

April 27, 2018

**UNIT 8: CIRCLE GEOMETRY**

**8.2: PROPERTIES OF  
CHORDS IN A  
CIRCLE**

**K. Sears**  
***MATH 9***



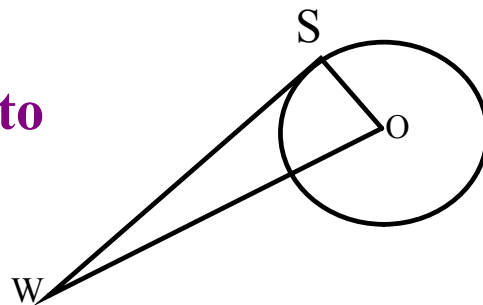
**WHAT'S THE POINT OF TODAY'S LESSON?**

**We will continue working on the Math 9 Specific Curriculum Outcome (SCO) "Shape and Space 1" OR "SS1" which states:**

**"Solve problems and justify the solution strategy using circle properties, including:**

- \* the perpendicular from the centre of a circle to a chord bisects the chord;**
- \* the measure of the central angle is equal to twice the measure of the inscribed angle subtended by the same arc;**
- \* the inscribed angles subtended by the same arc are congruent;**
- \* a tangent to a circle is perpendicular to the radius at the point of tangency."**

**WARM UP QUIZ:**  
(sketch and use the diagram to the right)



**COPY AND ANSWER:**

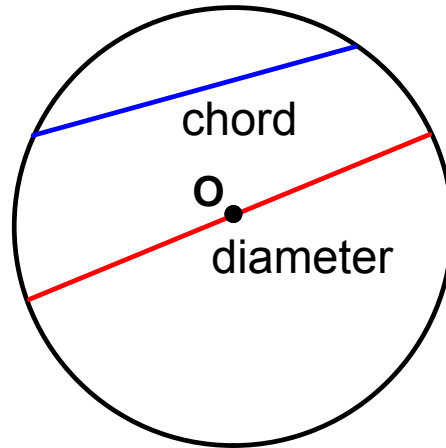
1. The tangent is line \_\_\_\_\_.
2. The centre of the circle is labeled \_\_\_\_\_.
3. The point of tangency is labeled \_\_\_\_\_.
4. The radius is line \_\_\_\_\_.
5. If **OW** is 17 cm and **SW** is 9 cm, what is the length of the radius to the nearest tenth?

### **HOMEWORK QUESTIONS?**

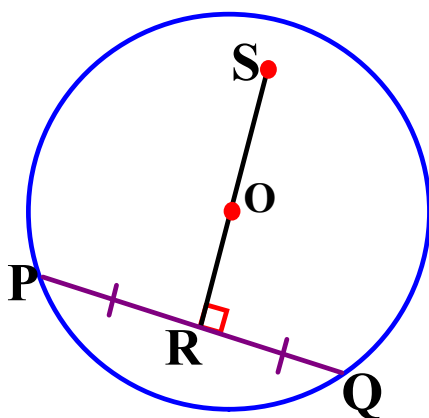
**(Pages 388/89/90/91, #3, 5, 6, 7, 9, 11, 12, 13, 14, 17, 18, 19, 20 & 22)**

**VOCABULARY:**

1. **CHORD:** A line segment that joins two points on a circle. (A diameter of a circle is actually a special chord through the centre of the circle.)

**VOCABULARY:**

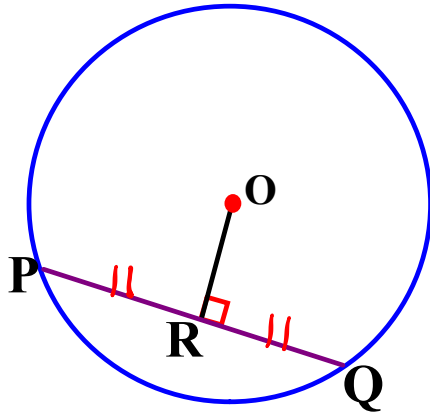
2. **PERPENDICULAR BISECTOR:** Intersects a line segment at  $90^\circ$  and divides the line segment into two equal parts.



**PQ = chord (line segment)**  
**SR = perpendicular bisector of PQ;**  
**therefore, PR = QR.**

**VOCABULARY:**

- 3. PERPENDICULAR TO CHORD PROPERTY 1 (PCP):** The perpendicular from the centre of a circle to a chord bisects the chord.



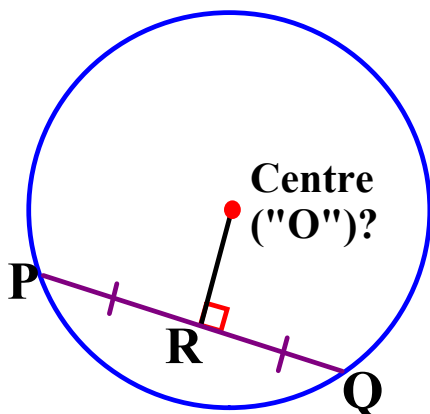
$O = \text{centre of the circle (given)}$

$\angle R = \angle R = 90^\circ \text{ (given)}$

$\therefore PR = QR \text{ (PCP)}$

**VOCABULARY:**

- 4. PERPENDICULAR TO CHORD PROPERTY 2 (PCP):** The perpendicular bisector of a chord in a circle passes through the centre of the circle.



$PR = QR \text{ (given)}$

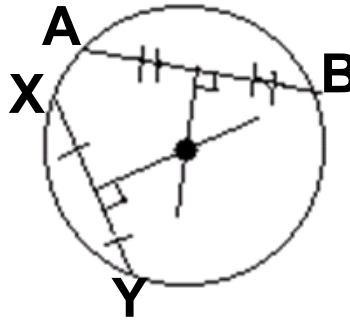
$\angle PRO = \angle QRO = 90^\circ \text{ (given)}$

$\therefore O = \text{centre of the circle (PCP)}$

## PCP 2 - Taking it Further

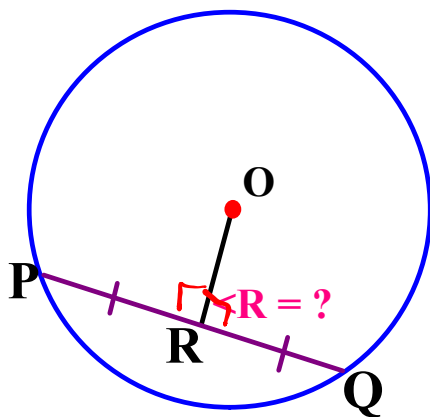
(You do not have to copy this - it is not used in grade 9 math; however, you may have to know this if you take more math courses after high school.)

To actually determine the location of the centre of a circle using PCP 2, two chords are drawn as well as their perpendicular bisectors. The point at which the two perpendicular bisectors intersect is the centre of the circle.



### VOCABULARY:

- 5. PERPENDICULAR TO CHORD PROPERTY 3 (PCP):** A line that joins the centre of a circle to the midpoint of a chord is perpendicular to the chord.



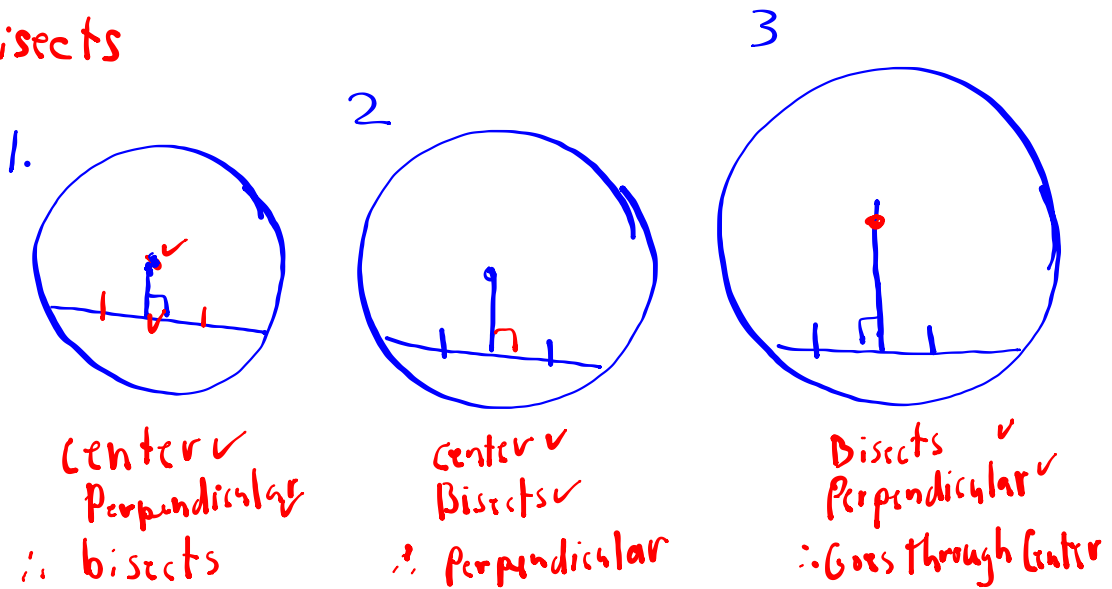
$$PR = QR \text{ (given)}$$

$O = \text{centre of the circle (given)}$

$$\therefore \angle PRO = \angle QRO = 90^\circ \text{ (PCP)}$$

- ① center
- ② meets  $90^\circ$
- ③ bisects

If you have 2 then you automatically have the third



Aren't they all saying the same thing?



**STOP!**



**YES!!!**

There are 3 pieces to the **Perpendicular to Chord Property** puzzle:

The perpendicular bisector of a chord in a circle passes through the centre of the circle, intersects with the chord at a  $90^\circ$  angle and cuts the chord into two equal pieces.

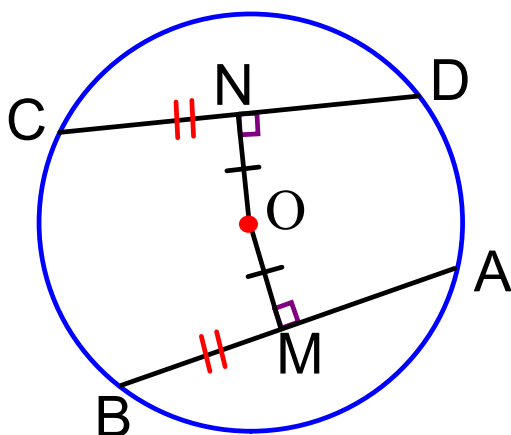
As long as you have 2 of the pieces of the puzzle, you automatically know the third.

**VOCABULARY:**

**PERPENDICULAR TO CHORD PROPERTY 4 (PCP):**

(Again, you do not have to copy this - it is not used in grade 9 math; however, you may have to know this if you take more math courses after high school.)

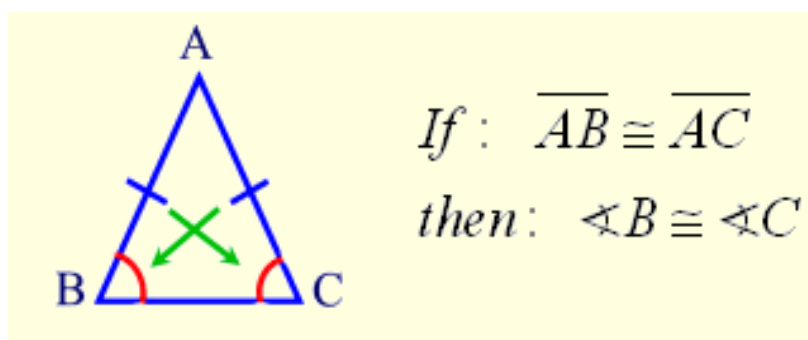
Two chords that are an equal distance from the centre of a circle are congruent.



If  $OM = ON$ ,  
then  $AB = CD$   
OR  
If  $AB = CD$ ,  
then  $OM = ON$

**VOCABULARY:**

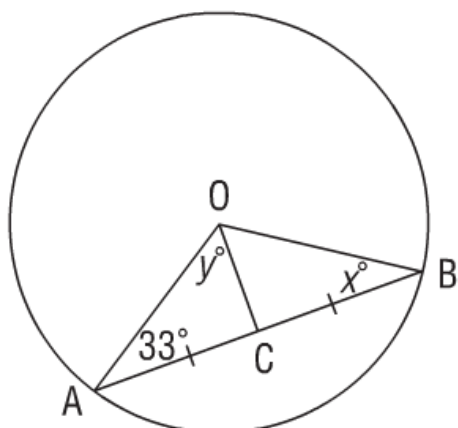
**6. ISOSCELES TRIANGLE THEOREM (ITT):** The two angles that are opposite to the two congruent sides in an isosceles triangle are also congruent.



If :  $\overline{AB} \cong \overline{AC}$   
then:  $\sphericalangle B \cong \sphericalangle C$

## Determining the Measure of Angles in a Triangle

**Example:** Determine the values of  $x^\circ$  and  $y^\circ$  in the diagram below.



$$\angle x = 33^\circ \text{ (ITT)}$$

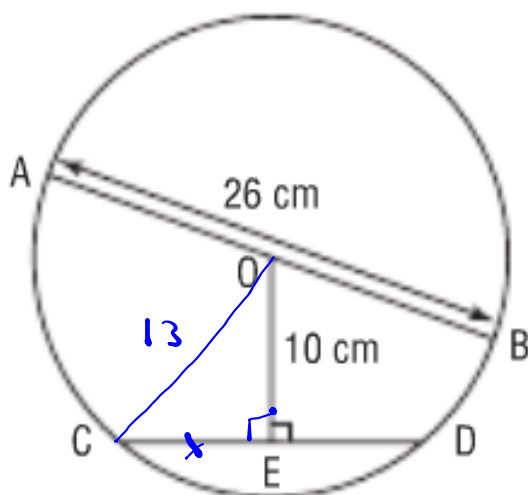
$$\angle A = 33^\circ \text{ (given)}$$

$$\angle ACO = 90^\circ \text{ (PCP)}$$

$$\angle y = 57^\circ \text{ (SATT)}$$

## Using the Pythagorean Theorem in a Circle

**Example:** What is the length of chord CD to the nearest tenth?



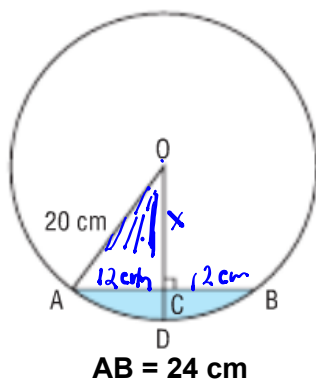
$$\begin{aligned} a^2 &= c^2 - b^2 \\ &= 13^2 - 10^2 \\ &= 169 - 100 \\ &= 69 \\ a &= \sqrt{69} \\ &= 8.3 \\ CD &= 2(8.3) \\ &= 16.6 \text{ cm} \end{aligned}$$

**ANSWER:** 16.6 cm



## Solving Problems Using the Property of a Chord and its Perpendicular

**Example:** Determine the length of CD in the diagram below.



$$OD = 20 \text{ (radius) given}$$

$$OC = x$$

$$a^2 = c^2 - b^2$$

$$x^2 = 20^2 - 12^2$$

$$= 400 - 144$$

$$= 256$$

$$x = 16$$

$$CD = 20 - 16 = 4 \text{ cm} \quad \text{ANSWER: 4 cm}$$

## CONCEPT REINFORCEMENT:

**MMS9:**

**PAGE 397: #3 TO #6**

**PAGE 398: #7 TO #12 [10(a) = 3.5]**

**PAGE 399: #13, 14, 15, 17, 18 & 19**

**PAGE 403: #4 TO #7**

**PAGE 419: #5 TO #8**