

MAY 30, 2017

**UNIT 4: SYSTEMS OF LINEAR
EQUATIONS**

**7.2: SOLVING A SYSTEM OF
LINEAR EQUATIONS
GRAPHICALLY**

**M. MALTBY INGERSOLL
*NUMBERS, RELATIONS AND FUNCTIONS 10***



WHAT'S THE POINT OF TODAY'S LESSON?

We will begin working on the NRF 10 Specific Curriculum Outcome (SCO) "Relations and Functions 10" OR "RF10" which states:

RF10: "Solve problems that involve systems of equations in two variables graphically and algebraically."



What does THAT mean???

SCO RF10 means that we will:

- * model a situation using a system of linear equations
- * relate a system of linear equations to the context of a problem
- * determine and verify the solution of a system of linear equations graphically
- * explain the meaning of the point of intersection of a system of linear equations
- * determine and verify the solution of a system of linear equations algebraically
- * explain, using examples, why a system of equations may have no solution, one solution or an infinite number of solutions
- * explain a strategy to solve a system of linear equations
- * solve a problem that involves a system of linear equations



HOMEWORK QUESTIONS???

(Distance / Midpoint Worksheets)

DEFINITION - SYSTEM OF LINEAR EQUATIONS:

Two equations of linear functions in the same two variables.

EXAMPLE: $12x + 24y = 780$
 $x = y + 20$

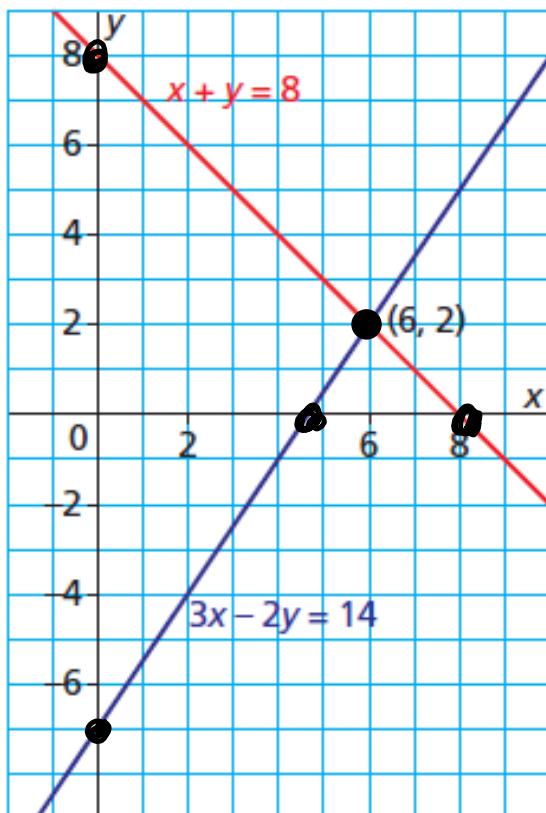
Systems of Linear Equations can be solved GRAPHICALLY (7.2) and also by using SUBSTITUTION (7.4) and ELIMINATION (7.5).

**Solving Systems
of Linear
Equations
Graphically:**

Solve this linear system.

$$x + y = 8 \quad (\text{x-int.} = 8; \text{y-int.} = 8)$$

$$3x - 2y = 14 \quad (\text{x-int.} = 4\frac{2}{3}; \text{y-int.} = -7)$$



The point of intersection appears to be $(6, 2)$.

Verify the solution. In each equation, substitute: $x = 6$ and $y = 2$

(6 , 2) : Solution???

$$\mathbf{x + y = 8}$$

$$\mathbf{6 + 2 = 8}$$

$$\mathbf{8 = 8}$$

$$\mathbf{3x - 2y = 14}$$

$$\mathbf{3(6) - 2(2) = 14}$$

$$\mathbf{18 - 4 = 14}$$

$$\mathbf{14 = 14}$$

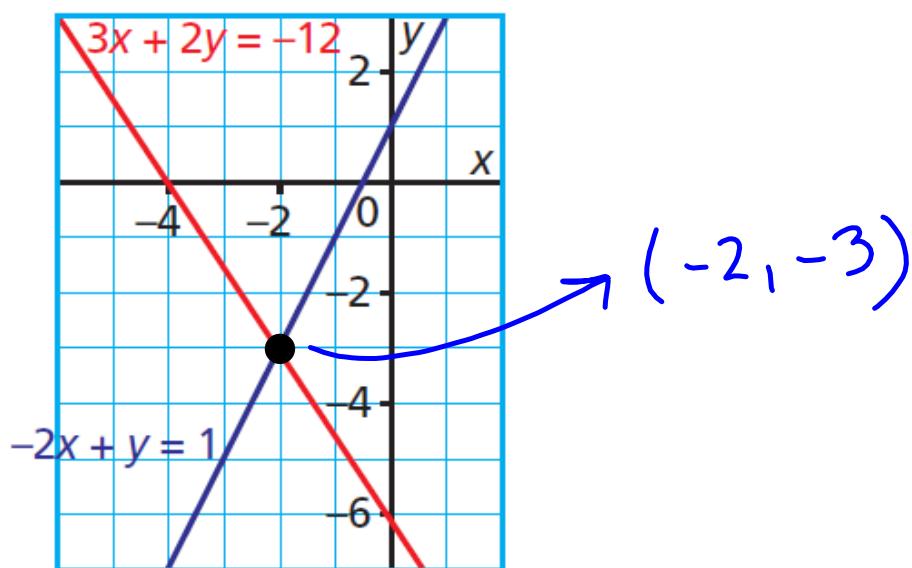
For each equation, the left side is equal to the right side.
So, $x = 6$ and $y = 2$ is the solution of the linear system.

SOLVING SYSTEMS OF LINEAR EQUATIONS GRAPHICALLY:

The solution of a linear system can be estimated by graphing both equations on the same grid. If the two lines intersect, the coordinates (x, y) of the point of intersection are the solution of the linear system.

Each equation of this linear system is graphed on a grid.

$$\begin{array}{ll} 3x + 2y = -12 & \textcircled{1} \quad (\text{x-int.} = -4 ; \text{y-int.} = -6) \\ -2x + y = 1 & \textcircled{2} \quad (\text{x-int.} = -0.5 ; \text{y-int.} = 1) \end{array}$$



(-2 , -3) : Solution???

$$3x + 2y = -12$$

$$-2x + y = 1$$

$$3(-2) + 2(-3) = -12$$

$$-2(-2) + (-3) = 1$$

$$(-6) + (-6) = -12$$

$$4 - 3 = 1$$

$$-12 = -12$$

$$1 = 1$$

For each equation, the left side is equal to the right side.

Since $x = -2$ and $y = -3$ satisfy each equation, these numbers are the solution of the linear system.

HOMEWORK:

- a) Write a linear system to model this situation:

To visit the Head-Smashed-In Buffalo Jump interpretive centre near Fort Macleod, Alberta, the admission fee is \$5 for a student and \$9 for an adult. In one hour, 32 people entered the centre and a total of \$180 in admission fees was collected.

- b) Graph the linear system then solve this problem: How many students and how many adults visited the centre during this time?

Attachments

Worksheet - Review of Coordinate Geometry (Math 10).doc

area of a triangle.doc

coord geom review.doc

Puzzle Worksheet - Graphing #2 (Coffee).pdf

Puzzle Worksheet - Graphing #1 (Cow).pdf

Puzzle Worksheet - Slope Point (given both).pdf

Puzzle Worksheet - Slope Point (given two points).pdf

Worksheet - Equation of a Line.pdf

Worksheet Solutions - Equation of a Line.pdf

Worksheet - Distance_Midpoint(2).pdf

Review - Coordinate Geometry.pdf