

## Curriculum Outcome

(N5) Determine the square root of positive rational numbers that are perfect squares.

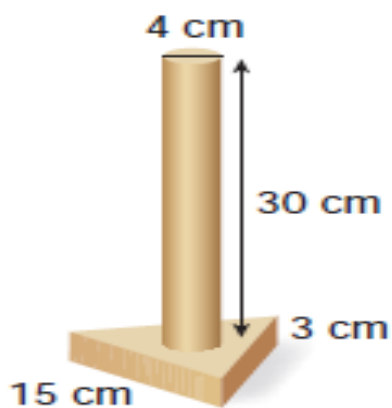
(N6) Determine an approximate square root of positive rational numbers that are non-perfect squares.

(SS2) Determine the surface area of composite 3-D objects to solve problems

(N4) \*\*Explain and apply the order of operations, including exponents, with and without technology.\*\*

**Apply****Warm Up**

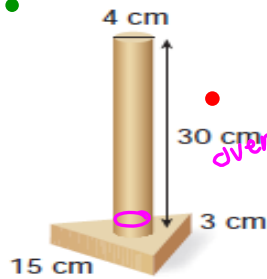
6. Here is the lamp stand from the top of page 33. The base of the lamp is a triangular prism with an equilateral triangle base. The surface of the stand is to be painted. What is the area that will be painted? Give the answer to the nearest whole number.



# Warm Up

## Apply

6. Here is the lamp stand from the top of page 33. The base of the lamp is a triangular prism with an equilateral triangle base. The surface of the stand is to be painted. What is the area that will be painted? Give the answer to the nearest whole number.



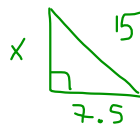
Cylinder:  $r = 2$ ,  $h = 30$

$$SA = 2\pi r^2 + 2\pi r h$$

overlap  $\rightarrow SA = 2(3.14)(2)^2 + 2(3.14)(2)(30)$

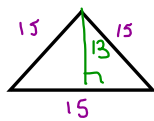
$$SA = \frac{25.12}{2} + 376.8$$

$$SA = 401.92 \text{ cm}^2$$



$$\begin{aligned} b^2 &= c^2 - a^2 \\ b^2 &= 15^2 - 7.5^2 \\ b^2 &= 225 - 56.25 \\ \sqrt{b^2} &= \sqrt{168.75} \\ b &= 13 \end{aligned}$$

-triangular prism

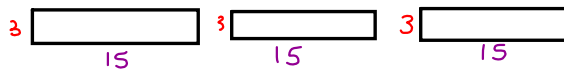


$$A = \frac{b \times h}{2}$$

$$A = \frac{15 \times 13}{2}$$

$$A = 97.5$$

$$2A = 195$$



$$A = b \times h$$

$$A = 3 \times 15$$

$$A = 45 \text{ cm}^2$$

$$45 \text{ cm}^2$$

$$45 \text{ cm}^2$$

$$SA = 195 + 45 + 45 + 45$$

$$= 330 \text{ cm}^2$$

$$T_{SA} = SA_1 + SA_2 - \text{overlap}$$

$$= 401.92 + 330 - 25.12$$

$$= 706.8 \text{ cm}^2$$

Class / Homework

Practice Page 40 - 43

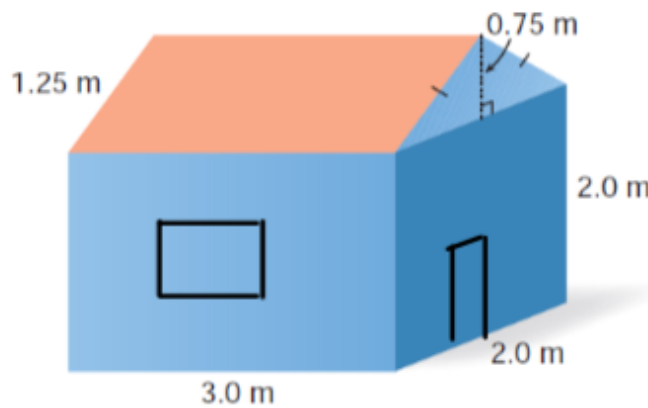
Questions :

Page 40-41

Questions: 3e, 4ab, 5ab, 7

7. Assessment Focus

a) A playhouse has the shape of a rectangular prism with a triangular prism roof. Determine the surface area of the playhouse.



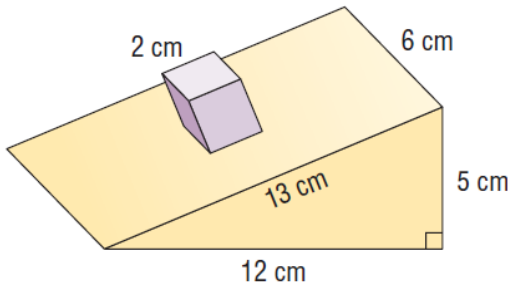
Without bottom

a)  $29 \text{ m}^2$

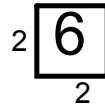
b)  $25.87 \text{ m}^2$

b) Door is  $0.5 \text{ m} \times 0.5 \text{ m}$   
2 Windows  $1.2 \text{ m} \times 1.2 \text{ m}$

3) e) cube on a triangular prism



Cube (2,2,2)



$$A = b \times h$$

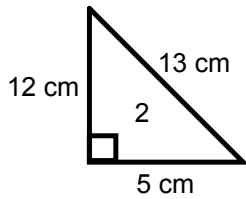
$$A = 2 \text{ cm} \times 2 \text{ cm}$$

$$A = 4 \text{ cm}^2$$

$$\times 6$$

$$= 24 \text{ cm}^2$$

Triangular Prism



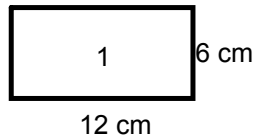
$$A = \frac{b \times h}{2}$$

$$A = \frac{5 \times 12}{2}$$

$$A = \frac{60}{2}$$

$$A = 30$$

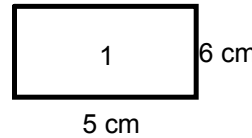
$$2A = 60 \text{ cm}^2$$



$$A = b \times h$$

$$A = 12 \times 6$$

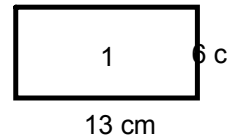
$$A = 72 \text{ cm}^2$$



$$A = b \times h$$

$$A = 5 \times 6$$

$$A = 30 \text{ cm}^2$$



$$A = b \times h$$

$$A = 13 \times 6$$

$$A = 78 \text{ cm}^2$$

$$SA \text{ Large} = 60 + 72 + 30 + 78$$

$$= 240 \text{ cm}^2$$

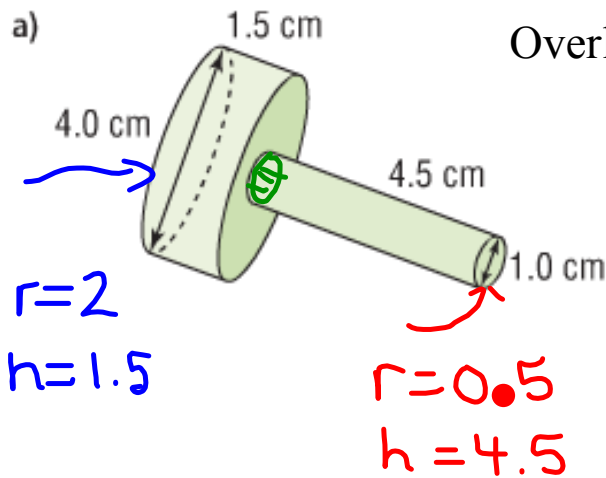
$$\text{Total SA} = \text{Triangular Prism} + \text{Cube} - \text{Overlap}$$

$$= 240 \text{ cm}^2 + 24 \text{ cm}^2 - 8 \text{ cm}^2$$

$$= 256 \text{ cm}^2$$

4

a)



Top

$$\begin{aligned} \text{Area of cylinder} &= 2\pi r^2 + 2\pi rh \\ &= 2(3.14)(2\text{cm})^2 + 2(3.14)(2\text{cm})(1.5\text{cm}) \\ &= 2(3.14)(4\text{cm}) + 2(3.14)(2\text{cm})(1.5\text{cm}) \\ &= 25.12 \text{ cm}^2 + 18.84 \text{ cm}^2 \\ &= 43.96 \text{ cm}^2 \end{aligned}$$

Long

Overlap

$$\begin{aligned} \text{Area of cylinder} &= 2\pi r^2 + 2\pi rh \\ &= 2(3.14)(0.5\text{cm})^2 + 2(3.14)(0.5\text{cm})(4.5\text{cm}) \\ &= 2(3.14)(0.25\text{cm}) + 2(3.14)(0.5\text{cm})(4.5\text{cm}) \\ &= 1.57 \text{ cm}^2 + 14.13 \text{ cm}^2 \\ &= 15.7 \text{ cm}^2 \end{aligned}$$

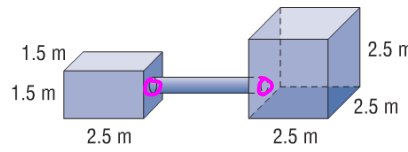
$$\begin{aligned} \text{Total SA} &= \text{Cylinder} + \text{Cylinder} - \text{Overlap} \\ &= 43.96 \text{ cm}^2 + 15.7 \text{ cm}^2 - 1.57 \text{ cm}^2 \\ &= 58.09 \text{ cm}^2 \\ &= 58.1 \text{ cm}^2 \end{aligned}$$

Homework solutions

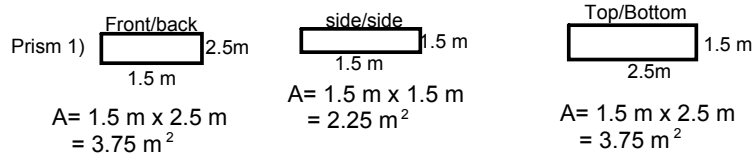
Solutions

- 4 b) The cylinder is 3.5 m long with diameter 0.5 m.

$h = 3.5$   
 $r = 0.25$



Area of cylinder =  $2\pi r^2 + 2\pi rh$   
 $= 2(3.14)(0.25\text{m})^2 + 2(3.14)(0.25\text{m})(3.5\text{m})$   
 $= 2(3.14)(0.0625\text{m}^2) + 2(3.14)(0.25\text{m})(3.5\text{m})$   
 $= 0.3925\text{m}^2 + 5.495\text{m}^2$   
 $= 5.8875\text{m}^2$



SA Prism 1 =  $2(3.75\text{ m}^2) + 2(2.25\text{ m}^2) + 2(3.75\text{ m}^2)$   
 $= 7.5\text{ m}^2 + 4.5\text{ m}^2 + 7.5\text{ m}^2$   
 $= 19.5\text{ m}^2$

Cube)

Surface area of 1 face =  $2.5\text{ m} \times 2.5\text{ m}$   
 $= 6.25\text{ m}^2$   
 $\frac{\times 6 \leftarrow 6 \text{ equal faces}}{37.5\text{ m}^2}$

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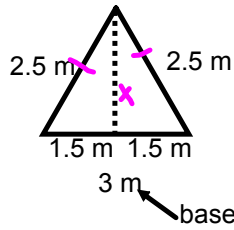
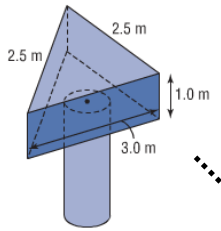
Total SA = Rectangular Prism + Cube + Cylinder - Total Overlap  
 $= 19.5\text{ m}^2 + 37.5\text{ m}^2 + 5.8875\text{ m}^2 - 0.785\text{ m}^2$   
 $= 61.6025\text{ m}^2$

Or if you rounded to the nearest tenth

Total SA = Rectangular Prism + Cube + Cylinder - Total Overlap  
 $= 19.5\text{ m}^2 + 37.5\text{ m}^2 + 5.8875\text{ m}^2 - 0.785\text{ m}^2$   
 $= 19.5\text{ m}^2 + 37.5\text{ m}^2 + 5.9\text{ m}^2 - 0.8\text{ m}^2$   
 $= 62.1\text{ m}^2$

5. Determine the surface area of each composite object.

a) The cylinder is 2.5 m long with radius 0.5 m.



$$\begin{aligned} \text{height}^2 &= c^2 - b^2 \\ &= (2.5 \text{ m})^2 - (1.5 \text{ m})^2 \\ &= 6.25 \text{ m}^2 - 2.25 \text{ m}^2 \\ &= 4 \text{ m}^2 \\ \text{height} &= \sqrt{4 \text{ m}^2} \\ \text{height} &= 2 \text{ m} \end{aligned}$$

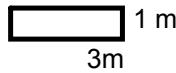
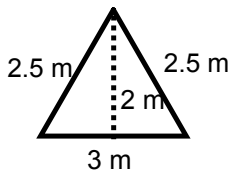
**Triangular prism**

$$A = \frac{b \times h}{2}$$

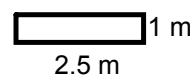
$$A = \frac{3 \text{ m} \times 2 \text{ m}}{2}$$

$$A = \frac{6 \text{ m}^2}{2}$$

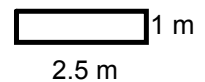
$$A = 3 \text{ m}^2$$



$$\begin{aligned} A &= b \times h \\ &= 3 \text{ m} \times 1 \text{ m} \\ &= 3 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 2.5 \text{ m} \times 1 \text{ m} \\ &= 2.5 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 2.5 \text{ m} \times 1 \text{ m} \\ &= 2.5 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Total SA Triangular Prism} &= 2 \text{ triangles} + \text{rectangle} + \text{rectangle} + \text{rectangle} \\ &= 2(3 \text{ m}^2) + 3 \text{ m}^2 + 2.5 \text{ m}^2 + 2.5 \text{ m}^2 \\ &= 6 \text{ m}^2 + 3 \text{ m}^2 + 2.5 \text{ m}^2 + 2.5 \text{ m}^2 \\ &= 14 \text{ m}^2 \end{aligned}$$

**Cylinder**

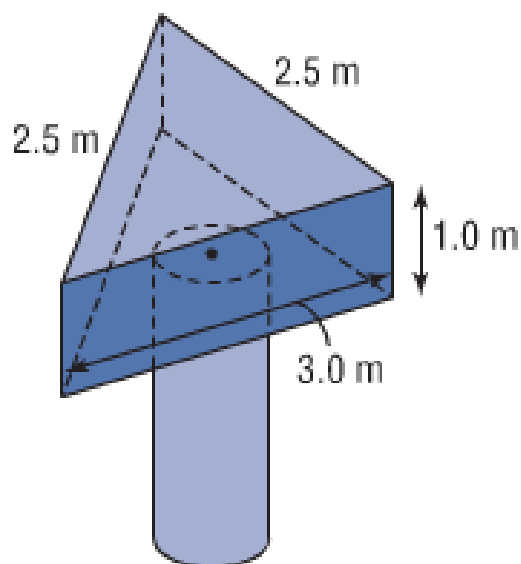
$$\begin{aligned} \text{Area of cylinder} &= 2\pi r^2 + 2\pi r h \\ &= 2(3.14)(0.5)^2 + 2(3.14)(0.5)(2.5) \\ &= 2(3.14)(0.25) + 2(3.14)(0.5)(2.5) \\ &= 1.57 \text{ m}^2 + 7.85 \text{ m}^2 \\ &= 9.42 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Total Surface} &= \text{Triangular Prism} + \text{Cylinder} - \text{total overlap} \\ &= 14 \text{ m}^2 + 9.42 \text{ m}^2 - 1.57 \text{ m}^2 \\ &= 21.85 \text{ m}^2 \end{aligned}$$

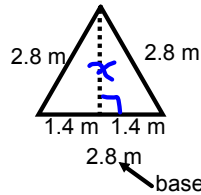
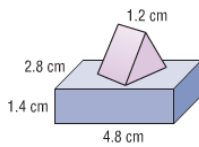


5. Determine the surface area of each composite object.

- a) The cylinder is 2.5 m long with radius 0.5 m.

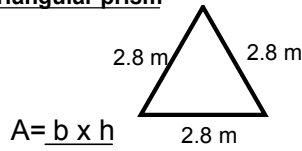


b) The base of the triangular prism is an equilateral triangle with side length 2.8 cm.

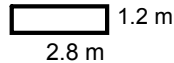


$$\begin{aligned} \text{height}^2 &= c^2 - b^2 \\ &= (2.8 \text{ m})^2 - (1.4 \text{ m})^2 \\ &= 7.84 \text{ m}^2 - 1.96 \text{ m}^2 \\ &= 5.88 \text{ m}^2 \\ \text{height} &= \sqrt{5.88 \text{ m}^2} \\ \text{height} &= 2.4 \text{ m} \end{aligned}$$

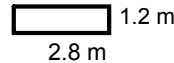
**Triangular prism**



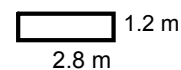
$$\begin{aligned} A &= \frac{b \times h}{2} \\ A &= \frac{2.8 \text{ m} \times 2.4 \text{ m}}{2} \\ A &= \frac{6.72 \text{ m}^2}{2} \\ A &= 3.36 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 2.8 \text{ m} \times 1.2 \text{ m} \\ &= 3.36 \text{ m}^2 \end{aligned}$$



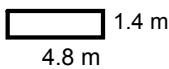
$$\begin{aligned} A &= b \times h \\ &= 2.8 \text{ m} \times 1.2 \text{ m} \\ &= 3.36 \text{ m}^2 \end{aligned}$$



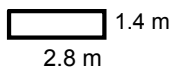
$$\begin{aligned} A &= b \times h \\ &= 2.8 \text{ m} \times 1.2 \text{ m} \\ &= 3.36 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Total SA Triangular Prism} &= 2 \text{ triangles} + \text{rectangle} + \text{rectangle} + \text{rectangle} \\ &= 2 (3.36 \text{ m}^2) + 3.36 \text{ m}^2 + 3.36 \text{ m}^2 + 3.36 \text{ m}^2 \\ &= 6.72 \text{ m}^2 + 3.36 \text{ m}^2 + 3.36 \text{ m}^2 + 3.36 \text{ m}^2 \\ &= 16.8 \text{ m}^2 \end{aligned}$$

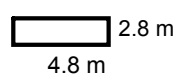
**Prism**



$$\begin{aligned} A &= b \times h \\ &= 4.8 \text{ m} \times 1.4 \text{ m} \\ &= 6.72 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 2.8 \text{ m} \times 1.4 \text{ m} \\ &= 3.92 \text{ m}^2 \end{aligned}$$

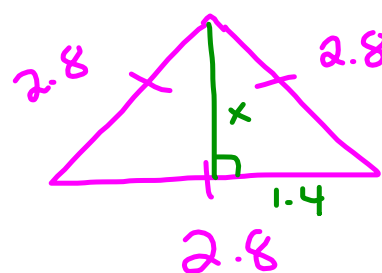
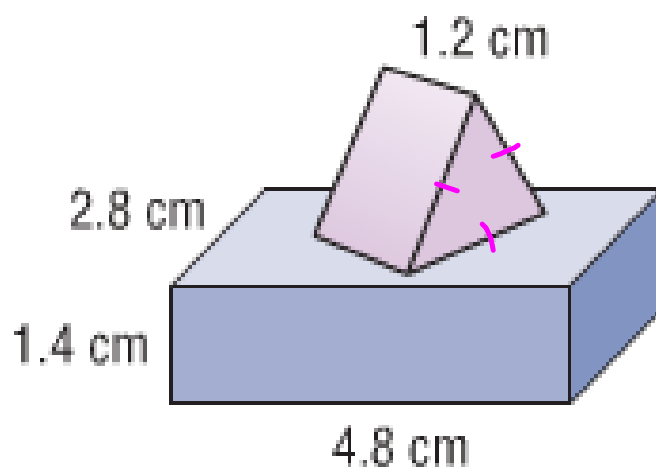


$$\begin{aligned} A &= b \times h \\ &= 2.8 \text{ m} \times 4.8 \text{ m} \\ &= 13.44 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Prism} &= 2 \text{ top} + 2 \text{ side} + 2 \text{ front} \\ &= 2 (6.72) + 2 (3.92) + 2(13.44) \\ &= 13.44 + 7.84 + 26.88 \\ &= 48.16 \end{aligned}$$

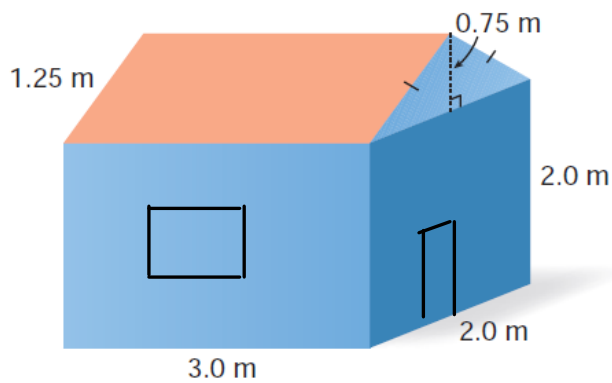
$$\begin{aligned} \text{Total SA} &= \text{Triangular Prism} + \text{Rectangular Prism} - \text{overlap} \\ &= 16.8 \text{ m}^2 + 48.12 \text{ m}^2 - 6.72 \text{ m}^2 \\ &= 64.92 \text{ m}^2 - 6.72 \text{ m}^2 \\ &= 58.2 \text{ m}^2 \end{aligned}$$

17) The base of the triangular prism is an equilateral triangle with side length 2.8 cm.



**7. Assessment Focus**

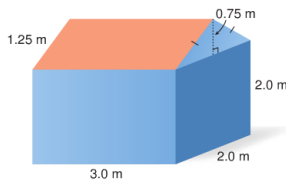
- a) A playhouse has the shape of a rectangular prism with a triangular prism roof. Determine the surface area of the playhouse.



$$a) 29 \text{ m}^2$$

$$b) 25.87 \text{ m}^2$$

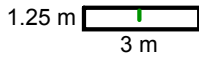
- b) Door is 0.5m x 0.5m  
 2 Windows 1.2m x 1.2m



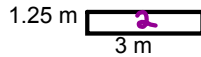
**Triangular Prism**

$$\begin{aligned} \text{Area of Triangle} &= \frac{b \times h}{2} \\ &= \frac{(2 \text{ m}) \times (0.75 \text{ m})}{2} \\ &= \frac{1.5 \text{ m}^2}{2} \\ &= 0.75 \text{ m}^2 \end{aligned}$$

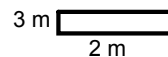
Without bottom



$$\begin{aligned} A &= b \times h \\ &= 1.25 \text{ m} \times 3 \text{ m} \\ &= 3.75 \text{ m}^2 \end{aligned}$$



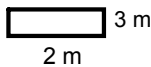
$$\begin{aligned} A &= b \times h \\ &= 1.25 \text{ m} \times 3 \text{ m} \\ &= 3.75 \text{ m}^2 \end{aligned}$$



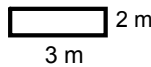
$$\begin{aligned} A &= b \times h \\ &= 2 \text{ m} \times 3 \text{ m} \\ &= 6 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Total SA of triangular prism} &= 2 \text{ Triangles} + \text{Rectangle} + \text{Rectangle} + \text{Rectangle} \\ &= 2(0.75 \text{ m}^2) + 3.75 \text{ m}^2 + 3.75 \text{ m}^2 + 6 \text{ m}^2 \\ &= 1.5 \text{ m}^2 + 3.75 \text{ m}^2 + 3.75 \text{ m}^2 + 6 \text{ m}^2 \\ &= 15 \text{ m}^2 \end{aligned}$$

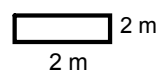
**Prism**



$$\begin{aligned} A &= b \times h \\ &= 3 \text{ m} \times 2 \text{ m} \\ &= 6 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 3 \text{ m} \times 2 \text{ m} \\ &= 6 \text{ m}^2 \end{aligned}$$



$$\begin{aligned} A &= b \times h \\ &= 2 \text{ m} \times 2 \text{ m} \\ &= 4 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Prism} &= 2 \text{ top} + 2 \text{ side} + 2 \text{ front} \\ &= 2 (6) + 2 (6) + 2(4) \\ &= 12 + 12 + 8 \\ &= 32 \end{aligned}$$

$$\begin{aligned} \text{Overlap} &= b \times h \\ &= 3 \text{ m} \times 2 \text{ m} \\ &= 6 \text{ m}^2 \\ &\quad \times 2 \text{ faces} \\ \hline &= 12 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \text{Bottom} &= b \times h \\ &= 3 \text{ m} \times 2 \text{ m} \\ &= 6 \text{ m}^2 \end{aligned}$$

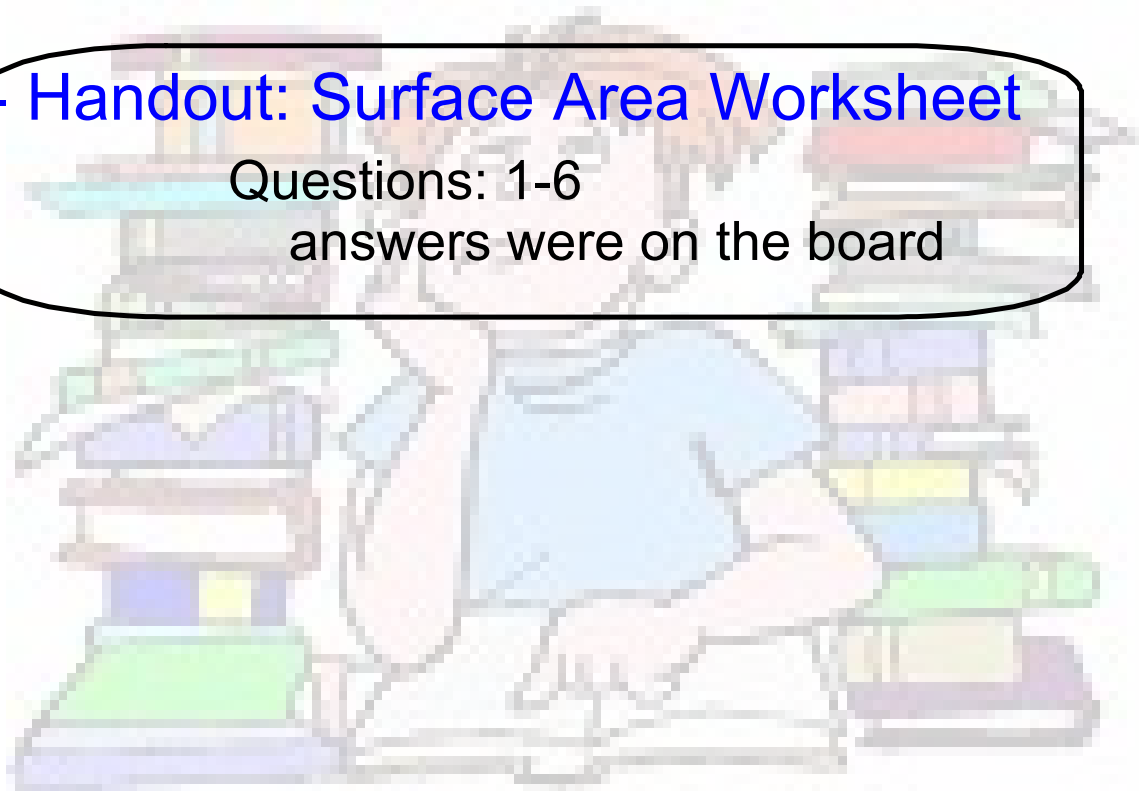
$$\begin{aligned} \text{without bottom} &= \text{Triangular Prism} + \text{Rectangular Prism} - \text{overlap} - \text{bottom} \\ &= 15 \text{ m}^2 + 32 \text{ m}^2 - 12 \text{ m}^2 - 6 \text{ m}^2 \\ &= 29 \text{ m}^2 \end{aligned}$$

Class / Homework  
Review For Test ●

- Handout: Surface Area Worksheet

Questions: 1-6

answers were on the board



**UNIT 3 ASSIGNMENT – SURFACE AREA OF COMPOSITE OBJECTS**

Determine the surface area of each composite object. Round answers to the nearest tenth, where necessary. Show ALL work on loose-leaf.

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- The cylinder below is connected to two **IDENTICAL EQUILATERAL TRIANGULAR prisms**. The cylinder's diameter is 10 cm.

# Worksheet

## Answers

$$1) 1680 \text{ cm}^2$$

$$2) 952.8 \text{ mi}^2$$

$$3) 791.3 \text{ cm}^2$$

$$4) 990 \text{ mm}^2$$

$$5) 528.9 \text{ cm}^2$$

$$6) 426.8 \text{ cm}^2$$