

OCTOBER 19, 2017**UNIT 2: FACTORS AND PRODUCTS****SECTION 3.8:
FACTORING SPECIAL
POLYNOMIALS****K. Sears***NUMBERS, RELATIONS AND FUNCTIONS 10*

Warm Up

Factor each of the following:

$25a^2 - 9b^2$

$(5a + 3b)(5a - 3b)$

$81w^{16} - 1$

$(9w^8 + 1)(9w^8 - 1)$

$(9w^8 + 1)(3w^4 + 1)(3w^4 - 1)$

$\overbrace{100x^2 - 140xy + 49y^2}$

$(10x - 7y)^2$

$$\textcircled{1} \text{ GCF } 5x(2x^2y + 3x - 7)$$

$$\textcircled{2} \text{ Perfect Squares } 9x^2 + 12x + 4 = (3x + 2)^2$$

$$\textcircled{3} \text{ Difference of Squares } 49b^2 - 81 = (7b - 9)(7b + 9)$$

$$\textcircled{4} \text{ Decomposition (Hard Trinomials) } \begin{array}{l} 6x^2 - 17xy + 5y^2 \quad \begin{array}{l} M \ 30 \\ A \ -17 \\ N \ -15 \end{array} \\ 6x^2 - 2xy - 15xy + 5y^2 \\ 2x(3x - y) - 5y(3x - y) \\ (3x - y)(2x - 5y) \end{array}$$

$$\textcircled{5} \text{ Simple Trinomials } \begin{array}{l} f^2 + 17f + 16 \quad \begin{array}{l} M \ 16 \\ A \ 17 \\ N \ 16 \end{array} \\ (f + 1)(f + 16) \\ \hline 4a^2 + 20a + 24 \quad \begin{array}{l} M \ 6 \\ A \ 5 \\ N \ 32 \end{array} \\ 4(a^2 + 5a + 6) \\ 4(a + 3)(a + 2) \end{array}$$

WHAT'S THE POINT OF TODAY'S LESSON?

We will continue working on the NRF 10 Specific Curriculum Outcome (SCO) "Algebra and Numbers 5" OR "AN5" which states:

"Demonstrate an understanding of common factors and trinomial factoring."



What does THAT mean???

SCO AN5 means that we will:

- * determine the common factors in the terms of a polynomial and express the polynomial in factored form
- * factor a polynomial that is a "difference of squares" and explain why it is a special case of trinomial factoring where $b = 0$
- * identify and explain errors in a polynomial factorization
- * factor a polynomial and verify by multiplying the factors
- * explain, using examples, the relationship between multiplication and factoring of polynomials
- * generalize and explain strategies used to factor a trinomial
- * express a polynomial as a product of its factors



Quiz

- Multiplying polynomials
- Factoring - GCF
 - simple trinomials

UNIT 2 – FACTORS AND PRODUCTS

Quiz – Sections 3.7, 3.3 & 3.5

K. Sears

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NAME: _____

DATE: _____

1. Expand and simplify where necessary. (5)

a) $3x(2x - 5)$

$6x^2 - 15x$

b) $(y + 4)(y - 10)$

$y^2 - 10y + 4y - 40$
 $y^2 - 6y - 40$

c) $(d - 6)^2$

$(d - 6)(d - 6)$
 $d^2 - 6d - 6d + 36$
 $d^2 - 12d + 36$

2. Factor. (10)

a) $8a^2 + 16a$

$8a(a + 2)$

b) $-5m^2n^2 + 10m^2n - 35mn$

$-5mn(m^2n - 2m + 7)$

c) $v^2 + 4v - 12$

$m = -12$
 $A = 4$
 $(v + 6)(v - 2)$

d) $4f^2 - 20f - 56$

$4(f^2 - 5f - 14)$
 $4(f - 7)(f + 2)$
 $m = -14$
 $A = -5$
 $N = -7 + 2$

Review - Factoring.pdf

Factoring Review

Name _____

Math 10 (Numbers, Functions and Relations 10)

Factor the common factor out of each expression.

1) $20r^5 + 4r^2 - 40$

2) $-5x^3 - 5x^2 - 5x$

3) $12n^5 - 48n^2 + 42n$

4) $-56a^7 + 48a^6 + 16a^3$

Factor each completely.

5) $x^2 + x - 56$

6) $6n^2 - 6n - 120$

7) $4k^2 - 24k - 28$

8) $x^2 - 3x - 18$

9) $b^2 - 7b - 8$

10) $a^2 + 13a + 30$

11) $30n^2 - 24n - 72$

12) $5x^2 - 21x - 54$

13) $16n^2 - 164n + 288$

14) $54x^2 - 90x$

15) $4x^2 + 6x$

16) $6n^2 - 5n + 1$

17) $4r^2 + 7r - 2$

18) $4n^2 - 4n - 35$

19) $6v^2 - 14v$

Answers to Math 10 (Numbers, Functions and Relations 10)

- | | | | |
|-------------------------|------------------------|------------------------|-----------------------------|
| 1) $4(5r^5 + r^2 - 10)$ | 2) $-5x(x^2 + x + 1)$ | 3) $6n(2n^4 - 8n + 7)$ | 4) $8a^3(-7a^4 + 6a^3 + 2)$ |
| 5) $(x + 8)(x - 7)$ | 6) $6(n - 5)(n + 4)$ | 7) $4(k + 1)(k - 7)$ | 8) $(x - 6)(x + 3)$ |
| 9) $(b - 8)(b + 1)$ | 10) $(a + 3)(a + 10)$ | 11) $6(5n + 6)(n - 2)$ | 12) $(5x + 9)(x - 6)$ |
| 13) $4(n - 8)(4n - 9)$ | 14) $18x(3x - 5)$ | 15) $2x(2x + 3)$ | 16) $(3n - 1)(2n - 1)$ |
| 17) $(r + 2)(4r - 1)$ | 18) $(2n + 5)(2n - 7)$ | 19) $2v(3v - 7)$ | |

Homework

Worksheet: Factoring Review #1 - 40



Bonus
Completely factor the following:

$$9(x^2 - 1)^4 + 8(x^2 - 1)^3$$

* Bonus Questions are due BEFORE homeroom begins!!!

2.11 Exercise Factoring Review

B You must be able to recognize which skills must be used to factor a polynomial. When you factor the following polynomials, always check for a common factor first. There are at least two expressions that cannot be factored. Can you find others?

- | | | |
|--------------------------------|----------------------------------|-------------------------|
| 1. $3a^2 + 6a$ | 2. $2x - 8xy$ | 3. $36a^3 - 4a^2$ |
| 4. $25a^4 - 9y^4$ | 5. $x^2 + 7x + 12$ | 6. $3a^2 - 3b^2$ |
| 7. $y^3 - 11y + 28$ | 8. $16x^2 - 8x + 1$ | 9. $a^2 - ab - 56b^2$ |
| 10. $4x^2 - 11x + 6$ | 11. $-1 + 9k^2$ | 12. $1 + 18y + 32y^2$ |
| 13. $2y^2 - 8y^3$ | 14. $x^2 + 6x + 8$ | 15. $56x^2 + 9x - 2$ |
| 16. $-16 - 9x^2$ | 17. $16 - 28x + 10x^2$ | 18. $m^4 - 16$ |
| 19. $8 - 14y + 5y^2$ | 20. $-(1 - a^4)$ | 21. $m^4 - 5m^2 - 36$ |
| 22. $6a^2 + 5a + 1$ | 23. $x^4 - y^4$ | 24. $p^2 - 2pq - 63q^2$ |
| 25. $m^4 + 3m^2 - 4$ | 26. $x^2 - xy$ | 27. $x^2 + 3xy - x$ |
| 28. $a^2 - 14a$ | 29. $3a^2 - 36a + 36$ | 30. $(a + b)^2 - c^2$ |
| 31. $-a^2 - 2ab - b^2$ | 32. $x^3 + 5x^2 - 6$ | 33. $x^4 + 18x^2 + 32$ |
| 34. $m^4 - 9m^2 - 112$ | 35. $x^8 - 1$ | 36. $2y^2 - 2y - 24$ |
| 37. $2x^2 - 8$ | 38. $4y^2 + 8y - 60$ | 39. $m^4 - 16$ |
| 40. $2x^2 - 16x + 32$ | 41. $x^3 - xy^2$ | 42. $x^4 - 5x^2 + 4$ |
| 43. $-48 - 3y^2$ | 44. $x^2y^2 - 2xy^2$ | |
| 45. $(x - y)^2 - (x + y)^2$ | 46. $9(a + b)^2 - (a - b)^2$ | |
| 47. $(a - b)^2 - 16(a + 2b)^2$ | 48. $25(2x + 1)^2 - (9x - 1)^2$ | |
| 49. $4(x - y)^2 - 16(x + y)^2$ | 50. $25(x + 2y)^2 - 9(x - 2y)^2$ | |

SOLUTIONS

200. $8(2x^2 + 7x + 3)$
 48. $(5x + 9)(x + 9) - 4(3x + 2)(x + 3)$
 49. $(2x + 2)(x + 2) - 4(2x + 2)(x + 2)$
 42. $(x - 1)(x + 1) - 4(x - 1)(x + 1)$
 41. $(x - 1)(x + 1) - 4(x - 1)(x + 1)$
 39. $(m + 4)(m + 4) - 4(m + 4)(m + 4)$
 38. $(x - 2)(x + 2) - 4(x - 2)(x + 2)$
 34. $(m + 4)(m + 4) - 4(m + 4)(m + 4)$
 31. $(a + b)^2 - 4(a + b)^2$
 29. $(x + 2)(x + 2) - 4(x + 2)(x + 2)$
 24. $(x + 2)(x + 2) - 4(x + 2)(x + 2)$
 22. $(x + 2)(x + 2) - 4(x + 2)(x + 2)$
 18. $(m + 4)(m + 4) - 4(m + 4)(m + 4)$
 16. $(x + 2)(x + 2) - 4(x + 2)(x + 2)$
 11. $(x + 2)(x + 2) - 4(x + 2)(x + 2)$
 9. $(a - 8)(a + 2) - 4(a - 8)(a + 2)$
 6. $(x + 2)(x + 2) - 4(x + 2)(x + 2)$
 1. $5a(a + 2) - 4(a + 2)(a + 2)$

Attachments

Review - Factoring.pdf

Worksheet - Factoring Review.doc