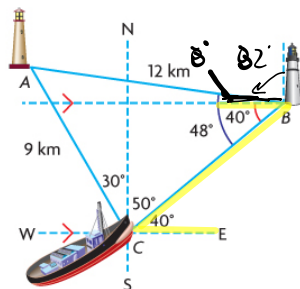
$$\begin{aligned} \frac{\sin B}{9} &= \frac{\sin 80^\circ}{12} \\ 9\left(\frac{\sin B}{9}\right) &= 9\left(\frac{\sin 80^\circ}{12}\right) \\ \sin B &= 9\left(\frac{\sin 80^\circ}{12}\right) \\ \sin B &= 0.7386... \end{aligned}$$

$$\begin{aligned} \angle B &= \sin^{-1}(0.7386...) \\ \angle B &= 47.612...^\circ \end{aligned}$$

I substituted the given information and then solved for $\sin B$.

The measure of $\angle B$ is 48° .

The answer seems reasonable. $\angle B$ must be less than 80° , because 9 km is less than 12 km.



I drew a diagram and marked the angles I knew. I knew east-west lines are all parallel, so the alternate interior angle at B must be 40° .

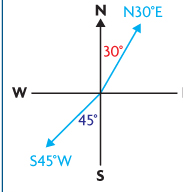
The captain must head $N82^\circ W$ from lighthouse B .

The line segment from lighthouse B to lighthouse A makes an 8° angle with west-east. I subtracted this from 90° to determine the direction west of north.

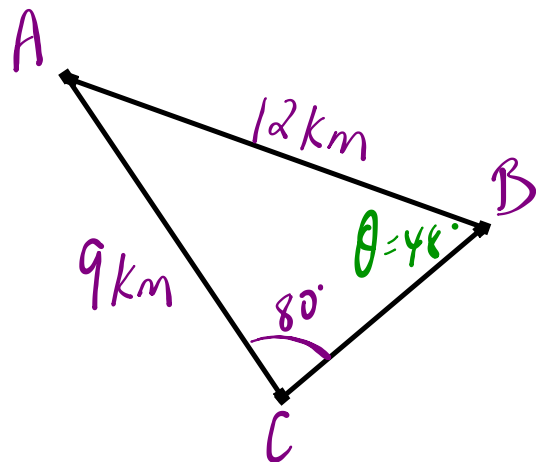
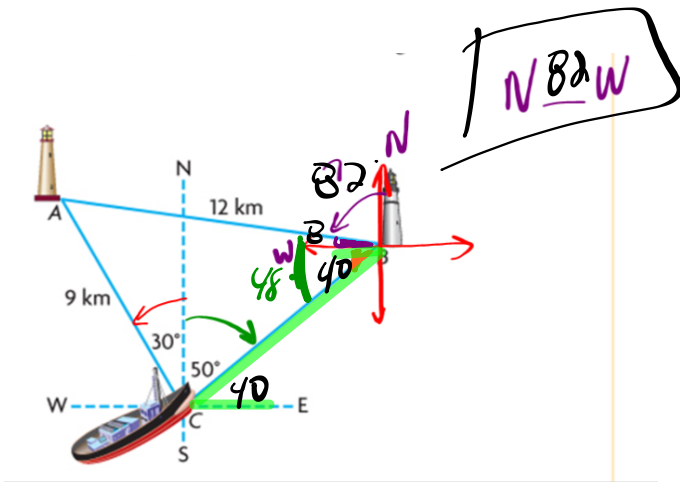
NOTE:

Communication **Tip**

Directions are often stated in terms of north and south on a compass. For example, $N30^\circ E$ means travelling in a direction 30° east of north. $S45^\circ W$ means travelling in a direction 45° west of south.



Compass Rose Animation



$$9 \frac{\sin \theta}{9} = \frac{9 \sin 80^\circ}{12}$$

$$\sin^{-1} \sin \theta = (0.7386)$$

$$\theta = 48^\circ$$

EX #2: Solving an application question...

(p. 166)

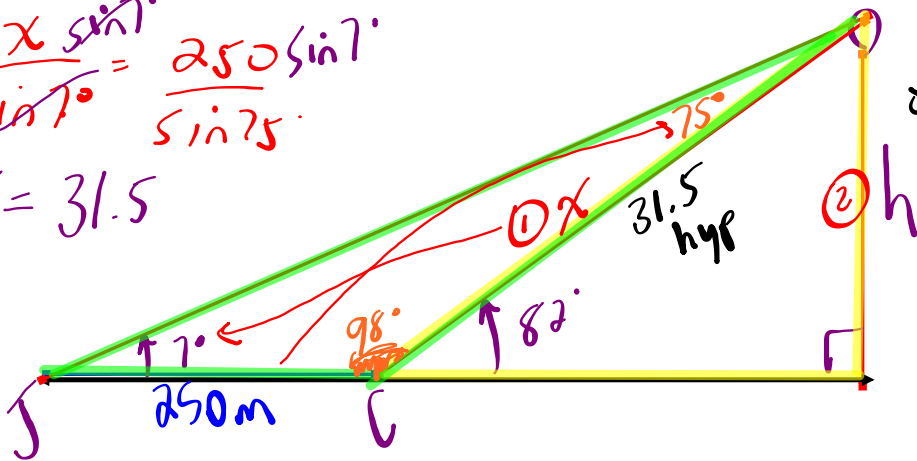
Colleen and Juan observed a tethered balloon advertising the opening of a new fitness centre. They were 250 m apart, joined by a line that passed directly below the balloon, and were on the same side of the balloon. Juan observed the balloon at an angle of elevation of 7° while Colleen observed the balloon at an angle of elevation of 82° . Determine the height of the balloon to the nearest metre.

$$\textcircled{1} \frac{x \sin 7^\circ}{\sin 7^\circ} = \frac{250 \sin 7^\circ}{\sin 75^\circ}$$

$$x = 31.5$$

$$\textcircled{2} \frac{31.5 \sin 82^\circ}{\sin 82^\circ} = \frac{h}{31.5}$$

$$31.2 \text{ m} = h$$



...

HOMEWORK: More Applications/Word Problems

Page 154 #5, 6, 9, 10, 11 (bearings - see example from Friday)

Page 172 #9, 10, 12, 13, 14

