

# QUESTIONS???

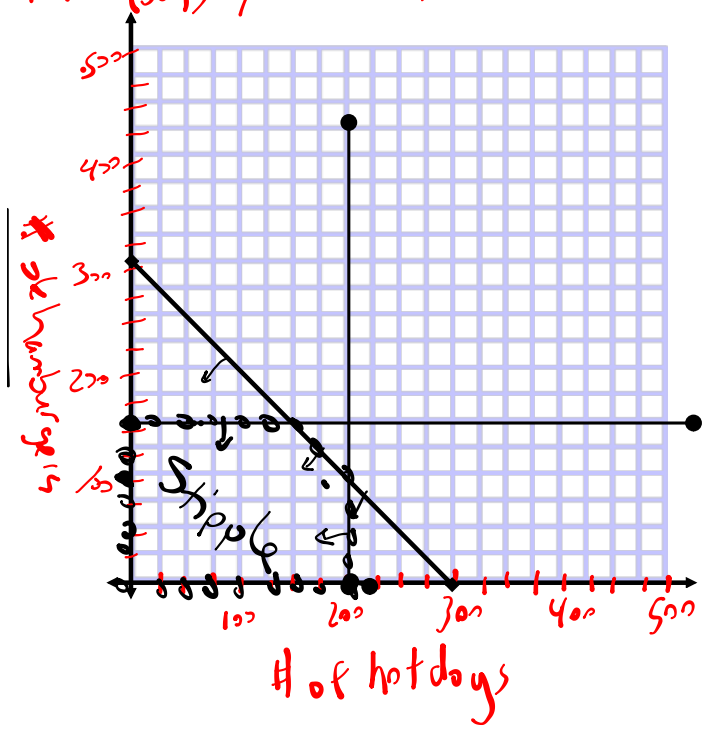
## HOMEWORK...

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**NOTE:**  
Create a model means graph the solution region

2. A fast-food concession stand sells hotdogs and hamburgers.
- Daily sales can be as high as 300 hamburgers and hot dogs combined.
  - The stand has room to stock no more than 200 hot dogs and no more than 150 hamburgers.
  - Hot dogs are sold for \$3.25, and hamburgers are sold for \$4.75.
- Create a model that could be used to determine the combination of hamburgers and hot dogs that will result in maximum sales.

$x \rightarrow$  # of hotdogs  $x \in W$   
 $y \rightarrow$  # of hamburgers  $y \in W$   
 $x + y \leq 300$   $x \leq 200$   $y \leq 150$   
 $x = 200$   $y = 150$   
vertical horizontal  
 $x \text{ int } (300, 0)$   $y \text{ int } (0, 300)$



5. A football stadium has 50 000 seats.
- Two-fifths of the seats are in the lower deck.
  - Three-fifths of the seats are in the upper deck.
  - At least 30 000 tickets are sold per game.
  - A lower deck ticket costs \$120, and an upper deck ticket costs \$80.

$x \rightarrow$  # of lower deck  
 $y \rightarrow$  # of upper deck  
 $x \leq W$      $y \leq W$

Create a model that could be used to determine a combination of tickets for lower-deck and upper-deck seats that should be sold to maximize revenue.

$$x + y \geq 30000$$

$$x \leq 20000$$

$$y \leq 30000$$

$$\frac{2}{5}(50000) = 20000$$

$$\frac{3}{5}(50000) = 30000$$

**GOAL**

Solve optimization problems.

**EXPLORE...**

The following system of linear inequalities has been graphed below:

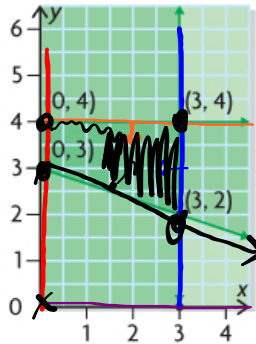
System of linear inequalities:

- $y \geq 0$
- $x \geq 0$
- $y \leq 4$
- $x \leq 3$
- $3y \geq -x + 9$

Quad 1

$$3y = -x + 9$$

$$y = -\frac{1}{3}x + 3$$



Test (0,0)

$$3y \geq -x + 9$$

$$0 \geq -0 + 9$$

$$0 \geq 9$$

No

- a) For each objective function, what points in the feasible region represent the minimum and maximum values?
- i)  $T = 5x + y$
  - ii)  $T = x + 5y$
- b) What do you notice about the optimal points for the two objective functions? Why do you think this happened?

**SAMPLE ANSWER**

a) i) For  $T = 5x + y$ ,

If (x, y) is...	Then...	
(3, 2)	$T = 5(3) + 2$ $T = 17$	
(3, 4)	$T = 5(3) + 4$ $T = 19$	maximum
(0, 3)	$T = 5(0) + 3$ $T = 3$	minimum
(0, 4)	$T = 5(0) + 4$ $T = 4$	

ii) For  $T = x + 5y$ ,

If (x, y) is...	Then...	
(3, 2)	$T = 3 + 5(2)$ $T = 13$	minimum
(3, 4)	$T = 3 + 5(4)$ $T = 23$	maximum
(0, 3)	$T = 0 + 5(3)$ $T = 15$	
(0, 4)	$T = 0 + 5(4)$ $T = 20$	

- b) I noticed that the values of the coefficients of the variables and the values of the variables themselves all contribute to the value of the objective function. For  $T = 5x + y$ , the x-value is multiplied by 5 and the y-value is multiplied by 1. For  $T = x + 5y$ , the x-value is multiplied by 1 and the y-value is multiplied by 5. In each case, the greater the coordinate that is multiplied by 5, the greater the value of the objective function is. The converse is true for the least values.

**EXAMPLE #1...**

The following model represents an optimization problem. Determine the maximum solution.

Restrictions:  $x \in \mathbb{R}$  and  $y \in \mathbb{R}$

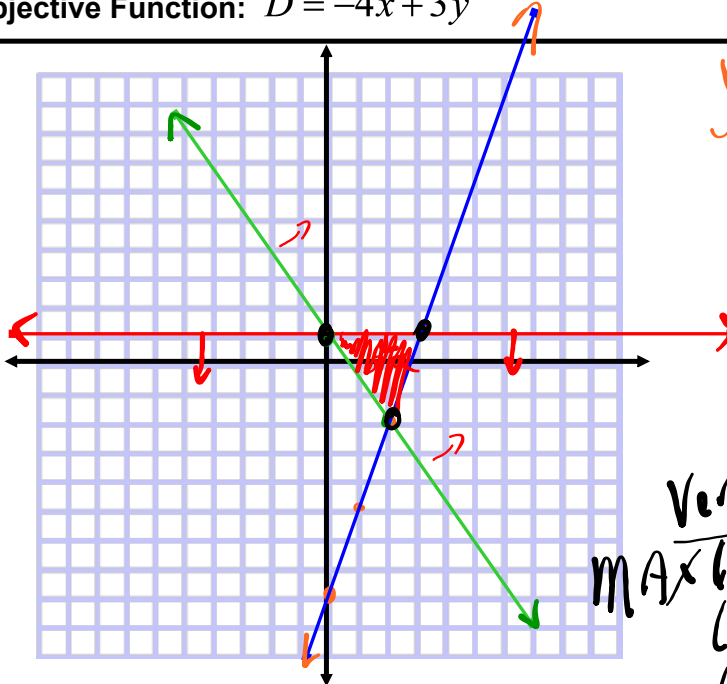
Constraints:  $y \leq 1$ ;  $2y \geq -3x + 2$ ;  $y \geq 3x - 8$

Objective Function:  $D = -4x + 3y$

$y = 1$   
horizontal

$$\frac{2y}{2} = \frac{-3x + 2}{2}$$

$$y = -\frac{3}{2}x + 1$$



$y = 3x - 8$   
 $LS \geq RS$

$$\frac{0}{1} \geq \frac{3(0) - 8}{1}$$

$$0 \geq -8$$

yes

$LS \geq RS$

$$\frac{2(0)}{2} \geq \frac{-3(0) + 2}{2}$$

$$0 \geq 1$$

NO

Vertices

	$D = -4x + 3y$
$(0, 1)$	$-4(0) + 3(1) = 3$
$(3, 1)$	$-4(3) + 3(1) = -9$
$(2, -2)$	$-4(2) + 3(-2) = -14$

Sub

### EXAMPLE of an OPTIMIZATION Problem...



Mick and Keith make MP3 covers to sell, using beads and stickers.

- At most, 45 covers with stickers and 55 bead covers can be made per day.
- Mick and Keith can make 45 or more covers, in total, each day.
- It costs \$0.75 to make a cover with stickers, \$1.00 to make one with beads.

Let  $x$  represent the number of covers with stickers and let  $y$  represent the number of bead covers.

Let  $C$  represent the cost of making the covers.

RESTRICTIONS:  $x \in \mathbb{W}$   $y \in \mathbb{W}$

CONSTRAINTS:  $x \leq 45$   $y \leq 55$   $x + y \geq 45$

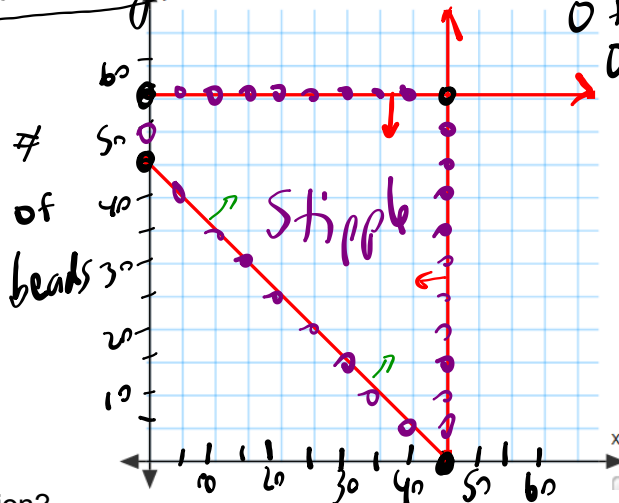
OBJECTIVE FUNCTION:  $C = 0.75x + 1.00y$

GRAPH Test  $(0,0)$   
 $45 \geq 45$   
 $0 + 0 \geq 45$   
 $0 \geq 45$   
 No

a) Graph the solution set.

$x + y = 45$   
 $x$ -int  $(45, 0)$   
 $y$ -int  $(0, 45)$

$y = 55$   
 $x = 45$



b) What are the vertices of the feasible region?

$(0, 45)$   $(0, 55)$   $(45, 0)$   $(45, 55)$  # of stickers

c) Which point would result in the maximum value of the objective function?

$(45, 55)$

d) Which point would result in the minimum value of the objective function?

$(45, 0)$

	45
$0.75 \cdot 0 + 1 \cdot 55$	55
$0.75 \cdot 45 + 1 \cdot 0$	33.75
$0.75 \cdot 45 + 1 \cdot 55$	88.75

## HOMEWORK...

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