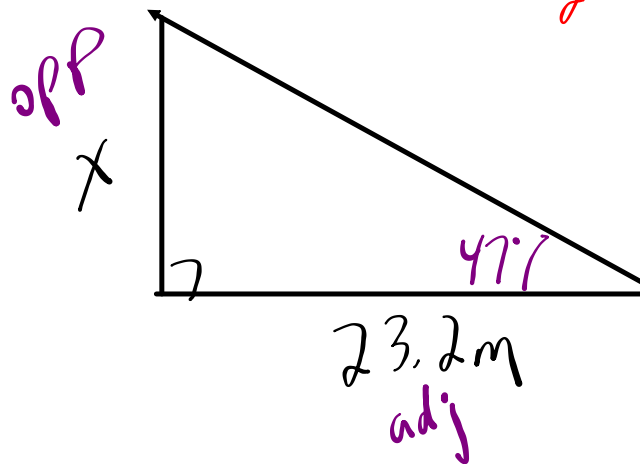


HOMWORK Questions???

15. A tree casts a shadow 23.2 m long when the angle of elevation of the sun is 47° . Find the height of the tree. (A)



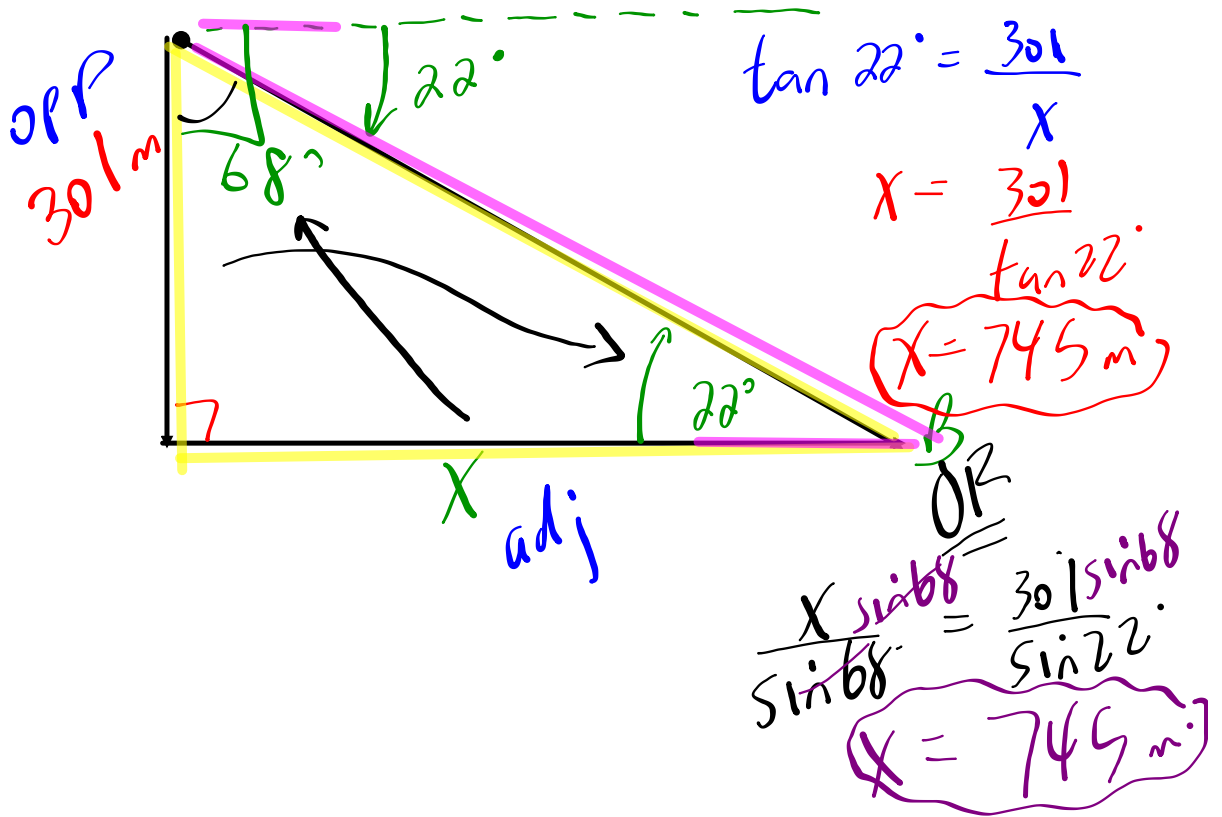
Solve LAH TOA

$$23.2 \tan 47^\circ = x$$

$$24.9 = x$$

$$x = 25$$

11. From the top of a cliff 301 m high, the angle of depression of a sailboat on the water is 22° . How far is the boat from the cliff?

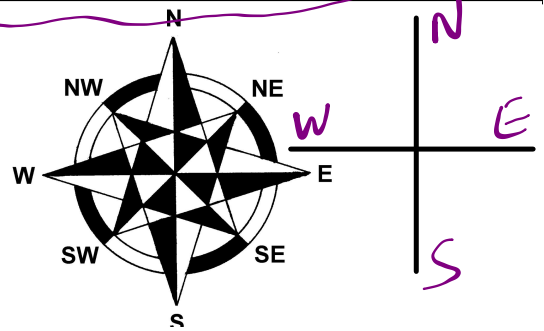
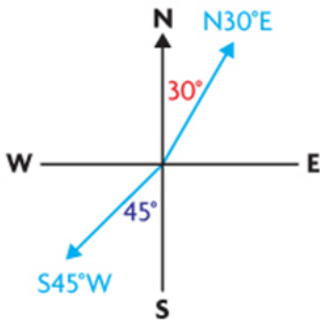


MORE APPLICATIONS... Bearings

NOTE:

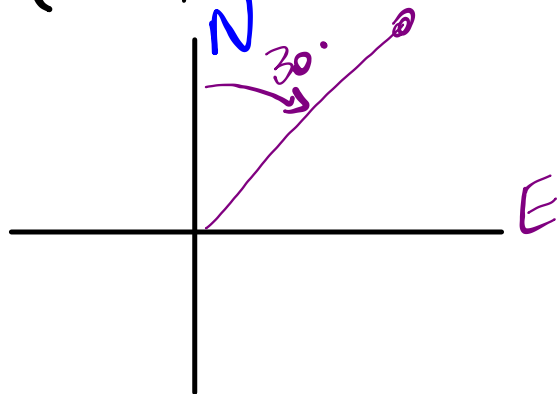
Communication | Tip

Directions are often stated in terms of north and south on a compass. For example, $N30^\circ E$ means travelling in a direction 30° east of north. $S45^\circ W$ means travelling in a direction 45° west of south.

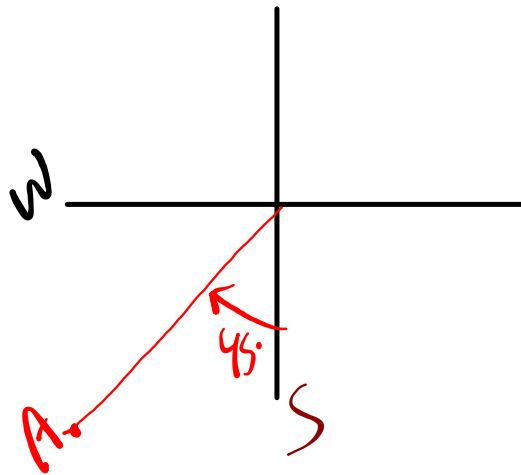


• Example → Draw a bearing

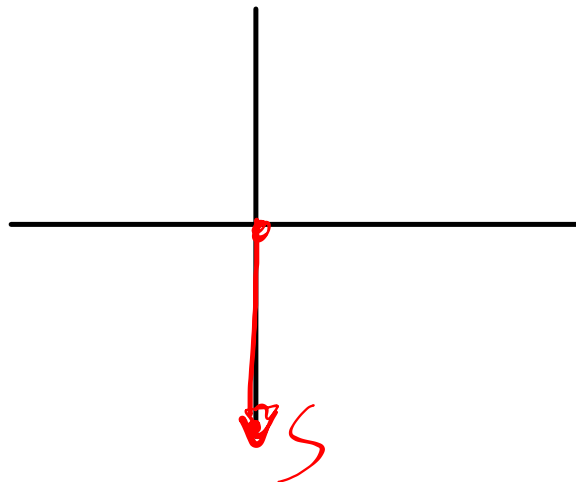
1) N30°E (say 30° East of North)



2) S45°W (say 45° West of South)



3) Due South



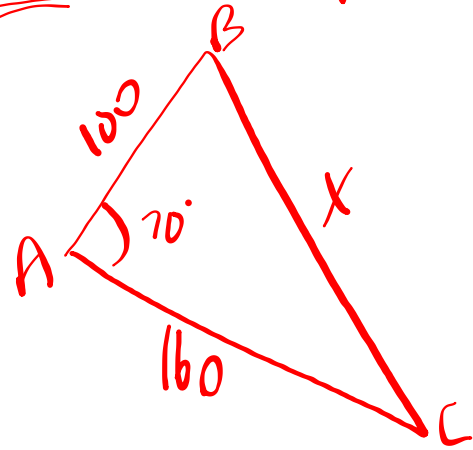
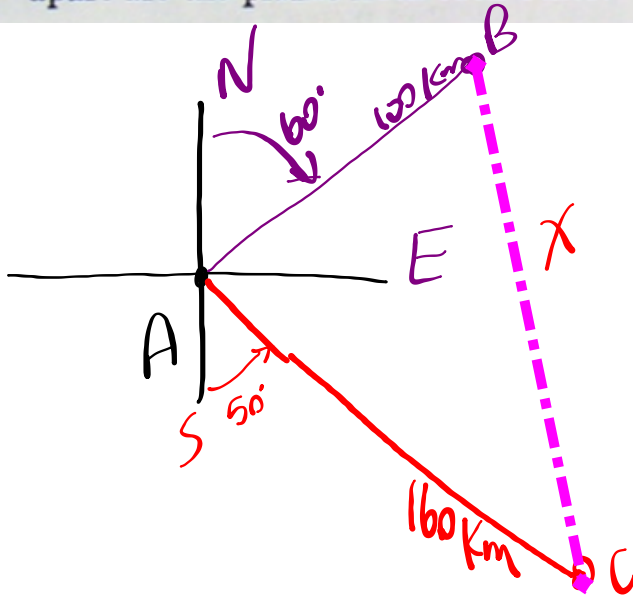
Booklet Questions... 10.12: #8 - 12

HW: #9-12

Let's do #8 TOGETHER...

8 In an airport control tower A, 2 planes at B and C are located at the same altitude on a radar screen. The range finder determines one plane to bear N60°E at 100 km while the other bears S50°E at 160 km. How far apart are the planes from each other?

**KEY → Draw 2 pictures*



$$x^2 = 100^2 + 160^2 - 2(100)(160)\cos 70^\circ$$

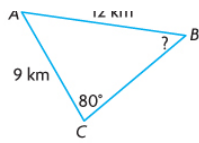
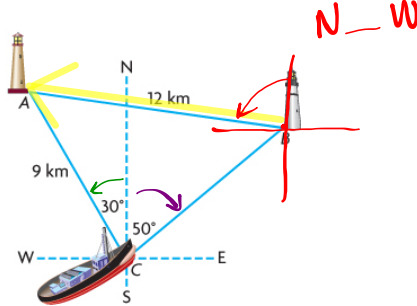
$$x = \sqrt{24655.4}$$

$$x = 157 \text{ km}$$

Applications: Bearings

Ex #1:(p. 122) Using reasoning to determine the measure of an angle

The captain of a small boat is delivering supplies to two lighthouses, as shown. His compass indicates that the lighthouse to his left is located at $N30^\circ W$ and the lighthouse to his right is located at $N50^\circ E$. Determine the compass direction he must follow when he leaves lighthouse B for lighthouse A .



I drew a diagram. I labelled the sides of the triangle I knew and the angle I wanted to determine.

$$\frac{\sin B}{AC} = \frac{\sin C}{AB}$$

I knew AC , AB , and $\angle C$, and I wanted to determine $\angle B$. So I used the sine law that includes these four quantities.

I used the proportion with $\sin B$ and $\sin C$ in the numerators so the unknown would be in the numerator.

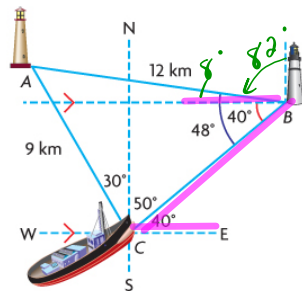
$$\begin{aligned} \frac{\sin B}{9} &= \frac{\sin 80^\circ}{12} \\ 9\left(\frac{\sin B}{9}\right) &= 9\left(\frac{\sin 80^\circ}{12}\right) \\ \sin B &= 9\left(\frac{\sin 80^\circ}{12}\right) \\ \sin B &= 0.7386... \end{aligned}$$

I substituted the given information and then solved for $\sin B$.

$$\begin{aligned} \angle B &= \sin^{-1}(0.7386...) \\ \angle B &= 47.612...^\circ \end{aligned}$$

The measure of $\angle B$ is 48° .

The answer seems reasonable. $\angle B$ must be less than 80° , because 9 km is less than 12 km.



I drew a diagram and marked the angles I knew. I knew east-west lines are all parallel, so the alternate interior angle at B must be 40° .

$N82^\circ W$

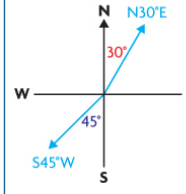
The captain must head $N82^\circ W$ from lighthouse B .

The line segment from lighthouse B to lighthouse A makes an 8° angle with west-east. I subtracted this from 90° to determine the direction west of north.

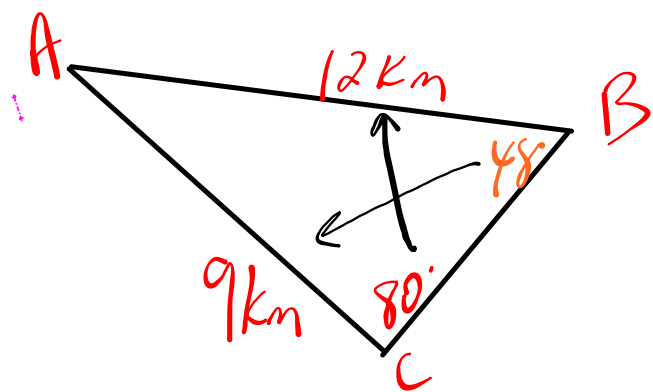
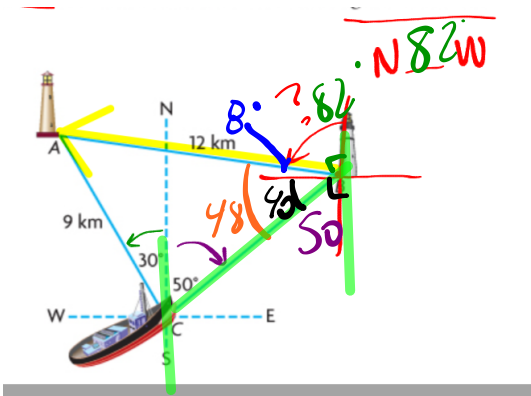
NOTE:

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Compass Rose Animation



$$\frac{9 \sin \theta}{9} = \frac{9 \sin 80^\circ}{12}$$

$$\sin^{-1} \sin \theta = (0.7386)$$

$$\theta = 48^\circ$$

10.12 # 9-12
Assignment HW

* Thurs
Text [p. 152 # 3
p. 154 # 11, 12