Warm Up

Describe the 3 C's for Ambiguous Case...

Calculation:
$$h = 65$$
in A

Calculation:
$$h = b \sin A$$

Cases: $Oach$

No Solution

1 Right D

2 Priving

Acute (Calc)

** 2) Obtuse (180-0)

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MUST
MEMORIZE
THESE
NOTES
IN ORDER
TO KNOW
AMBIGUOUS
CASE

Criteria for the Ambiguous Case...

- Must be given SSA
- · Given angle is acute
- a < b

*** If ALL 3 criteria are met, then...



CALCULATE THE ALTITUDE

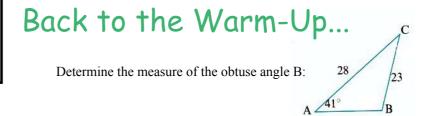
alt = b sin A

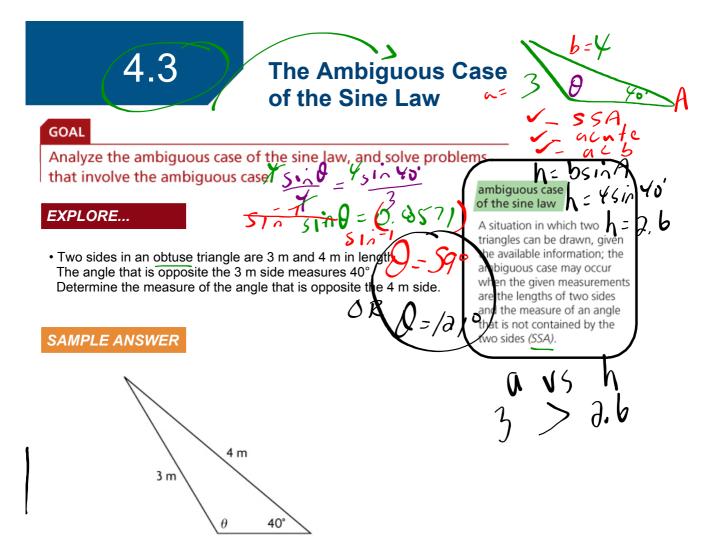
CASE 1: a < altitude; there is NO SOLUTION

CASE 2: a = altitude; there is <u>ONE SOLUTION</u> [Right Triangle]

CASE 3: a >altitude; this is the 'AMBIGUOUS CASE'...TWO SOLUTIONS

- 1) Acute Triangle (angle, θ , is found with Law of Sines)
- 2) Obtuse Triangle (angle is $180^{\circ} \theta$)





$$\theta = 180 - 58.9869...^{\circ}$$

 $\theta = 121.0130...^{\circ}$

 $\theta = 58.9869...^{\circ}$

 $\frac{\sin\theta}{4} = \frac{\sin 40^{\circ}}{3}$

 $\sin \theta = 0.8570...$

The angle measure is about 121°.

Notes - Ambiguous Case.pdf

In Summary

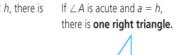
Key Idea

• The ambiguous case of the sine law may occur when you are given two side lengths and the measure of an angle that is opposite one of these sides. Depending on the measure of the given angle and the lengths of the given sides, you may need to construct and solve zero, one, or two triangles.

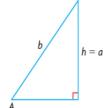
Need to Know

• In $\triangle ABC$ below, where h is the height of the triangle, $\angle A$ and the lengths of sides a and b are given, and $\angle A$ is acute, there are four possibilities to consider:

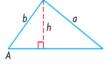
If $\angle A$ is acute and a < h, there is no triangle.

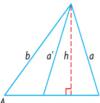






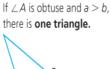
If $\angle A$ is acute and a > b or a = b, there is **one triangle.** If $\angle A$ is acute and h < a < b, there are two possible triangles.

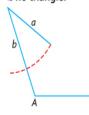




• If $\angle A$, a, and b are given and $\angle A$ is obtuse, there are two possibilities to consider:

If $\angle A$ is obtuse and a < b or a = b, there is no triangle.



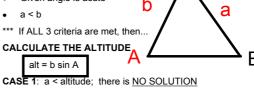




Criteria for the Ambiguous Case...

- Must be given SSA
- Given angle is acute
 - a < b

*** If ALL 3 criteria are met, then...



CASE 2: a = altitude; there is <u>ONE SOLUTION</u> [Right Triangle]

CASE 3: a >altitude; this is the 'AMBIGUOUS CASE'...TWO SOLUTIONS

- 1) Acute Triangle (angle, θ , is found with Law of Sines)
- 2) Obtuse Triangle (angle is 180° θ)

EXAMPLE 1

Connecting the SSA situation to the number of possible triangles

acute angle

Given each SSA situation for $\triangle ABC$, determine how many triangles are possible.

$$\triangle A = 30^{\circ}, a = 4 \text{ m}, \text{ and } b = 12 \text{ m}$$

 $\triangle A = 30^{\circ}$, a = 8 m, and b = 12 m

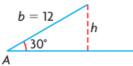
(b) $\angle A = 30^{\circ}$, a = 6 m, and b = 12 m

d) $\angle A = 30^{\circ}$, a = 15 m, and b = 12 m

triangle

1 (ight D

Saskia's Solution



I drew the beginning of a triangle with a 30° angle and a 12 m side.

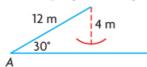
sin 30° =

I used the sine ratio to calculate the height of the triangle.

 $12 \sin 30^\circ = h$ 6 m = h

I can use this height as a benchmark to decide on side lengths opposite the 30° angle that will result in zero, one, or two triangles.

a) $\angle A = 30^{\circ}$, a = 4 m, and b = 12 m



Since a < b and a < h, I knew that no triangles are possible.

I used a compass to be certain. I set the compass tips to represent 4 m. I placed one tip of the compass at the open end of the 12 m side and swung the pencil tip toward the other side. The pencil couldn't reach the base, so a 4 m side could not close the triangle.

No triangles are possible.

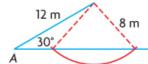
b) $\angle A = 30^{\circ}$, a = 6 m, and b = 12 m

Since a < b and a = h, there is only one possible triangle, a right triangle.

A compass arc intersects the base at only one point.

One triangle is possible.

c) $\angle A = 30^{\circ}$, a = 8 m, and b = 12 m

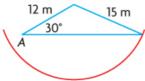


Since a < b and a > h, there are two possible triangles.

A compass arc intersects the base at two points.

Two triangles are possible.

d) $\angle A = 30^{\circ}$, a = 15 m, and b = 12 m



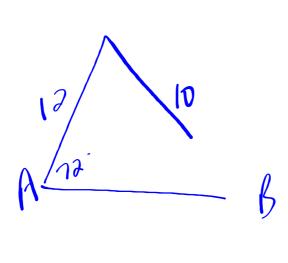
Since a > b, only one triangle is possible.

A compass arc intersects the base at only one point.

One triangle is possible.

Example 2:

Solve the triangle ABC if a = 10, b = 12 and angle $A = 72^{\circ}$.



A SSA

- given ungle

a c b

h = /2 sin 72

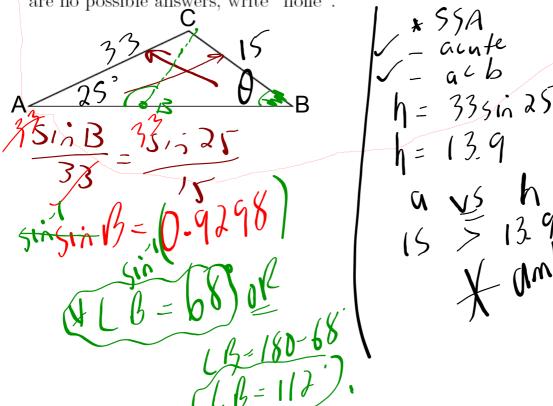
h = 11.4

A VS

No Solution

Example 3:

Given that $A = 25^{\circ}$, a = 15, and b = 33, find the measure of angle B to the nearest degree. If there are two answers, give both of them. If there are no possible answers, write "none".



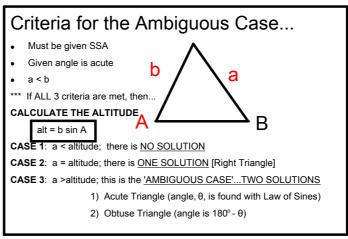
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HOMEWORK...

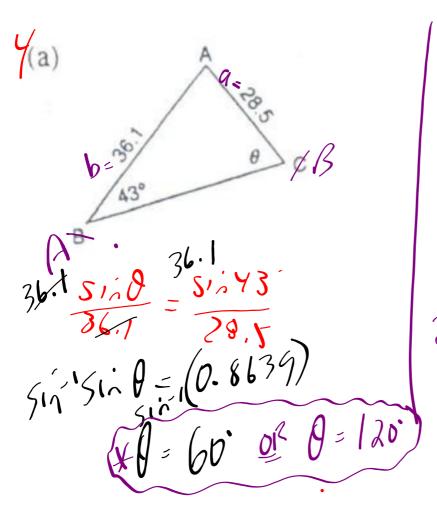
Worksheet - Ambiguous Case.pdf

Do questions #1, 2 & 4

MEMORIZE!!! -> DUIZ



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