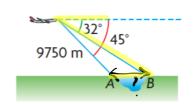
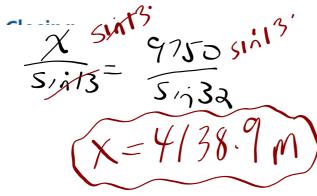
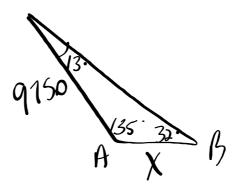
HOMEWORK: More Applications/Word Problems ???

Page 154 #5, 6, 9, 10, 11 (bearings - see example from Friday)
Page 172 #9, 10, 12, 13, 14

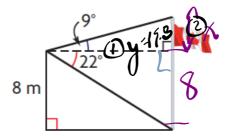
14. A surveyor in an airplane observes that the angles of depression to points *A* and *B*, on opposite shores of a lake, measure 32° and 45°, as shown. Determine the width of the lake, *AB*, to the nearest metre.



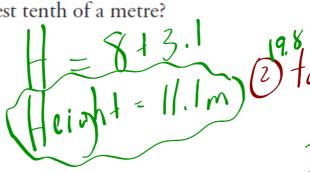




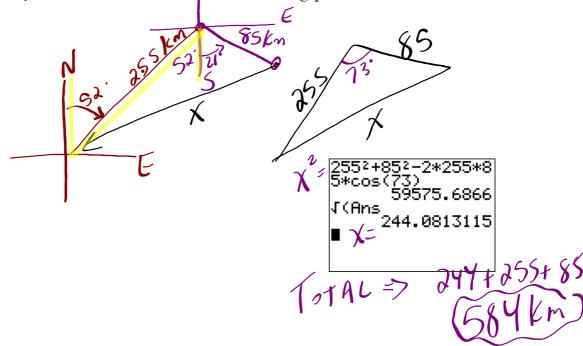
apartment building, the angle of elevation to the top of a flagpole across the



flagpole across the street is 9°. The angle of depression is 22° to the base of the flagpole. How tall is the flagpole, to the nearest tenth of a metre?

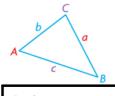


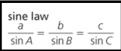
11. A bush pilot delivers supplies to a remote camp by flying 255 km in the direction N52°E. While at the camp, the pilot receives a radio message to pick up a passenger at a village. The village is 85 km S21°E from the camp. What is the total distance, to the nearest kilometre, that the pilot will have flown by the time he returns to his starting point?



Trigonometry Summary AND 'The AMBIGUOUS Case'...

Need to Know

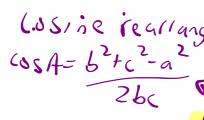




cosine law $a^2 = b^2 + c^2 - 2bc \cos A$

oblique triangle

A triangle that does not contain a 90° angle.



• The sine law and cosine law are used with obtuse triangles in the same way that they are used with acute triangles.

	Use the sine law when you know	Use the cosine law when you know	
	 the lengths of two sides and the measure of the angle that 	- the lengths of two sides and the measure of the contained	
	is opposite a known side	angle	
_		Sn	
	* SSH		
	1		
	- the measures of two angles	- the lengths of all three sides	5
5	SAA	, (5)	
	or		
4	/ /	*	

Be careful when using the sine law to determine the measure of an angle. Ambiguous Case The inverse sine of a ratio always gives an acute angle, but the supplementary angle has the same ratio. You must decide whether the acute angle, θ , or the obtuse angle, $180^{\circ} - \theta$, is the correct angle for your triangle.

Notes - Ambiguous Case.pdf

In Summary

Key Idea

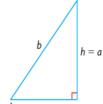
• The ambiguous case of the sine law may occur when you are given two side lengths and the measure of an angle that is opposite one of these sides. Depending on the measure of the given angle and the lengths of the given sides, you may need to construct and solve zero, one, or two triangles.

Need to Know

• In $\triangle ABC$ below, where h is the height of the triangle, $\angle A$ and the lengths of sides a and b are given, and $\angle A$ is acute, there are four possibilities to consider:

If $\angle A$ is acute and a < h, there is no triangle.



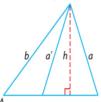


If $\angle A$ is acute and a = h,

If $\angle A$ is acute and a > b or a = b, there is **one triangle.**

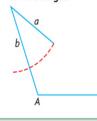


If $\angle A$ is acute and h < a < b, there are two possible triangles.

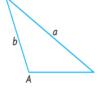


• If $\angle A$, a, and b are given and $\angle A$ is obtuse, there are two possibilities to consider:

If $\angle A$ is obtuse and a < b or a = b, there is no triangle.

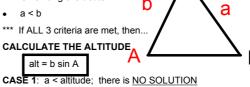


If $\angle A$ is obtuse and a > b, there is one triangle.



Criteria for the Ambiguous Case...

- Must be given SSA
- Given angle is acute
 - a < b



CASE 2: a = altitude; there is <u>ONE SOLUTION</u> [Right Triangle]

CASE 3: a >altitude; this is the 'AMBIGUOUS CASE'...TWO SOLUTIONS

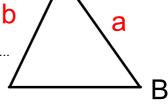
- 1) Acute Triangle (angle, θ , is found with Law of Sines)
- 2) Obtuse Triangle (angle is 180° θ)

MUST
MEMORIZE
THESE
NOTES
IN ORDER
TO KNOW
AMBIGUOUS
CASE

Criteria for the Ambiguous Case...

- Must be given SSA
- · Given angle is acute
- a < b

*** If ALL 3 criteria are met, then...



CALCULATE THE ALTITUDE

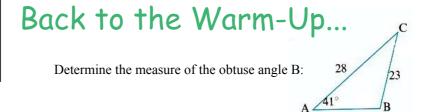
alt = b sin A

CASE 1: a < altitude; there is NO SOLUTION

CASE 2: a = altitude; there is <u>ONE SOLUTION</u> [Right Triangle]

CASE 3: a >altitude; this is the 'AMBIGUOUS CASE'...TWO SOLUTIONS

- 1) Acute Triangle (angle, θ , is found with Law of Sines)
- 2) Obtuse Triangle (angle is $180^{\circ} \theta$)



EXAMPLE 1

Connecting the SSA situation to the number of possible triangles

Given each SSA situation for $\triangle ABC$, determine how many triangles are possible.

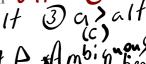
/ a < b a(+=12sin 30

- a) $\angle A = 30^{\circ}$, a = 4 m, and b = 12 m
- c) $\angle A = 30^{\circ}$, a = 8 m, and b = 12 m
- **b)** $\angle A = 30^{\circ}$, a = 6 m, and b = 12 m
- d) $\angle A = 30^{\circ}$, a = 15 m, and b = 12 m \bigcirc

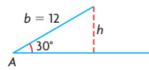




Dacalt Dacalt



Saskia's Solution



I drew the beginning of a triangle with a 30° angle and a 12 m side.

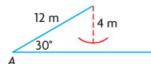
 $\sin 30^\circ = \frac{h}{12}$

I used the sine ratio to calculate the height of the triangle.

 $12 \sin 30^\circ = h$ 6 m = h

I can use this height as a benchmark to decide on side lengths opposite the 30° angle that will result in zero, one, or two triangles.

a) $\angle A = 30^{\circ}$, a = 4 m, and b = 12 m

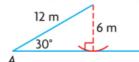


Since a < b and a < h, I knew that no triangles are possible.

I used a compass to be certain. I set the compass tips to represent 4 m. I placed one tip of the compass at the open end of the 12 m side and swung the pencil tip toward the other side. The pencil couldn't reach the base, so a 4 m side could not close the triangle.

No triangles are possible.

b) $\angle A = 30^{\circ}$, a = 6 m, and b = 12 m

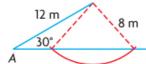


Since a < b and a = h, there is only one possible triangle, a right triangle.

A compass arc intersects the base at only one point.

One triangle is possible.

c) $\angle A = 30^{\circ}$, a = 8 m, and b = 12 m

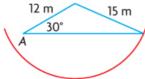


Since a < b and a > h, there are two possible triangles.

A compass arc intersects the base at two points.

Two triangles are possible.

d) $\angle A = 30^{\circ}$, a = 15 m, and b = 12 m



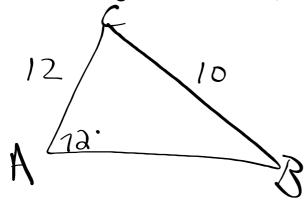
Since a > b, only one triangle is possible.

A compass arc intersects the base at only one point.

One triangle is possible.

Example 2:

Solve the triangle ABC if a = 10, b = 12 and angle $A = 72^{\circ}$.

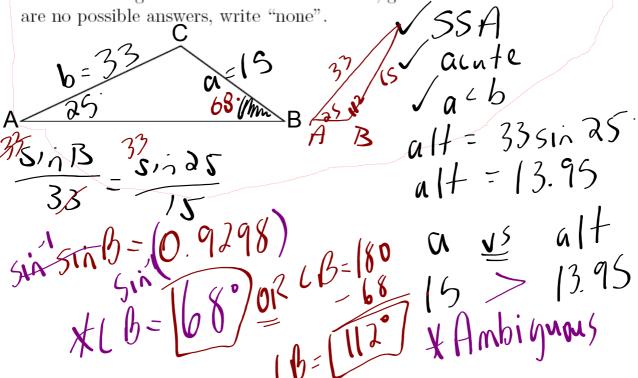


angle
$$A = 72$$
.

 $X \leq SA$
 $V = angle acute$
 $V = a \leq b$
 $alt = 12\sin 7a$
 $alt = 11.41$
 $alt = 11.41$
 $alt = 11.41$

Example 3:

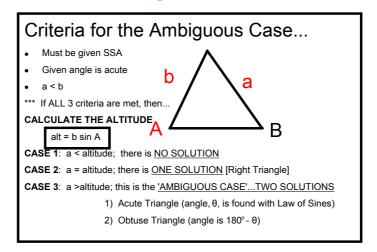
Given that $A = 25^{\circ}$, a = 15, and b = 33, find the measure of angle B to the nearest degree. If there are two answers, give both of them. If there are no possible answers, write "none".



HOMEWORK...

Worksheet - Ambiguous Case.pdf

Do questions #1, 2 & 4 **MEMORIZE!!!**



Notes - Ambiguous Case.pdf

Worksheet - Ambiguous Case.pdf