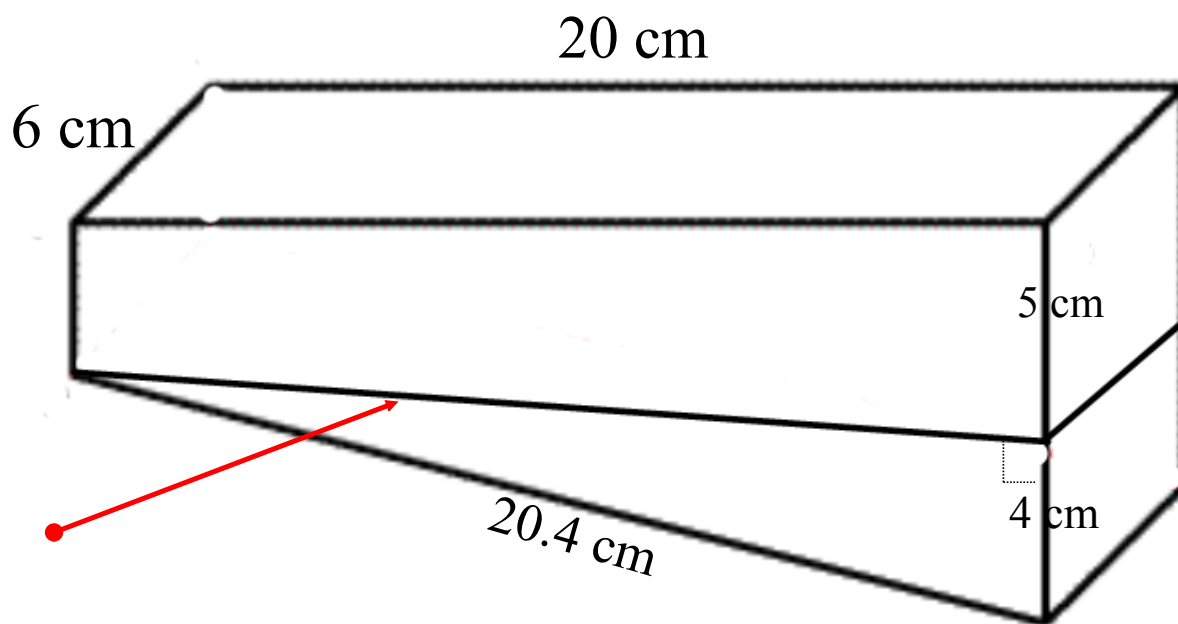


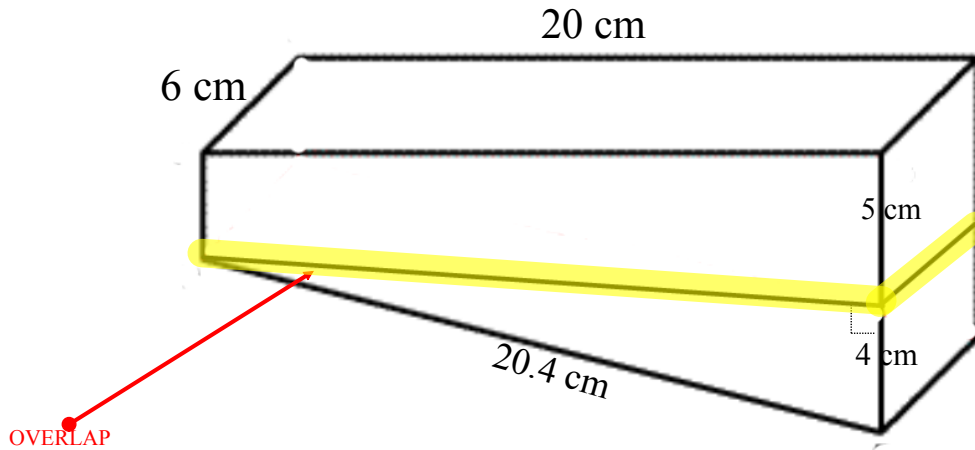
Warm Up



OVERLAP

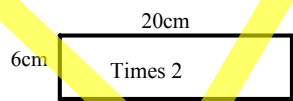
Calculate the surface area

Method 1)



Step 1) Calculate the Surface area of each Prism INDIVIDUALLY

Rectangular prism (Surface)

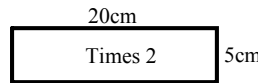


$$A = 6\text{cm} \times 20\text{ cm}$$

$$= 120\text{ cm}^2$$

$$2(120)\text{ cm}^2$$

$$240\text{ cm}^2$$

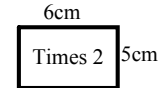


$$A = 5\text{cm} \times 20\text{ cm}$$

$$= 100\text{ cm}^2$$

$$2(100\text{ cm}^2)$$

$$200\text{ cm}^2$$



$$A = 5\text{cm} \times 6\text{ cm}$$

$$= 30\text{ cm}^2$$

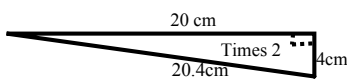
$$2(30\text{ cm}^2)$$

$$60\text{ cm}^2$$

$$\text{Area of rectangular prims} = 240\text{ cm}^2 + 200\text{ cm}^2 + 60\text{ cm}^2$$

$$= 500\text{ cm}^2$$

Triangular Prism

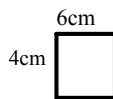


$$A = (20\text{ cm} \times 4\text{ cm}) / 2$$

$$= (80\text{ cm}^2) / 2$$

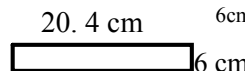
$$= 40\text{ cm}^2$$

$$2A = 80\text{ cm}^2$$



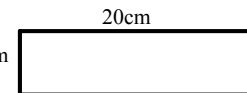
$$A = 4\text{ cm} \times 6\text{ cm}$$

$$= 24\text{ cm}^2$$



$$A = 20.4\text{ cm} \times 6\text{ cm}$$

$$= 122.4\text{ cm}^2$$



$$A = 6\text{ cm} \times 20\text{ cm}$$

$$= 120\text{ cm}^2$$

$$\text{Area of triangular prism}$$

$$= 80\text{ cm}^2 + 24\text{ cm}^2 + 122.4\text{ cm}^2 + 120\text{ cm}^2$$

$$= 346.4\text{ cm}^2$$

Total Surface Area = Rectangular prism + Triangular Prism - (OVERLAP)

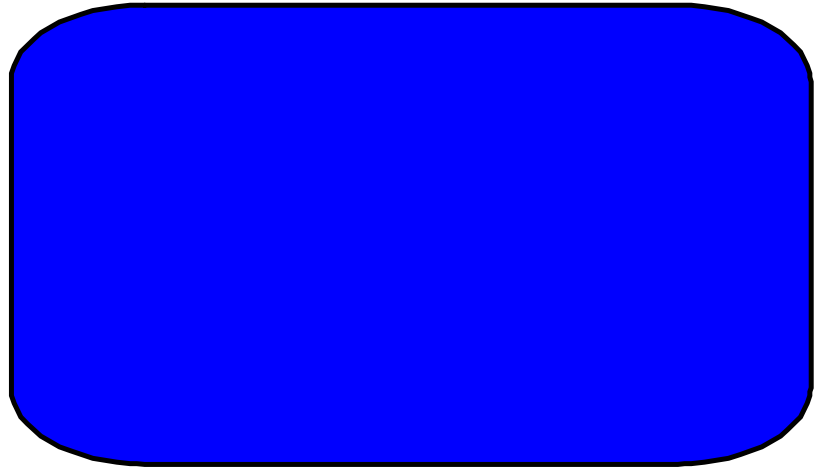
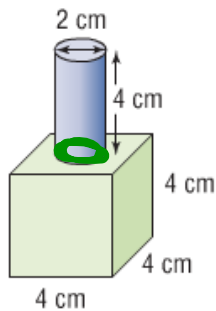
$$= (500\text{ cm}^2) + 346.4\text{ cm}^2 - 240\text{ cm}^2$$

$$= 606.4\text{ cm}^2$$

Homework solutions

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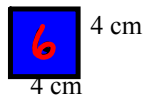
3 a) cylinder on a cube



$$\begin{aligned}
 \text{Area of cylinder} &= 2\pi r^2 + 2\pi rh \\
 &= 2(3.14)(1\text{cm})^2 + 2(3.14)(1\text{cm})(4\text{cm}) \\
 &= 2(3.14)(1\text{cm}) + 2(3.14)(1\text{cm})(4\text{cm}) \\
 &= 6.28 \text{ cm}^2 + 25.12 \text{ cm}^2 \\
 &= 31.4 \text{ cm}^2
 \end{aligned}$$



Cube

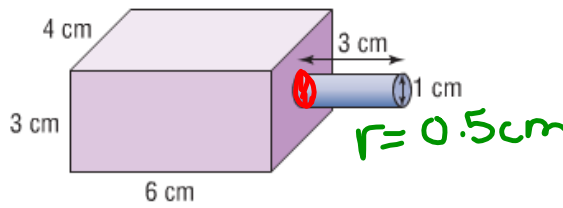


$$\begin{aligned}
 \text{area} &= 4\text{cm} \times 4\text{cm} \\
 &= 16 \text{ cm}^2
 \end{aligned}$$

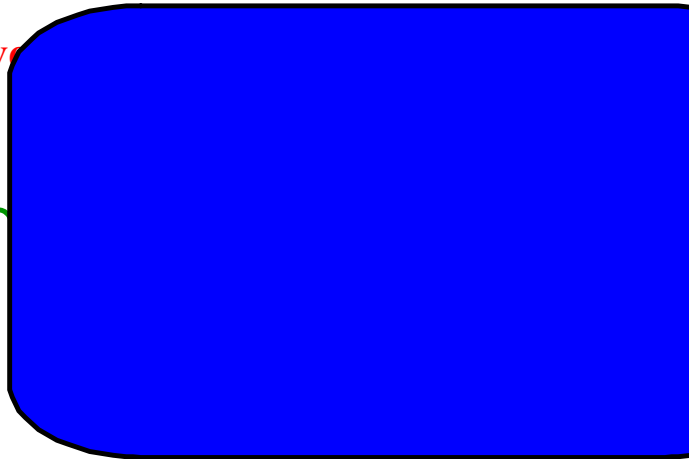
$$\begin{aligned}
 \text{Area} &= 6 \text{ faces} \times (\text{area of one face}) \\
 &= 6 \times (16 \text{ cm}^2) \\
 &= 96 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Total SA} &= \text{Cylinder} + \text{Cube} - \text{Overlap} \\
 &= 31.4 \text{ cm}^2 + 96 \text{ cm}^2 - 6.28 \text{ cm}^2 \\
 &= 121.12 \text{ cm}^2 \\
 &= 121 \text{ cm}^2
 \end{aligned}$$

3 b) cylinder on a rectangular prism

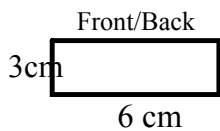


Overlap

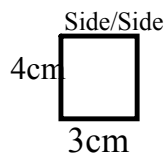


$$\begin{aligned}
 \text{Area of cylinder} &= 2\pi r^2 + 2\pi rh \\
 &= 2(3.14)(0.5\text{cm})^2 + 2(3.14)(0.5\text{cm})(3\text{cm}) \\
 &= 2(3.14)(0.25\text{cm}) + 2(3.14)(0.5\text{cm})(3\text{cm}) \\
 &= 1.57\text{ cm}^2 + 9.42\text{ cm}^2 \\
 &= 10.99\text{ cm}^2
 \end{aligned}$$

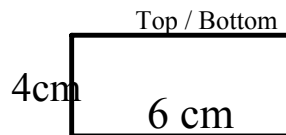
Rectangular Prism



$$\begin{aligned}
 A &= 3\text{cm} \times 6\text{ cm} \\
 &= 18\text{ cm}^2 \\
 2A &= 36
 \end{aligned}$$



$$\begin{aligned}
 A &= 3\text{cm} \times 4\text{ cm} \\
 &= 12\text{ cm}^2 \\
 2A &= 24
 \end{aligned}$$



$$\begin{aligned}
 A &= 4\text{cm} \times 6\text{ cm} \\
 &= 24\text{ cm}^2 \\
 2A &= 48
 \end{aligned}$$

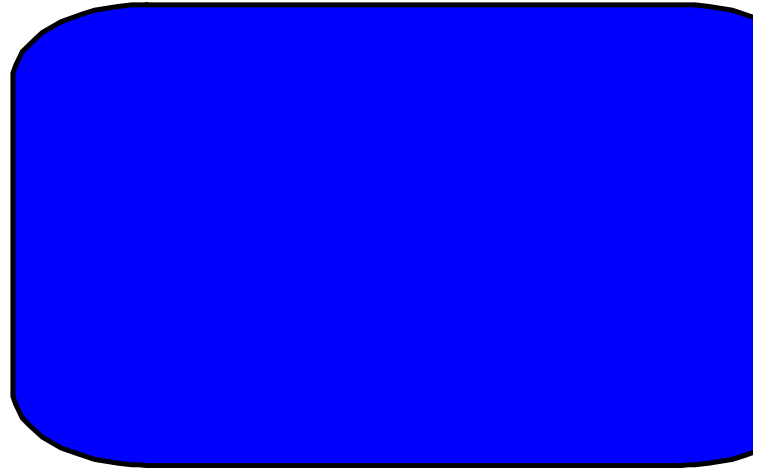
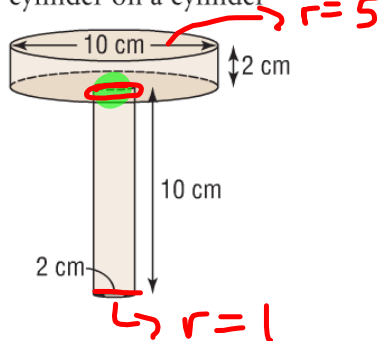
$$\begin{aligned}
 \text{Rectangular Prism SA} &= 2(18\text{ cm}^2) + 2(12\text{cm}^2) + 2(24\text{cm}^2) \\
 &= 36\text{ cm}^2 + 24\text{cm}^2 + 48\text{cm}^2 \\
 &= 108\text{cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Total SA} &= \text{Cylinder} + \text{Rect Prism} - \text{Overlap} \\
 &= 10.99\text{ cm}^2 + 108\text{ cm}^2 - 1.57\text{ cm}^2 \\
 &= 117.42\text{ cm}^2 \\
 &= 117\text{ cm}^2
 \end{aligned}$$

Homework solutions

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3c c) cylinder on a cylinder

long tube

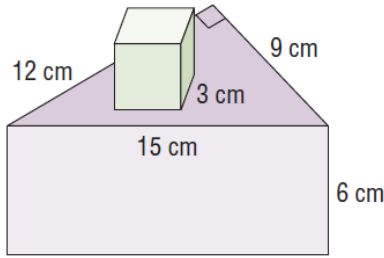
$$\begin{aligned}
 \text{Area of cylinder} &= 2\pi r^2 + 2\pi rh \\
 &= 2(3.14)(1\text{cm})^2 + 2(3.14)(1\text{cm})(10\text{cm}) \\
 &= 2(3.14)(1\text{cm}) + 2(3.14)(1\text{cm})(10\text{cm}) \\
 &= 6.28 \text{ cm}^2 + 62.8 \text{ cm}^2 \\
 &= 69.08 \text{ cm}^2
 \end{aligned}$$

puck shape

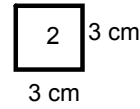
$$\begin{aligned}
 \text{Area of 2nd cylinder} &= 2\pi r^2 + 2\pi rh \\
 &= 2(3.14)(5\text{cm})^2 + 2(3.14)(5\text{cm})(2\text{cm}) \\
 &= 2(3.14)(25\text{cm}) + 2(3.14)(5\text{cm})(2\text{cm}) \\
 &= 157 \text{ cm}^2 + 62.8 \text{ cm}^2 \\
 &= 219.8 \text{ cm}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Total SA} &= \text{Cylinder} + \text{Cylinder} - \text{Overlap} \\
 &= 69.08 \text{ cm}^2 + 219.8 \text{ cm}^2 - 6.28 \text{ cm}^2 \\
 &= 282.6 \text{ cm}^2 \\
 &= 283 \text{ cm}^2
 \end{aligned}$$

d) cube on a triangular prism



Over lap



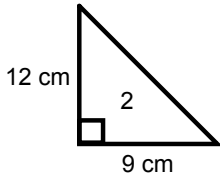
$$A = b \times h$$

$$A = 3 \times 3$$

$$A = 9 \text{ cm}^2$$

$$2A = 18 \text{ cm}^2$$

Triangular Prism



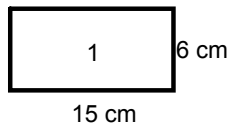
$$A = \frac{b \times h}{2}$$

$$A = \frac{9 \times 12}{2}$$

$$A = \frac{108}{2}$$

$$A = 54$$

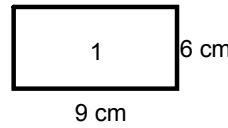
$$2A = 108 \text{ cm}^2$$



$$A = b \times h$$

$$A = 15 \times 6$$

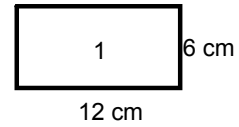
$$A = 90 \text{ cm}^2$$



$$A = b \times h$$

$$A = 9 \times 6$$

$$A = 54 \text{ cm}^2$$



$$A = b \times h$$

$$A = 12 \times 6$$

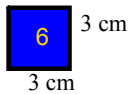
$$A = 72 \text{ cm}^2$$

$$\text{Total SA Large} = 2 \text{ Triangles} + \text{Side} + \text{Side} + \text{Side}$$

$$= 108 + 90 + 54 + 72$$

$$= 324 \text{ cm}^2$$

Cube



$$A = b \times h$$

$$A = 3 \times 3$$

$$A = 9 \text{ cm}^2$$

$$\text{Area} = 6 \text{ faces} \times (\text{area of one face})$$

$$= 6 \times (9 \text{ cm}^2)$$

$$= 54 \text{ cm}^2$$

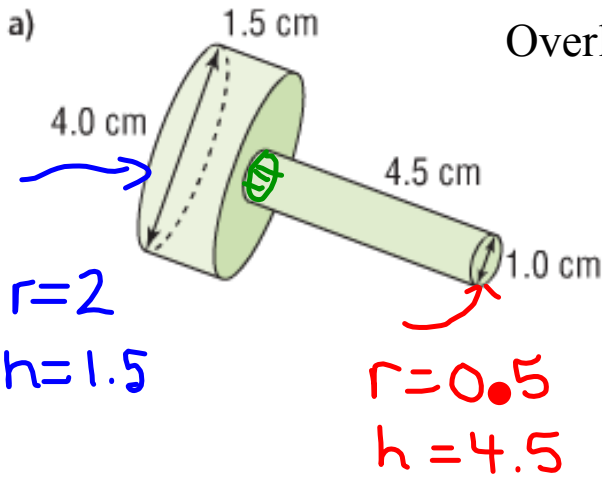
$$\text{Total SA} = \text{Triangular Prism} + \text{Cube} - \text{Overlap}$$

$$= 324 \text{ cm}^2 + 54 \text{ cm}^2 - 18 \text{ cm}^2$$

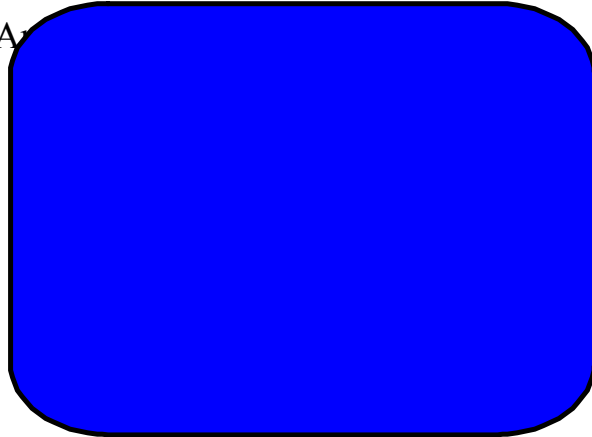
$$= 360 \text{ cm}^2$$

4

a)



Overlap:



Top

$$\begin{aligned} \text{Area of cylinder} &= 2\pi r^2 + 2\pi rh \\ &= 2(3.14)(2\text{cm})^2 + 2(3.14)(2\text{cm})(1.5\text{cm}) \\ &= 2(3.14)(4\text{cm}) + 2(3.14)(2\text{cm})(1.5\text{cm}) \\ &= 25.12 \text{ cm}^2 + 18.84 \text{ cm}^2 \\ &= 43.96 \text{ cm}^2 \end{aligned}$$

Overlap

Long

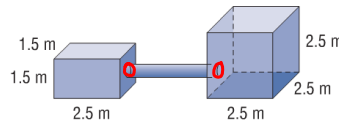
$$\begin{aligned} \text{Area of cylinder} &= 2\pi r^2 + 2\pi rh \\ &= 2(3.14)(0.5\text{cm})^2 + 2(3.14)(0.5\text{cm})(4.5\text{cm}) \\ &= 2(3.14)(0.25\text{cm}) + 2(3.14)(0.5\text{cm})(4.5\text{cm}) \\ &= 1.57 \text{ cm}^2 + 14.13 \text{ cm}^2 \\ &= 15.7 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Total SA} &= \text{Cylinder} + \text{Cylinder} - \text{Overlap} \\ &= 43.96 \text{ cm}^2 + 15.7 \text{ cm}^2 - 1.57 \text{ cm}^2 \\ &= 58.09 \text{ cm}^2 \\ &= 58.1 \text{ cm}^2 \end{aligned}$$

Homework solutions

Solutions

- 4 b) The cylinder is 3.5 m long with diameter 0.5 m.



overlap 1

$$\begin{aligned}
 A &= \pi r^2 \\
 &= (3.14) (0.25\text{m})^2 \\
 &= (3.14) (0.0625\text{m}) \\
 &= 0.19625\text{m}^2 \\
 &\quad \times 2 \text{ for face involved} \\
 &= 0.3925\text{m}^2
 \end{aligned}$$

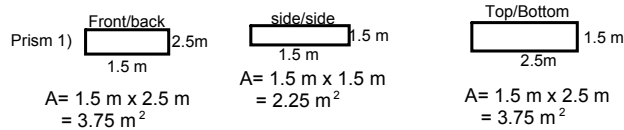
Overlap 2

$$\begin{aligned}
 A &= \pi r^2 \\
 &= (3.14) (0.25\text{m})^2 \\
 &= (3.14) (0.0625\text{m}) \\
 &= 0.19625\text{m}^2 \\
 &\quad \times 2 \text{ for face involved} \\
 &= 0.3925\text{m}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{total overlap} &= \text{overlap 1} + \text{overlap 2} \\
 &= 0.3925\text{m}^2 + 0.3925\text{m}^2 \\
 &= 0.785\text{m}^2
 \end{aligned}$$

overlap x 2

$$\begin{aligned}
 \text{Area of cylinder} &= 2\pi r^2 + 2\pi rh \\
 &= 2(3.14)(0.0625\text{m}^2) + 2(3.14)(0.25\text{m})(3.5\text{m}) \\
 &= 0.3925\text{m}^2 + 5.495\text{m}^2 \\
 &= 5.8875\text{m}^2
 \end{aligned}$$



$$\begin{aligned}
 \text{SA Prism 1} &= 2(3.75\text{m}^2) + 2(2.25\text{m}^2) + 2(3.75\text{m}^2) \\
 &= 7.5\text{m}^2 + 4.5\text{m}^2 + 7.5\text{m}^2 \\
 &= 19.5\text{m}^2
 \end{aligned}$$

Cube)

$$\begin{aligned}
 \text{Surface area of 1 face} &= 2.5\text{m} \times 2.5\text{m} \\
 &= 6.25\text{m}^2 \\
 &\quad \times 6 \leftarrow 6 \text{ equal faces} \\
 &= 37.5\text{m}^2
 \end{aligned}$$

$$\begin{aligned}
 \text{Total SA} &= \text{Rectangular Prism} + \text{Cube} + \text{Cylinder} - \text{Total Overlap} \\
 &= 19.5\text{m}^2 + 37.5\text{m}^2 + 5.8875\text{m}^2 - 0.785\text{m}^2 \\
 &= 61.6025\text{m}^2
 \end{aligned}$$

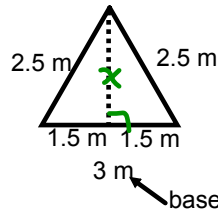
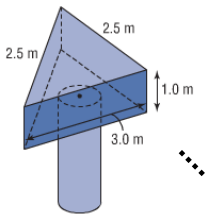
4 circles

Or if you rounded to the nearest tenth

$$\begin{aligned}
 \text{Total SA} &= \text{Rectangular Prism} + \text{Cube} + \text{Cylinder} - \text{Total Overlap} \\
 &= 19.5\text{m}^2 + 37.5\text{m}^2 + 5.8875\text{m}^2 - 0.785\text{m}^2 \\
 &= 19.5\text{m}^2 + 37.5\text{m}^2 + 5.9\text{m}^2 - 0.8\text{m}^2 \\
 &= 62.1\text{m}^2
 \end{aligned}$$

5. Determine the surface area of each composite object.

a) The cylinder is 2.5 m long with radius 0.5 m.

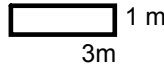
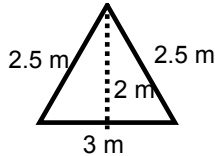


Missing Side

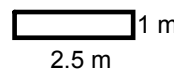
$$\begin{aligned} \text{height}^2 &= c^2 - b^2 \\ &= (2.5 \text{ m})^2 - (1.5 \text{ m})^2 \\ &= 6.25 \text{ m}^2 - 2.25 \text{ m}^2 \\ &= 4 \text{ m}^2 \\ \text{height} &= \sqrt{4 \text{ m}^2} \\ \text{height} &= 2 \text{ m} \end{aligned}$$

Triangular prism

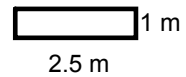
$$\begin{aligned} A &= \frac{b \times h}{2} \\ A &= \frac{3 \text{ m} \times 2 \text{ m}}{2} \\ A &= \frac{6 \text{ m}^2}{2} \\ A &= 3 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 3 \text{ m} \times 1 \text{ m} \\ &= 3 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 2.5 \text{ m} \times 1 \text{ m} \\ &= 2.5 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 2.5 \text{ m} \times 1 \text{ m} \\ &= 2.5 \text{ m}^2 \end{aligned}$$

●

$$\begin{aligned} \text{Total SA Triangular Prism} &= 2 \text{ triangles} + \text{rectangle} + \text{rectangle} + \text{rectangle} \\ &= 2 (3 \text{ m}^2) + 3 \text{ m}^2 + 2.5 \text{ m}^2 + 2.5 \text{ m}^2 \\ &= 6 \text{ m}^2 + 3 \text{ m}^2 + 2.5 \text{ m}^2 + 2.5 \text{ m}^2 \\ &= 14 \text{ m}^2 \end{aligned}$$

Cylinder

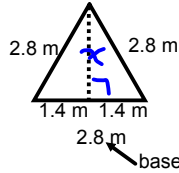
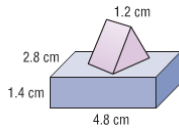
$$\begin{aligned} \text{Area of cylinder} &= 2\pi r^2 + 2\pi rh \\ &= 2(3.14)(0.5)^2 + 2(3.14)(0.5)(2.5) \\ &= 2(3.14)(0.25) + 2(3.14)(0.5)(2.5) \\ &= 1.57 \text{ m}^2 + 7.85 \text{ m}^2 \\ &= 9.42 \text{ m}^2 \end{aligned}$$

Area of Overlap

$$\begin{aligned} \text{Area of circle} &= \pi r^2 \\ &= (3.14)(0.5)^2 \\ &= (3.14)(0.25) \\ &= 0.785 \text{ m}^2 \\ &\quad \times 2 \text{ faces} \\ \hline &= 1.57 \text{ m}^2 \end{aligned}$$

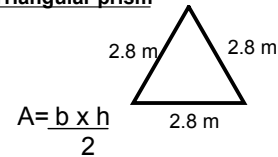
$$\begin{aligned} \text{Total Surface} &= \text{Triangular Prism} + \text{Cylinder} - \text{total overlap} \\ &= 14 \text{ m}^2 + 9.42 \text{ m}^2 - 1.57 \text{ m}^2 \\ &= 21.85 \text{ m}^2 \end{aligned}$$

b) The base of the triangular prism is an equilateral triangle with side length 2.8 cm.

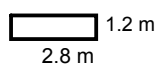


$$\begin{aligned} \text{height}^2 &= c^2 - b^2 \\ &= (2.8 \text{ m})^2 - (1.4 \text{ m})^2 \\ &= 7.84 \text{ m}^2 - 1.96 \text{ m}^2 \\ &= 5.88 \text{ m}^2 \\ \text{height} &= \sqrt{5.88 \text{ m}^2} \\ \text{height} &= 2.4 \text{ m} \end{aligned}$$

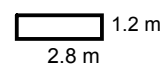
Triangular prism



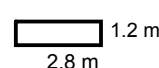
$$\begin{aligned} A &= \frac{b \times h}{2} \\ A &= \frac{2.8 \text{ m} \times 2.4 \text{ m}}{2} \\ A &= \frac{6.72 \text{ m}^2}{2} \\ A &= 3.36 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 2.8 \text{ m} \times 1.2 \text{ m} \\ &= 3.36 \text{ m}^2 \end{aligned}$$



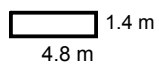
$$\begin{aligned} A &= b \times h \\ &= 2.8 \text{ m} \times 1.2 \text{ m} \\ &= 3.36 \text{ m}^2 \end{aligned}$$



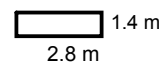
$$\begin{aligned} A &= b \times h \\ &= 2.8 \text{ m} \times 1.2 \text{ m} \\ &= 3.36 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Total SA Triangular Prism} &= 2 \text{ triangles} + \text{rectangle} + \text{rectangle} + \text{rectangle} \\ &= 2 (3.36 \text{ m}^2) + 3.36 \text{ m}^2 + 3.36 \text{ m}^2 + 3.36 \text{ m}^2 \\ &= 6.72 \text{ m}^2 + 3.36 \text{ m}^2 + 3.36 \text{ m}^2 + 3.36 \text{ m}^2 \\ &= 16.8 \text{ m}^2 \end{aligned}$$

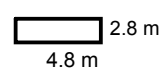
Prism



$$\begin{aligned} A &= b \times h \\ &= 4.8 \text{ m} \times 1.4 \text{ m} \\ &= 6.72 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 2.8 \text{ m} \times 1.4 \text{ m} \\ &= 3.92 \text{ m}^2 \end{aligned}$$



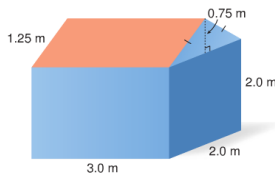
$$\begin{aligned} A &= b \times h \\ &= 4.8 \text{ m} \times 2.8 \text{ m} \\ &= 13.44 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Prism} &= 2 \text{ top} + 2 \text{ side} + 2 \text{ front} \\ &= 2 (6.72) + 2 (3.92) + 2(13.44) \\ &= 13.44 + 7.84 + 26.88 \\ &= 48.16 \end{aligned}$$

Overlap Area

$$\begin{aligned} A &= b \times h \\ &= 2.8 \text{ m} \times 1.2 \text{ m} \\ &= 3.36 \text{ m}^2 \\ &\quad \times 2 \text{ faces} \\ \hline &= 6.72 \text{ m}^2 \end{aligned}$$

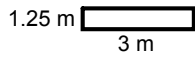
$$\begin{aligned} \text{Total SA} &= \text{Triangular Prism} + \text{Rectangular Prism} - \text{overlap} \\ &= 16.8 \text{ m}^2 + 48.12 \text{ m}^2 - 6.72 \text{ m}^2 \\ &= 64.92 \text{ m}^2 - 6.72 \text{ m}^2 \\ &= 58.2 \text{ m}^2 \end{aligned}$$



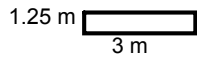
Triangular Prism

With bottom

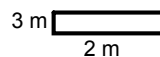
$$\begin{aligned} \text{Area of Triangle} &= \frac{b \times h}{2} \\ &= \frac{(2 \text{ m}) \times (0.75 \text{ m})}{2} \\ &= \frac{1.5 \text{ m}^2}{2} \\ &= 0.75 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 1.25 \text{ m} \times 3 \text{ m} \\ &= 3.75 \text{ m}^2 \end{aligned}$$



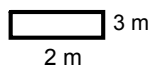
$$\begin{aligned} A &= b \times h \\ &= 1.25 \text{ m} \times 3 \text{ m} \\ &= 3.75 \text{ m}^2 \end{aligned}$$



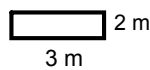
$$\begin{aligned} A &= b \times h \\ &= 2 \text{ m} \times 3 \text{ m} \\ &= 6 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Total SA} &= 2 \text{ Triangles} + \text{Rectangle} + \text{Rectangle} + \text{Rectangle} \\ \text{of triangular prism} &= 2(0.75 \text{ m}^2) + 3.75 \text{ m}^2 + 3.75 \text{ m}^2 + 6 \text{ m}^2 \\ &= 1.5 \text{ m}^2 + 3.75 \text{ m}^2 + 3.75 \text{ m}^2 + 6 \text{ m}^2 \\ &= 15 \text{ m}^2 \end{aligned}$$

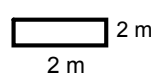
Prism



$$\begin{aligned} A &= b \times h \\ &= 3 \text{ m} \times 2 \text{ m} \\ &= 6 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 3 \text{ m} \times 2 \text{ m} \\ &= 6 \text{ m}^2 \end{aligned}$$

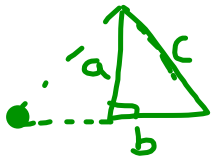


$$\begin{aligned} A &= b \times h \\ &= 2 \text{ m} \times 2 \text{ m} \\ &= 4 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Prism} &= 2 \text{ top} + 2 \text{ side} + 2 \text{ front} \\ &= 2(6) + 2(6) + 2(4) \\ &= 12 + 12 + 8 \\ &= 32 \end{aligned}$$

$$\begin{aligned} \text{Overlap} &= b \times h \\ &= 3 \text{ m} \times 2 \text{ m} \\ &= 6 \text{ m}^2 \\ &\quad \text{x 2 faces} \\ \hline &= 12 \text{ m}^2 \end{aligned}$$

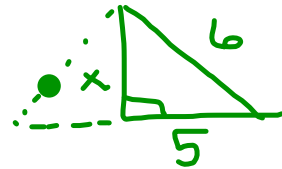
$$\begin{aligned} \text{with bottom} &= \text{Triangular Prism} + \text{Rectangular Prism} - \text{overlap} \\ &= 15 \text{ m}^2 + 32 \text{ m}^2 - 12 \text{ m}^2 \\ &= 35 \text{ m}^2 \end{aligned}$$



$$c^2 = a^2 + b^2$$

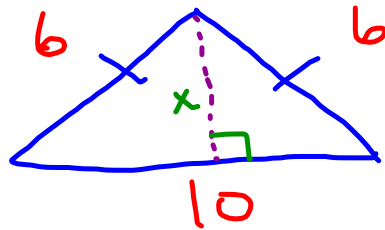
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5a, b



x

$$x^2 = c^2 - b^2$$



$$A = \frac{b \times h}{2}$$

$$= \frac{10 \times (x)}{2}$$

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Class / Homework
Review For Test ●

- Handout: Surface Area Worksheet

Questions: 1-6

answers were on the board

- Questions from Textbook:

page 45 - 46

#2(b, d, f, h)

12ac

#3(a,b,c,d,e)

#13ab

#4(a,d)

#15(bc)

#5 (a, c, e)

#16(bc)

#6 (b,d)

#19(a)

7(ad)

Page 31

#10 Warehouse question

Worksheet

Answers

$$1) 1680 \text{ cm}^2$$

$$2) 952.8 \text{ mi}^2$$

$$3) 791.3 \text{ cm}^2$$

$$4) 990 \text{ mm}^2$$

$$5) 528.9 \text{ cm}^2$$

$$6) 426.8 \text{ cm}^2$$

