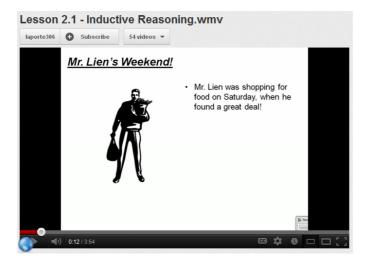
REVIEW...



Homework Questions P.12 #11,16 113 11. Paula claims that whenever you square an odd integer, the result is an odd number. Is her conjecture reasonable? Justify your decision.

$$3^{2} = 9$$

$$(-11)^{2} = 121$$

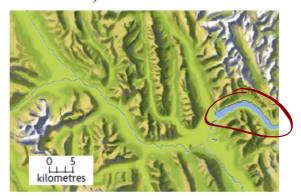
$$(101)^{2} = 10701$$

13. Text messages often include cryptic abbreviations, such as L2G (love to go), 2MI (too much information), LOL (laugh out loud), and MTF (more to follow). Make a conjecture about the cryptic abbreviations used in text messages, and provide evidence to support your conjecture.

Conjecture > Use the 1st letter
in each word

TTYL

16. The map below does not have any roads or urban areas marked. However, there is a town of 7000 people somewhere in this area. Make a conjecture about where the town is. Justify your decision.



Conjecture -> Towns were built wourd water ways

1.3

Using Reasoning to Find a Counterexample to a Conjecture

GOAL

Invalidate a conjecture by finding a contradiction.

To restate what you have read so far, a conjecture is a mathematical statement that has been proposed as a true statement, but not yet proven or disproved.

Once a conjecture is proven, it is a mathematical fact.

One method to test a conjecture is to attempt to **disprove** it by using a **counterexample**.

For example:

Conjecture: All prime numbers are odd. Counterexample: But 2 is a prime number.

The counterexample disproves the conjecture, hence we can conclude that not all prime numbers are odd.

EXAMPLE #2:

Conjecture:



For all real numbers x, the expressions x^2 is greater than or equal to x

Conjecture: For all real numbers x, the expressions x^2 is greater than or equal to x

Here is a counterexample:

 $(0.5)^2 = 0.25$, and 0.25 is **not** greater than or equal to 0.5

In fact, any number between 0 and 1 is a counterexample. The conjecture is false.



PAGE 21

Using reasoning to find a counterexample to a conjecture

Matt found an interesting numeric pattern:

$$1 \cdot 8 + 1 = 9$$

$$12 \cdot 8 + 2 = 98$$

$$123 \cdot 8 + 3 = 987$$

$$1234 \cdot 8 + 4 = 9876$$

Matt thinks that this pattern will continue.

Search for a counterexample to Matt's conjecture.

Kublu's Solution

$$1 \cdot 8 + 1 = 9$$

$$12 \cdot 8 + 2 = 98$$

$$123 \cdot 8 + 3 = 987$$

$$1234 \cdot 8 + 4 = 9876$$

The pattern seemed to be related to the first factor (the factor that wasn't 8), the number that was added, and the product.

	Α	В
1	$1 \cdot 8 + 1$	9
2	12 • 8 + 2	98
3	123 • 8 + 3	987
4	1234 • 8 + 4	9876
5	12345 • 8 + 5	98765
6	123456 · 8 + 6	987654
7	1234567 · 8 + 7	9876543
8	12345678 • 8 + 8	98765432
9	123456789 • 8 + 9	987654321

I used a spreadsheet to see if the pattern continued. The spreadsheet showed that it did.

When I came to the tenth step in the sequence,

each way that 10 and 0 could be represented.

I had to decide whether to use 10 or 0 in the first

factor and as the number to add. I decided to check

 $12345678910 \cdot 8 + 10 = 98765431290$

 $123456789\mathbf{0} \cdot 8 + \mathbf{10} = 9876543130$

 $12345678910 \cdot 8 + 0 = 98765431280$

 $123456789\mathbf{0} \cdot 8 + \mathbf{0} = 9876543120$

The pattern holds true until 9 of the 10 digits are included. At the tenth step in the sequence, a counterexample is found.

Since the pattern did not continue, Matt's conjecture is invalid.

Revised conjecture: When the value of the addend is 1 to 9, the pattern will continue.

I decided to revise Matt's conjecture by limiting it.

Your Turn

If Kublu had not found a counterexample at the tenth step, should she have continued looking? When would it be reasonable to stop gathering evidence if all the examples supported the conjecture? Justify your decision.



-					
A	n	S	И	/e	r

Mathematical HISTORY???

Goldbach's Conjecture

One famous example of an unproven conjecture has remained undecided for nearly 300 years.

In the early 1700's, Christian Goldbach, a Prussian mathematician, noticed that many even numbers greater than 2 can be written as the sum of two primes. Expanding on examples like these, Goldbach wrote the following conjecture:

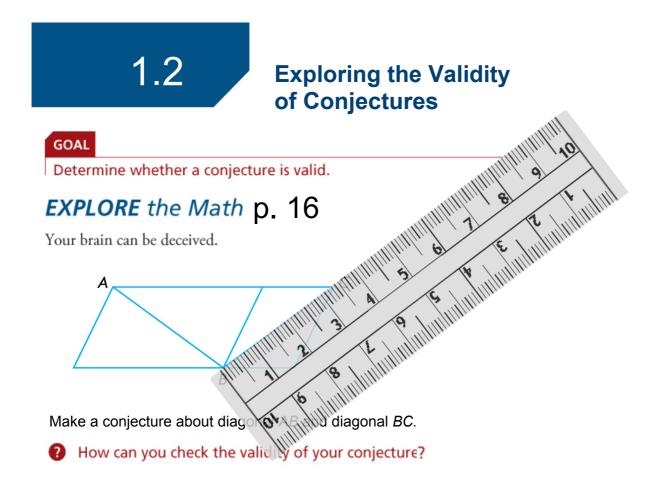
4 = 2 + 2	10 = 3 + 7	16 = 3 + 13
6 = 3 + 3	12 = 5 + 7	18 = 5 + 13
8 = 3 + 5	14 = 3 + 11	20 = 3 + 17

Conjecture: Every even number greater than 2 can be written as the sum of two primes.

To this day, no one has proven **Goldbach's Conjecture** or found a counterexample to show that it is false. It is still unknown whether this conjecture is true or false. It is known, however, that all even numbers up to 4×10^{18} confirm Goldbach's Conjecture.

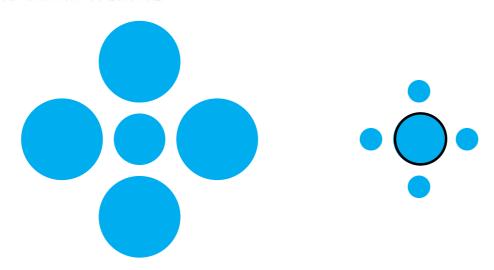


Christian Goldbach (1690 – 1764) was a German mathematician famous for his eponymous Conjecture. Goldbach's Conjecture is one of the most infamous problems in mathematics, and states that every even integer number greater than 2 can be expressed as the sum of two prime numbers. For example, 4=2+2, 6=3+3, and 8=3+5. While there have not been any counter-examples found up through $4\times10^{18} (as of 2012)$, the conjecture has not yet been formally proven.



EXPLORE the Math

Your brain can be deceived.

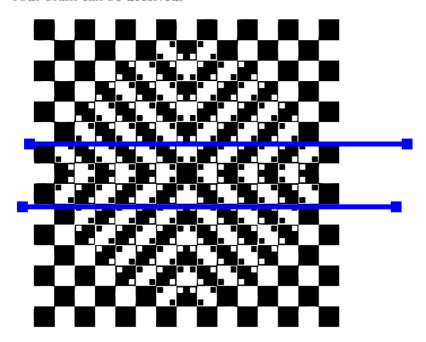


Make a conjecture about the circles in the centre.

? How can you check the validity of your conjecture?

EXPLORE the Math

Your brain can be deceived.

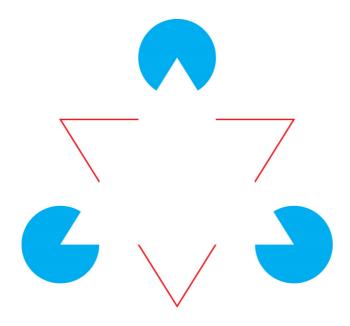


Make a conjecture about the lines.

? How can you check the validity of your conjecture?

EXPLORE the Math

Your brain can be deceived.



Make a conjecture about the number of triangles.

? How can you check the validity of your conjecture?

Reflecting

- Describe the steps you took to verify your conjectures.
- B. After collecting evidence, did you decide to revise either of your conjectures? Explain.
- **C.** Can you be certain that the evidence you collect leads to a correct conjecture? Explain.

Answers

- A. Both measurement and visual inspection helped to verify or discredit the conjectures.
- **B.** My conjectures changed as follows after collecting more evidence:
 - · First image: Both diagonals are the same length.
 - · Second image: The centre circles of the figures are the same size.
 - Third image: The rows and columns of white and black shapes are placed in straight lines.
 - · Fourth image: There are no triangles in the figure.
- **C.** For these images, the revised conjectures hold true for the accuracy of the tools I used. I cannot be absolutely sure that my new conjectures are valid until the precision of the tools is considered.

Some other optical illusions... Nalli han a e nbed nb. ca

M. C. Escher...

http://www.mcescher.com/



Three Dragons



three_dragons.wmv

3D Chalk Art.. Julian Beever



"Julian Beever is an English, Belgium-based chalk artist who has been creating trompe-l'œil chalk drawings on pavement surfaces since the mid-1990s. His works are created using a projection called anamorphosis, and create the illusion of three dimensions when viewed from the correct angle."

44 Amazing Julian Beever's 3D Pavement armings

1.2 - Validity of Conjectures? In Summary page 17

1.3 - Counterexamples

In Summary page 22

Key Idea

• Some conjectures initially seem to be valid, but are shown not to be valid after more evidence is gathered.

Need to Know

- The best we can say about a conjecture reached through inductive reasoning is that there is evidence either to support or deny it.
- · A conjecture may be revised, based on new evidence.

Key Ideas

- Once you have found a counterexample to a conjecture, you have disproved the conjecture. This means that the conjecture is invalid.
- . You may be able to use a counterexample to help you revise a conjecture.

Need to Know

- A single counterexample is enough to disprove a conjecture.
- Even if you cannot find a counterexample, you cannot be certain that there is not one. Any supporting evidence you develop while searching for a counterexample, however, does increase the likelihood that the conjecture is true.

HOMEWORK...

p. 17: #1 & 2

p. 22: #1, 3, 5, 8, 12, 17

1s3e3 final.mp4 three_dragons.wmv