

## HOMEWORK???

p. 252: #1 - (3)

p. 248: #4, 6

3. Meg is building a bookshelf to display her cookbooks and novels.
- She has no more than 50 cookbooks and no more than 200 novels.
  - She wants to display at least 2 novels for every cookbook.
  - The cookbook spines are about half an inch wide, and the novel spines are about a quarter of an inch wide.
- Meg wants to know how long to make the bookshelf.

The following model represents this situation.

Let  $c$  represent the number of cookbooks.

Let  $n$  represent the number of novels.

Let  $W$  represent the width of the bookshelf.

Restrictions:

$c \in \mathbb{W}, n \in \mathbb{W}$

Constraints:

$c \geq 0$

$n \geq 0$

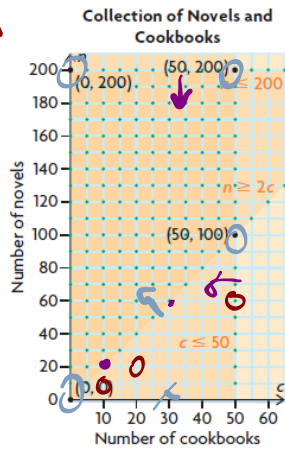
$c \leq 50$

$n \leq 200$

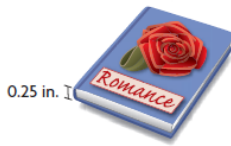
$n \geq 2c$

Objective function:

$W = 0.5c + 0.25n$



- Which point in the feasible region represents the greatest number of books (both cookbooks and novels) that Meg could have? Explain how you know.
- Can she display the same number of cookbooks as novels? Explain.
- What point represents the most cookbooks and the fewest novels?
- What point represents the number of cookbooks that would require the longest shelf? How long would the shelf have to be?
- What point represents the number of cookbooks that would require the shortest shelf?



Test (30,0)

$$n = 2c$$

$c$	$n$
10	20
30	60

$$\begin{array}{l} n \geq 2c \\ c \geq n/2 \end{array}$$

0	2(30)
	60
	n/0

a) (50, 200)

b) No

c) (50, 100)

d) (50, 200)

$$W = 0.5(50) + 0.25(200)$$

$$W = 25 + 50$$

$$W = 75 \text{ inches}$$

e)

$0.5(0) + 0.25(200)$	50
$0.5(50) + 0.25(100)$	50

**EXAMPLE #1...**

The vertices of the feasible region of a graph of a system of linear inequalities are  $(-4, -8)$ ;  $(5, 0)$  and  $(1, -6)$ . Which point would result in the minimum value of the objective function  $C = 0.50x - 0.60y$ ?

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	$C = 0.50x - 0.60y$
$(-4, -8)$	$0.5(-4) - 0.6(-8) = 2.8$
$(5, 0)$	$0.5(5) - 0.6(0) = 2.5$
$(1, -6)$	$0.5(1) - 0.6(-6) = 4.1$

**EXAMPLE #2...**

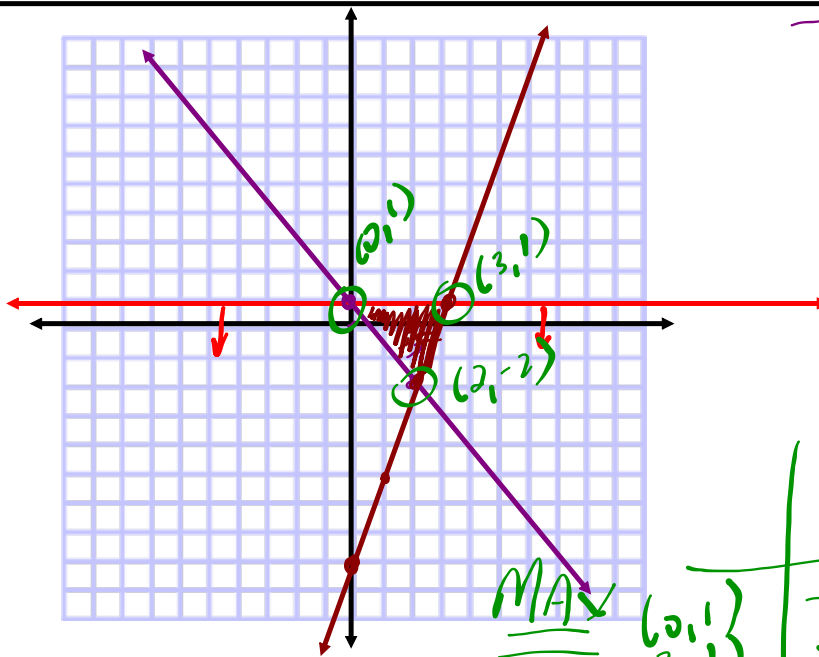
The following model represents an optimization problem. Determine the maximum solution.

Restrictions:  $x \in \mathbb{R}$  and  $y \in \mathbb{R}$

Constraints:  $y \leq 1$ ;  $2y \geq -3x + 2$ ;  $y \geq 3x - 8$

Objective Function:  $D = -4x + 3y$

$y = 1$       $2y = -\frac{3}{2}x + \frac{2}{2}$       $y = 3x - 8$   
 $y = -\frac{3}{2}x + 1$



$2y \geq -3x + 2$   
 $LS \geq RS$   
 $\frac{2(0)}{0} \geq \frac{-3(0) + 2}{2}$       $\frac{0}{0} \geq \frac{-8}{1}$   
 $0 \geq 1$       $0 \geq -8$   
 No     Yes

$D = -4x + 3y$   
 $\left. \begin{matrix} (0, 1) \\ (3, 1) \\ (2, -2) \end{matrix} \right\} \begin{matrix} -4(0) + 3(1) = 3 \\ -4(3) + 3(1) = -9 \\ -4(2) + 3(-2) = -14 \end{matrix}$

## **Practice Questions...**

p. 259: #1, 2, 4, 6, 11, 12, 13