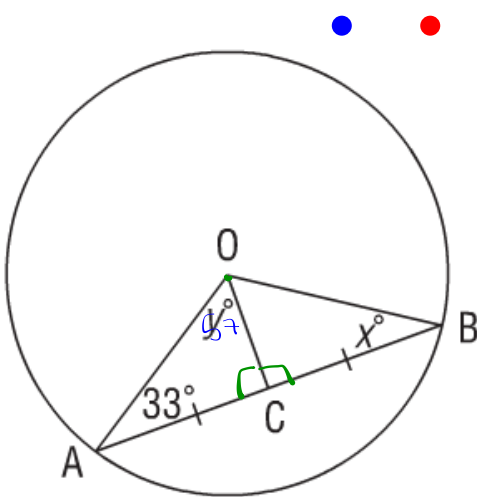


## Determining the Measure of Angles in a Triangle

Example #1. Determine the values of  $x^\circ$  and  $y^\circ$ .



$$\angle OCA = 90^\circ \quad (\text{chord } \overline{AB})$$

$$\angle OCB = 90^\circ$$

$$y = 57^\circ \quad (180 - 90 - 33^\circ)$$

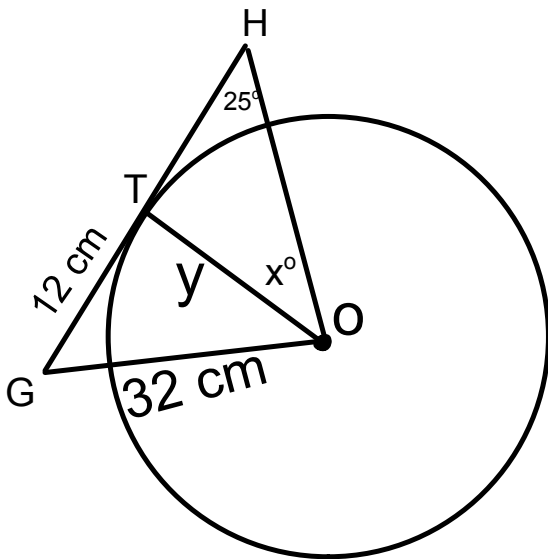
$$(S A T T)$$

$$x = 33^\circ \quad (I T T)$$

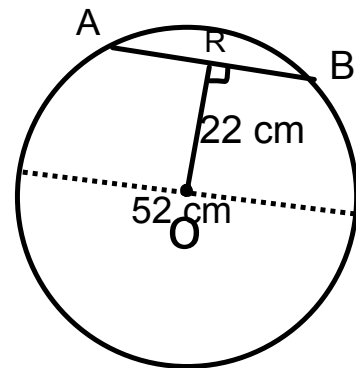
# Warm Up

Day 2

Determine the unknowns:



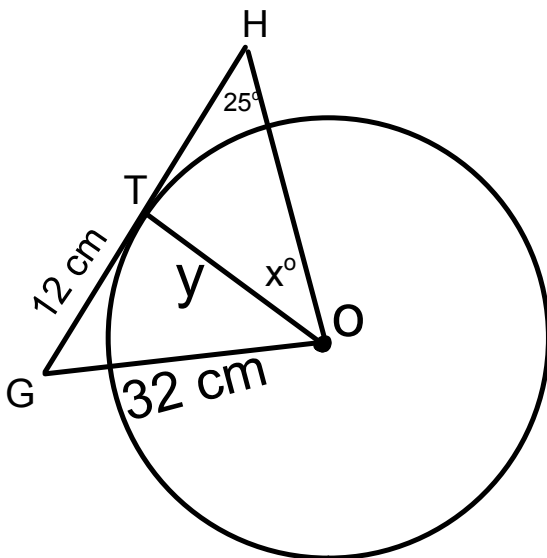
What is the length of the cord AB?



# Warm Up

## Day 2

Determine the unknowns:



$$\left. \begin{array}{l} \angle OTH = 90^\circ \\ \angle OTG = 90^\circ \end{array} \right\} \text{(Tang P)}$$

$$x = 65^\circ \text{ (SATT)}$$

or

$$180 - 90 - 25$$

$$y \Rightarrow \text{leg}$$

$$a^2 = c^2 - b^2$$

$$a^2 = 32^2 - 12^2$$

$$a^2 = 1024 - 144$$

$$\sqrt{a^2} = \sqrt{880}$$

$$a = 29.7 \text{ cm}$$

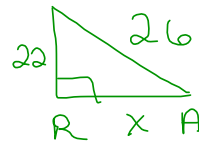
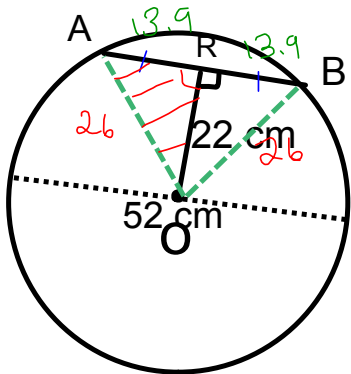
# Warm Up

Day 2

Determine the unknowns:

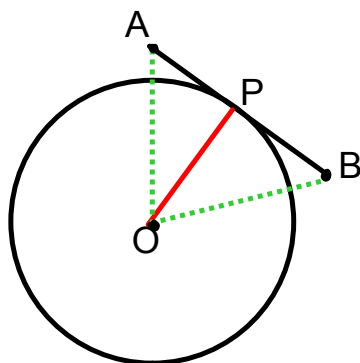
What is the length of the cord AB?

$$AR = BR \quad (\text{Chord 1})$$



$$\begin{aligned} RA \\ a^2 &= c^2 - b^2 \\ a^2 &= 26^2 - 22^2 \\ a^2 &= 676 - 484 \\ \sqrt{a^2} &= \sqrt{192} \\ a &= 13.9 \end{aligned}$$

$$\begin{aligned} AB &= 2(13.9) \\ &= 27.8 \text{ cm} \end{aligned}$$



Tangent Properties:

$$\angle APO = 90^\circ \text{ (Tang P)}$$

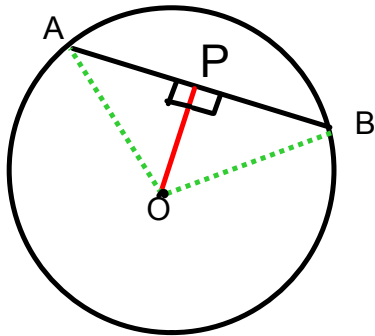
$$\angle BPO = 90^\circ \text{ (Tang P)}$$

To Solve use:

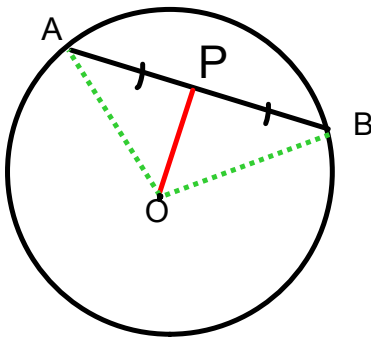
$$\text{Angle} = \underline{\quad}^\circ \text{ (SATT)}$$

$$\text{Side} = \underline{\quad} \text{ cm (Pythagorean theorem)}$$

## Chord Properties:

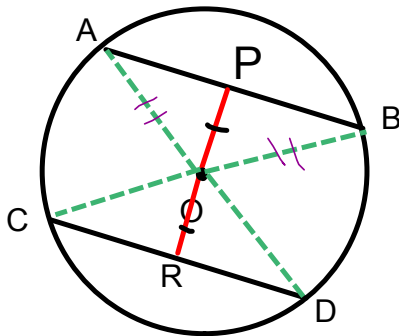


$$AP = PB \text{ (Chord P 1)}$$



$$\angle APO = 90^\circ \text{ (Chord P 3)}$$

$$\angle BPO = 90^\circ \text{ (Chord P 3)}$$



$$AB = CD \text{ (Chord P 4)}$$

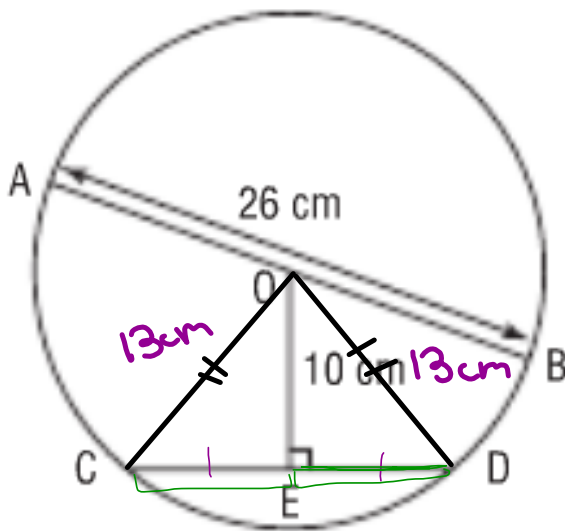
To Solve use:

$$\text{Angle} = \underline{\quad}^\circ \text{ (SATT) or (ITT)}$$

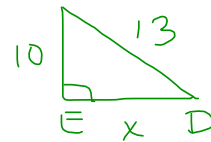
$$\text{Side} = \underline{\quad} \text{ cm (Pythagorean theorem)}$$

## Using the Pythagorean Theorem in a Circle

Example #2. What is the length of chord CD, to the nearest tenth?



$$CE = ED \text{ (Chord P)}$$



$$ED = x$$

$$a^2 = c^2 - b^2$$

$$\sqrt{a^2} = \sqrt{13^2 - 10^2}$$

$$a = 8.3 \text{ cm}$$

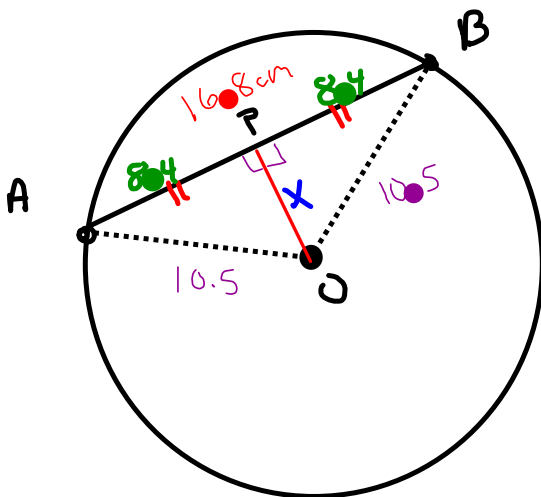
$$CD = 2(8.3)$$

$$= 16.6$$

## EXAMPLE...

A chord that is 16.8 cm in length, is drawn in a circle that has a ~~diameter~~ of 21 cm. How far is the chord from the center of the circle?

$$r = 10.5$$



$$\begin{array}{l} AP = 8.4 \\ PB = 8.4 \end{array} \left. \vphantom{\begin{array}{l} AP = 8.4 \\ PB = 8.4 \end{array}} \right\} \begin{array}{l} \text{Ch P} \\ 1, 2, 3 \end{array}$$

O P

$$a^2 = c^2 - b^2$$

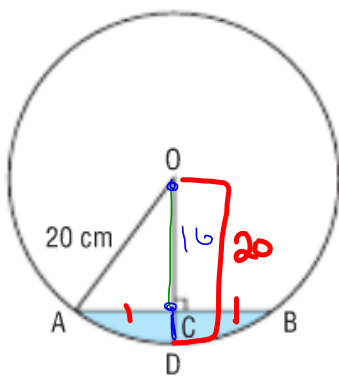
$$\sqrt{a^2} = \sqrt{10.5^2 - 8.4^2}$$

$$a = 6.3 \text{ cm}$$



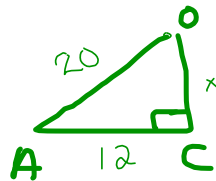
## Solving Problems Using the Property of a Chord and its Perpendicular

Example #3. Determine the length of CD.



$$AB = 24 \text{ cm}$$

$$AC = 12 \quad \left. \begin{array}{l} AC = 12 \\ CB = 12 \end{array} \right\} \text{(Chord P1,2,3)}$$



$$x \Rightarrow \text{leg}$$

$$a^2 = c^2 - b^2$$

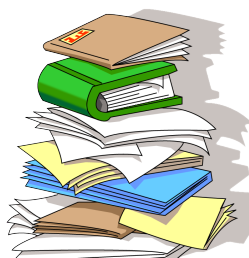
$$\sqrt{a^2} = \sqrt{20^2 - 12^2}$$

$$a = \sqrt{256}$$

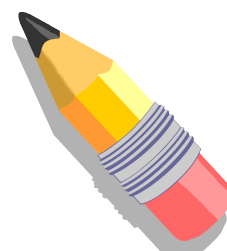
$$a = 16$$

$$CD = 20 - 16$$

$$= 4$$



## Homework :



p.397 - 398

Questions: 3, 4, 5, 6

6, 7(b), 10(a), 11, 14, 15