



TEST Is Now  
MONDAY, MAY 28<sup>th</sup>




## Chapter 8: Notes

$$c^2 = a^2 + b^2$$

$$a^2 = c^2 - b^2$$


(SATT)

&lt; \_\_\_ = 90° (Tang P)

< \_\_\_ = \_\_\_° ( ins/cent >, )

(ITT)

&lt; \_\_\_ = 90° (Chord P)

< \_\_\_ = \_\_\_° ( ins >, )

(SAT)

(CAT)

\_\_\_ = \_\_\_ (Chord P)

&lt; \_\_\_ = \_\_\_° ( ins &gt;, diam)

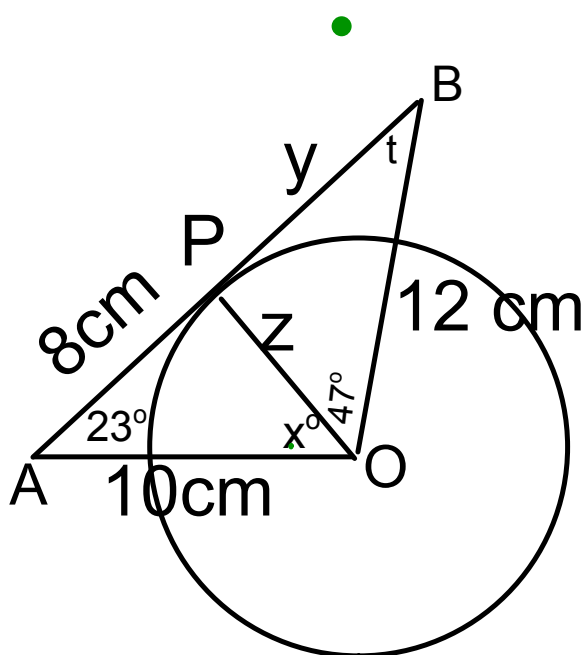
(CyAT)

(OAT)

(EAT)

&lt; \_\_\_ = \_\_\_° (CyQuad)

Calculate all the unknowns:



$$\angle APO = 90^\circ \text{ (tang P)}$$

$$\angle BPO$$

$$\angle AOP = 67^\circ \text{ (S A T T)}$$

$$\angle PBO = 43^\circ \text{ (S A T T)}$$

$$z \Rightarrow \text{leg}$$

$$a^2 = c^2 - b^2$$

$$10^2 - 8^2$$

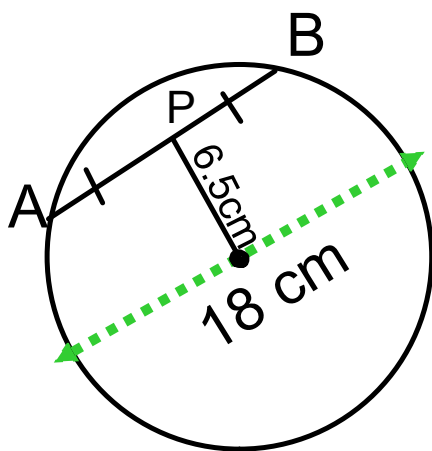
$$z = 6$$

$$y = \text{leg}$$

$$a^2 = c^2 - b^2$$

$$y = 10 \bullet 4$$

Calculate the length of the chord:



$$\left. \begin{array}{l} \angle APO = 90^\circ \\ \angle BPO = 90^\circ \end{array} \right\} \text{(chord P)}$$

AP  $\rightarrow$  leg

$$a^2 = c^2 - b^2$$

$$a^2 = 9^2 - 6.5^2$$

$$a^2 = 81 - 42.25$$

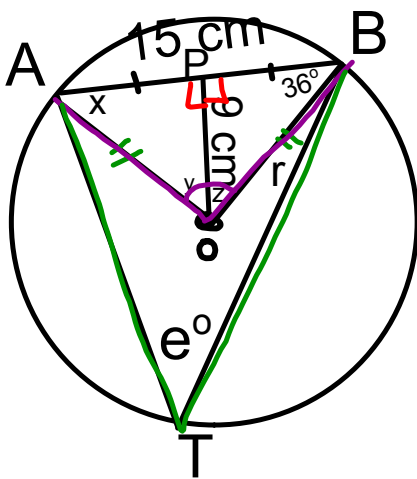
$$\sqrt{a^2} = \sqrt{38.75}$$

$$a = 6.2$$

$$AB = 2(6.2)$$

$$AB = 12.4 \text{ cm}$$

Calculate all the unknowns:



$$\left. \begin{aligned} \angle APO &= 90^\circ \\ \angle BPO &= 90^\circ \end{aligned} \right\} \text{chord}$$

$$\angle BAO = x^\circ = 36^\circ \text{ (ITT)}$$

$$\angle AOP = y^\circ = 180 - 90 - 36$$

$$y = 54^\circ \text{ (SATT)}$$

$$\angle BOP = z = 54^\circ \text{ (SATT)}$$

$$\angle ATB = e = 54^\circ \text{ (Ins/cent, } \widehat{AB})$$

radius  $\rightarrow$  hyp

$$c^2 = a^2 + b^2$$

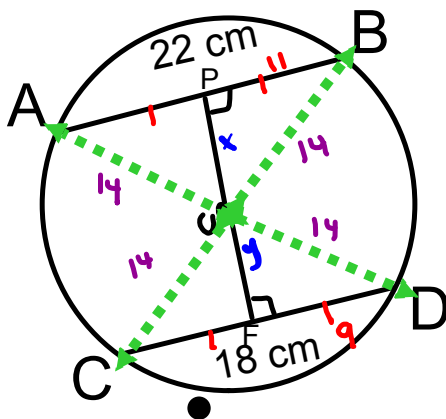
$$c^2 = 9^2 + 7.5^2$$

$$c^2 = 81 + 56.25$$

$$\sqrt{c^2} = \sqrt{137.25}$$

$$c = 11.7$$

Calculate the largest distance between the two chords if the Chord AB is 22cm and the Chord CD is 18cm and the diameter of the circle is 28 cm:  
Sketch a diagram



$$AP = PB \text{ (chord)}$$

$$x \rightarrow \text{leg}$$

$$a^2 = c^2 - b^2$$

$$a^2 = 14^2 - 11^2$$

$$a^2 = 196 - 121$$

$$\sqrt{a^2} = \sqrt{75}$$

$$a = 8.7$$

$$\text{Total distance} = 8.7 + 10.7 = 19.4$$

$$CF = FD \text{ (chord)}$$

$$y \rightarrow \text{leg}$$

$$a^2 = c^2 - b^2$$

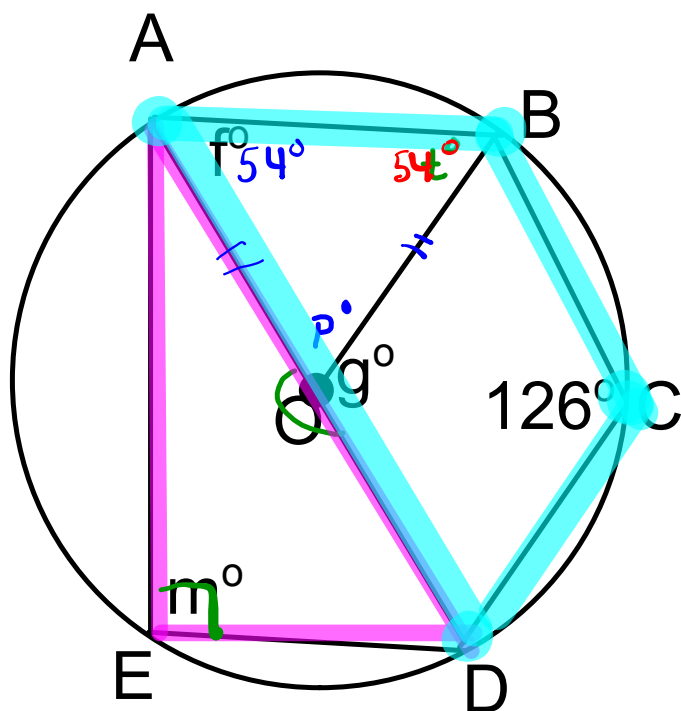
$$a^2 = 14^2 - 9^2$$

$$a^2 = 196 - 81$$

$$\sqrt{a^2} = \sqrt{115}$$

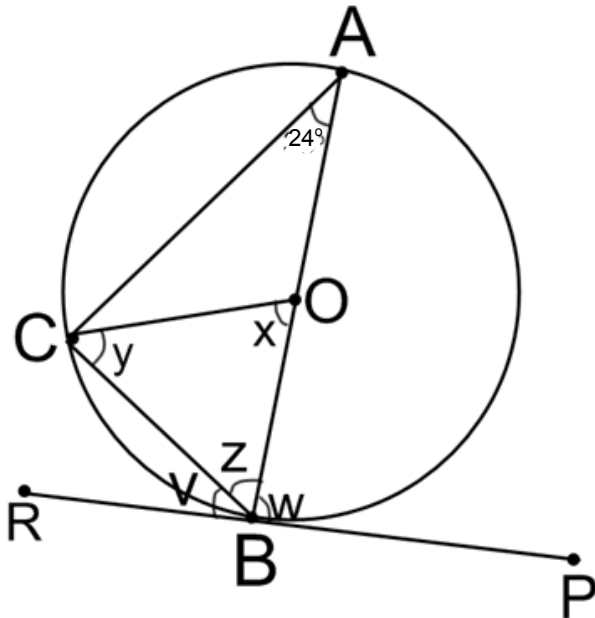
$$a = 10.7$$

# Warm Up



$m = 90^\circ$  (ins  $\angle$ ,  $d^\circ$ )  
 $f^\circ = 54^\circ$  (cyc  $\angle$   $u$   $a$ )  
 $t^\circ = 54^\circ$  (ITT)  
 $P^\circ = 72^\circ$  (SATT)  
 $g = 108^\circ$  (SAT) .)

# Warm Up



Do on your own

$$x = 48^\circ \text{ (cent } \angle \text{ CB)}$$

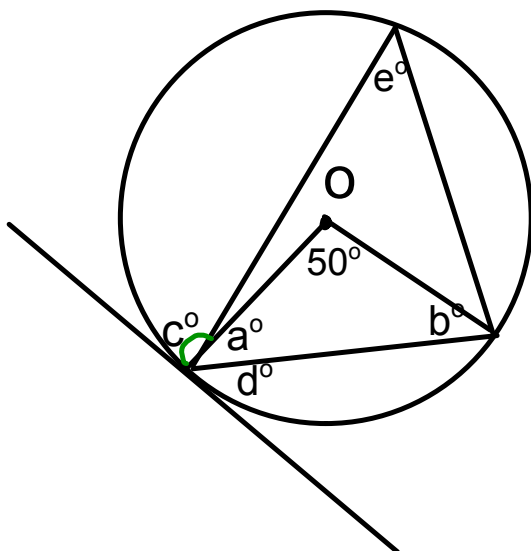
$$w = 90^\circ \text{ (tang P)}$$

$$\left. \begin{matrix} y = 66^\circ \\ z = 66^\circ \end{matrix} \right\} \text{ Iso } \Delta$$

$$V = 24^\circ \text{ (st line)}$$



Warm Up

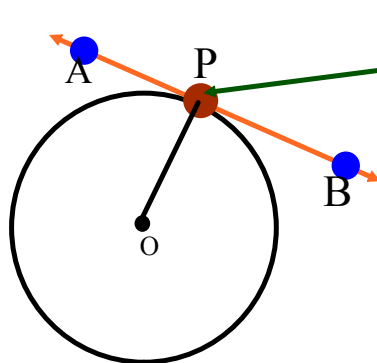


$$\left. \begin{array}{l} a^\circ = 65^\circ \\ b^\circ = 65^\circ \end{array} \right\} (I+t)$$

## Tangent Properties

- **tangent** - a line that touches a circle/curve at only 1 point.  
- the point of contact is called the **point of tangency**.

ex:



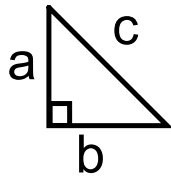
Line **AB** is a **tangent**

"**P**" is the **point of tangency**

Center is Denoted by "**O**"

# Chapter 8: Notes

## Pythagorean theorem

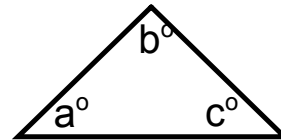


Hyp = ?  
 $c^2 = a^2 + b^2$

Leg = ?  
 $a^2 = c^2 - b^2$

## Angle Sum of Triangle Theorem

**(SATT)**

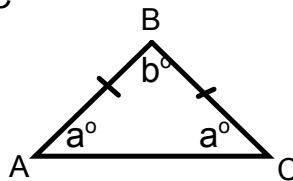


$$a^\circ + b^\circ + c^\circ = 180^\circ$$

## Isosceles Triangle Theorem **(ITT)**

Two sides are equal :  $AB = BC$

Base angles are equal:  
 $\angle A = \angle C$



If  $a^\circ = ?$

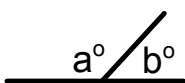
$$a^\circ = \frac{180 - b}{2}$$

If  $b^\circ = ?$

$$b^\circ = 180 - a^\circ - a^\circ$$

### Angle Properties

#### Supplementary Angle Theorem **(SAT)**



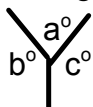
$$a^\circ + b^\circ = 180^\circ$$

#### Complimentary Angle Theorem **(CAT)**



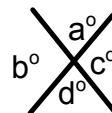
$$a^\circ + b^\circ = 90^\circ$$

#### Cyclic Angle Theorem **(CyAT)**



$$a^\circ + b^\circ + c^\circ = 360^\circ$$

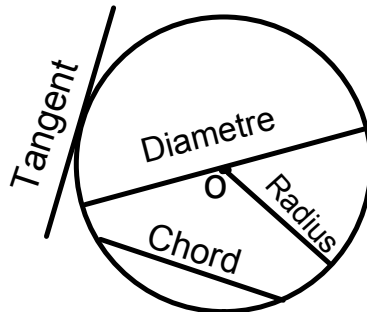
#### Opposite Angle Theorem **(OAT)**



$$a^\circ = d^\circ$$

$$b^\circ = c^\circ$$

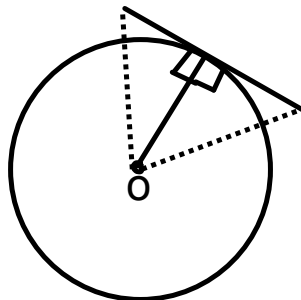
### Information about circles



### Tangent Property

$$\angle \_ = 90^\circ \text{ (Tang P)}$$

- a radius hits a tangent at  $90^\circ$



To solve unknown sides :  
Pythagorean Theorem

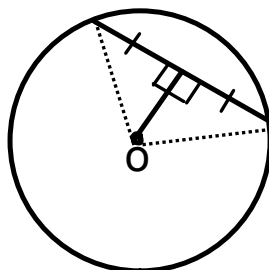
To solve unknown angles :  
SATT

### Chord Property

$$\text{If chord lengths are indicated} \\ \angle \_ = \angle \_ = 90^\circ \text{ (Chord P)}$$

a line coming from the centre of the circle

- hits chord at a  $90^\circ$  angle
- cuts the chord into two equal pieces



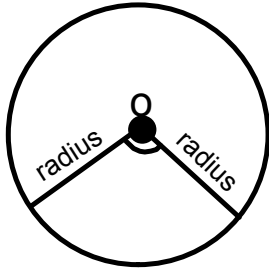
$$\text{If } 90^\circ \text{ is indicated} \\ \_ = \_ \text{ (Chord P)}$$

To solve unknown sides :  
Pythagorean Theorem

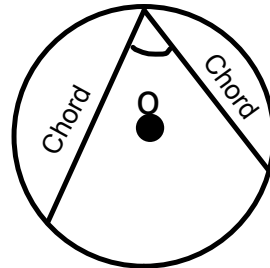
To solve unknown angles :  
SATT  
ITT

# Circle Properties

## Central Angle

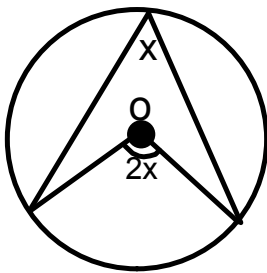


## Inscribed Angle



### Property # 1: Central & Inscribed Angles

$$\angle \text{---} = \text{---}^\circ \text{ ( ins/cent >, \overset{\frown}{\text{---}} )}$$

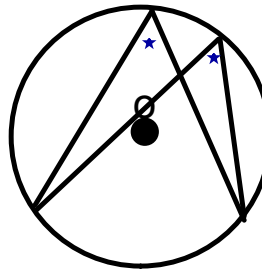


- The central angle is double the inscribed angle

- The inscribed angle is half the central angle

### Property # 2: Inscribed Angles

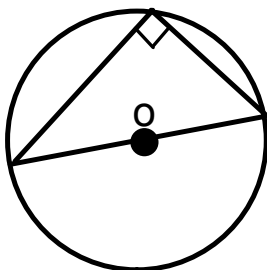
$$\angle \text{---} = \text{---}^\circ \text{ ( ins >, \overset{\frown}{\text{---}} )}$$



- Inscribed angles coming from the same arc are equal

### Property # 3: Inscribed from Diameter

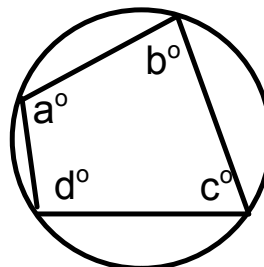
$$\angle \text{---} = \text{---}^\circ \text{ ( ins >, \text{diam} )}$$



- Inscribed angles coming from the diameter are  $90^\circ$

### Property # 4: Cyclic Quadrilateral

$$\angle \text{---} = \text{---}^\circ \text{ (CyQuad)}$$



- Opposite angles in a cyclic quad must add up to  $180^\circ$

$$a^\circ + c^\circ = 180^\circ$$

$$b^\circ + d^\circ = 180^\circ$$



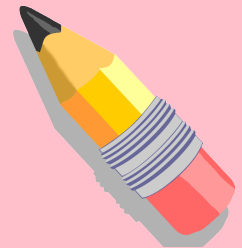
Homework:

**TEST Tomorrow**

p. 418 - 419

#

- |   |    |
|---|----|
| 1 | 8  |
| 2 | 9  |
| 5 | 10 |
| 6 |    |
| 7 |    |



Practice Test page 420

**1,2,3**

## Attachments

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CSI Crime Scene Investigation.mp3

Worksheet - Angles in a Circle.doc