

## Quadratic Equations: Review Section

### MULTIPLE CHOICE

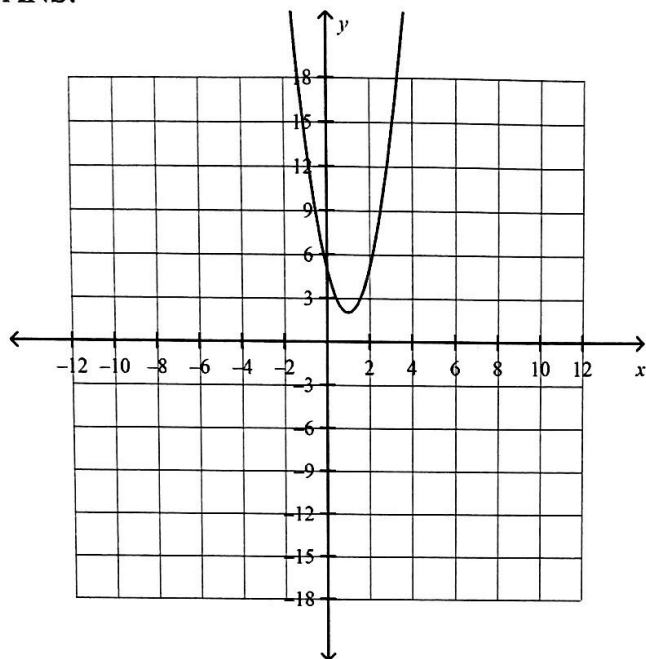
1. ANS: A                   PTS: 1                   DIF: Average           OBJ: Section 4.1  
NAT: RF 5               TOP: Graphical Solutions of Quadratic Equations  
KEY: two real roots
2. ANS: D                   PTS: 1                   DIF: Easy               OBJ: Section 4.2  
NAT: RF 5               TOP: Factoring Quadratic Equations           KEY: factor trinomial
3. ANS: A                   PTS: 1                   DIF: Average           OBJ: Section 4.2  
NAT: RF 5               TOP: Factoring Quadratic Equations           KEY: factor trinomial
4. ANS: C                   PTS: 1                   DIF: Difficult           OBJ: Section 4.2  
NAT: RF 5               TOP: Factoring Quadratic Equations           KEY: solve trinomial
5. ANS: C                   PTS: 1                   DIF: Easy               OBJ: Section 4.2  
NAT: RF 5               TOP: Factoring Quadratic Equations           KEY: solve factored trinomial
6. ANS: A                   PTS: 1                   DIF: Easy               OBJ: Section 4.3  
NAT: RF 5               TOP: Solving Quadratic Equations by Completing the Square  
KEY: perfect square trinomial
7. ANS: C                   PTS: 1                   DIF: Average           OBJ: Section 4.3  
NAT: RF 5               TOP: Solving Quadratic Equations by Completing the Square  
KEY: vertex form
8. ANS: D                   PTS: 1                   DIF: Difficult           OBJ: Section 4.4  
NAT: RF 5               TOP: The Quadratic Formula                   KEY: quadratic formula
9. ANS: C                   PTS: 1                   DIF: Average           OBJ: Section 4.4  
NAT: RF 5               TOP: The Quadratic Formula                   KEY: quadratic formula | extraneous root
10. ANS: D                   PTS: 1                   DIF: Average           OBJ: Section 4.4  
NAT: RF 5               TOP: The Quadratic Formula                   KEY: quadratic formula | parabolic motion
11. ANS: B                   PTS: 1                   DIF: Difficult           OBJ: Section 4.4  
NAT: RF 5               TOP: The Quadratic Formula                   KEY: x-intercepts

### COMPLETION

1. ANS:  $y = -0.75x^2 - 2.25x - 1.5$   
PTS: 1                   DIF: Average           OBJ: Section 4.1           NAT: RF 5  
TOP: Graphical Solutions of Quadratic Equations           KEY: roots of quadratic equation

## SHORT ANSWER

1. ANS:



There are no zeros.

PTS: 1                    DIF: Average                    OBJ: Section 4.1                    NAT: RF 5  
 TOP: Graphical Solutions of Quadratic Equations                    KEY: zeros | x-intercepts

2. ANS:

- a)  $k = 20.25$
- b)  $k < 20.25$
- c)  $k > 20.25$

PTS: 1                    DIF: Difficult                    OBJ: Section 4.4                    NAT: RF 5  
 TOP: The Quadratic Formula                    KEY: number of roots

3. ANS:

Rearrange the equation so all terms are on the same side:

$$3x^2 - 8x + 4 = 0$$

Calculate the discriminant  $b^2 - 4ac$ :

$$\begin{aligned} (-8)^2 - 4(3)(4) &= 64 - 48 \\ &= 16 \end{aligned}$$

Since the discriminant is positive (greater than zero), the equation has 2 real roots.

$$\mathbf{a)} \quad x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{8 \pm \sqrt{16}}{2(3)}$$

$$= \frac{8 \pm 4}{6}$$

$$= 2 \text{ and } \frac{2}{3}$$

$$\mathbf{b)} \quad 3x^2 - 8x + 4 = 0$$

$$(3x - 2)(x - 2) = 0$$

$$3x - 2 = 0 \quad x - 2 = 0$$

$$3x = 2 \quad x = 2$$

$$x = \frac{2}{3}$$

PTS: 1

DIF: Average

OBJ: Section 4.3 | Section 4.4

NAT: RF 5

TOP: Factoring Quadratic Equations | The Quadratic Formula

KEY: roots of quadratic equation | solve factored trinomial

4. ANS:

$$\begin{aligned}
 x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\
 &= \frac{10 \pm \sqrt{(-10)^2 - 4(3)(6)}}{2(3)} \\
 &= \frac{10 \pm \sqrt{100 - 72}}{6} \\
 &= \frac{10 \pm \sqrt{28}}{6} \\
 &= \frac{10 \pm 2\sqrt{7}}{6} \\
 &= \frac{5 \pm \sqrt{7}}{3} \\
 &= \frac{5 + \sqrt{7}}{3} \text{ and } \frac{5 - \sqrt{7}}{3}
 \end{aligned}$$

PTS: 1

DIF: Average

OBJ: Section 4.4 NAT: RF 5

TOP: The Quadratic Formula

KEY: roots of quadratic equation | quadratic formula

5. ANS:

The  $x$ -intercepts are  $-2$  and  $3$ . These correspond to factors of  $(x + 2)$  and  $(x - 3)$ . The equation is of the form  $y = a(x + 2)(x - 3)$ .

Expand and simplify the right side of the equation:

$$y = a(x + 2)(x - 3)$$

$$= a(x^2 - x - 6)$$

Substitute the known point on the curve  $(0.5, -6.25)$  to determine the value of  $a$ :

$$y = a(x^2 - x - 6)$$

$$-6.25 = a[(0.5)^2 - 0.5 - 6]$$

$$-6.25 = a(0.25 - 6.5)$$

$$-6.25 = a(-6.25)$$

$$a = 1$$

The value of  $a$  is 1, so the equation is  $y = x^2 - x - 6$ .

PTS: 1

DIF: Easy

OBJ: Section 4.1

NAT: RF 5

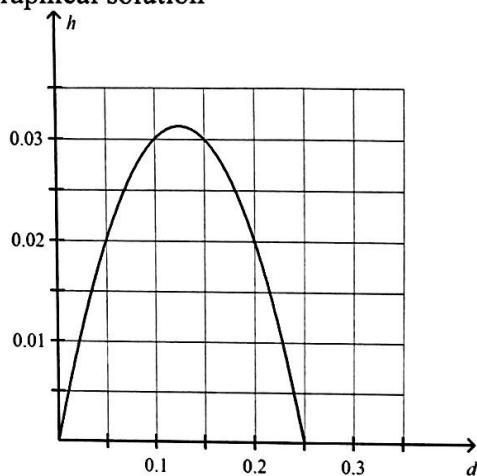
TOP: Graphical Solutions of Quadratic Equations

KEY: quadratic function | parabola

## PROBLEM

1. ANS:

Graphical solution



Determine the zeros of the function (or roots of the equation) by setting  $h = 0$  and then factoring the equation:

$$0 = -2d^2 + 0.5d$$

$$0 = d(-2d + 0.5)$$

$$d = 0 \text{ or } -2d + 0.5 = 0$$

$$d = 0 \text{ or } d = 0.25$$

The ball travels 0.25 m or 25 cm horizontally.

PTS: 1

DIF: Difficult

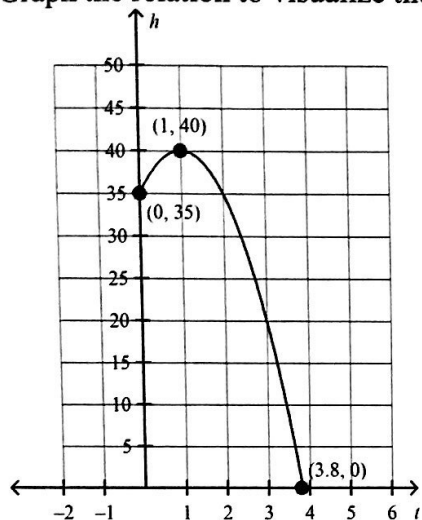
OBJ: Section 4.1 | Section 4.2

NAT: RF 5

TOP: Graphical Solutions of Quadratic Equations | Factoring Quadratic Equations

2. ANS:

Graph the relation to visualize the situation.



From the graph:

- a) The maximum height of the ball is 40 m.
- b) It takes 1 s to reach the maximum height.
- c) The  $t$ -intercept is approximately 3.8. The ball hits the ground after about 3.8 s.

From the equation:

- d) When  $t = 0$ ,  $h = 35$ . The bridge is 35 m above the river.

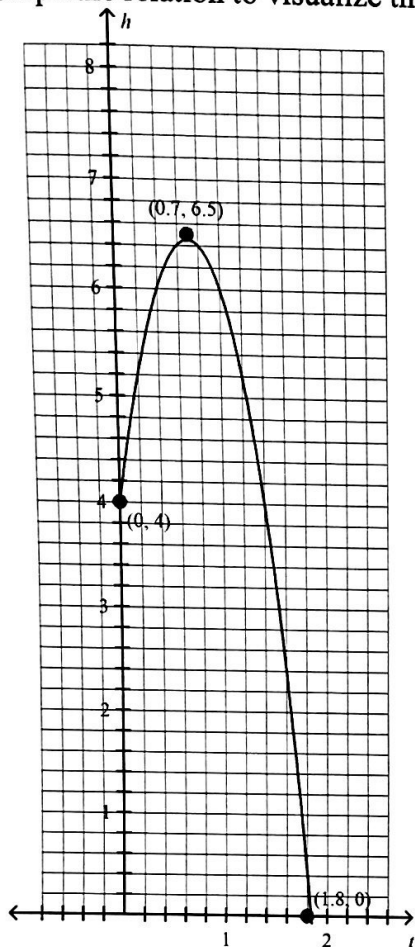
PTS: 1      DIF: Average      OBJ: Section 4.1      NAT: RF 5

TOP: Graphical Solutions of Quadratic Equations

KEY: maximum | x-intercepts | parabolic motion

3. ANS:

Graph the relation to visualize the situation.



From the graph:

- a) The maximum height is about 6.5 m.
- b) It takes about 0.7 s to reach the maximum height.
- c) The  $t$ -intercept is about 1.8. It takes Nina about 1.8 s to enter the water.
- d) Substituting  $t = 0$  into the equation, or reading from the graph at  $t = 0$ ,  $h = 4$ . So, the board is 4 m above the water.

PTS: 1      DIF: Difficult      OBJ: Section 4.1      NAT: RF 5

TOP: Graphical Solutions of Quadratic Equations

KEY: maximum | x-intercepts | parabolic motion

4. ANS:

Let  $x$  represent the first number and  $x + 3$  represent the second.

Then,

$$x^2 + (x + 3)^2 = 89$$

$$x^2 + x^2 + 6x + 9 = 89$$

$$2x^2 + 6x - 80 = 0$$

$$x^2 + 3x - 40 = 0$$

$$(x + 8)(x - 5) = 0$$

$$x = 5 \text{ or } x = -8$$

Since the result is a whole number, the negative value is rejected and the numbers are 5 and 8.

PTS: 1

DIF: Easy

OBJ: Section 4.2 NAT: RF 5

TOP: Factoring Quadratic Equations

KEY: factor quadratic

5. ANS:

Use the Pythagorean theorem.

$$(x + 4)^2 + x^2 = 20^2$$

$$x^2 + 8x + 16 + x^2 = 400$$

$$2x^2 + 8x - 384 = 0$$

Factor the trinomial to find the zeros of the quadratic relation.

$$2x^2 + 8x - 384 = 0$$

$$x^2 + 4x - 192 = 0$$

$$(x + 16)(x - 12) = 0$$

$$x = -16 \text{ or } x = 12$$

The zeros are  $-16$  and  $12$ .Since a negative distance is not reasonable, the value for  $x$  is  $12$ .The dimensions of the rectangle are  $12$  cm by  $16$  cm.

PTS: 1

DIF: Difficult

OBJ: Section 4.2 NAT: RF 5

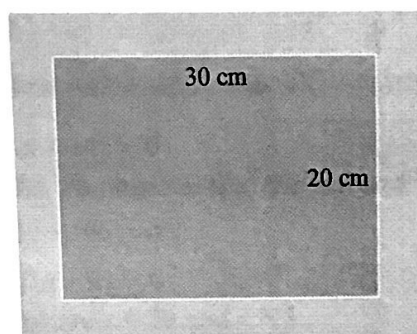
TOP: Factoring Quadratic Equations

KEY: roots of quadratic equation



6. ANS:

Sketch a diagram to visualize the situation.



The area of the photo is  $30 \text{ cm} \times 20 \text{ cm} = 600 \text{ cm}^2$ . The area of the border is four times this or  $2400 \text{ cm}^2$ . Therefore, the area of the photo and border is  $3000 \text{ cm}^2$ .

Let  $x$  be the width of the border, in centimetres.

The outside dimensions of the border are  $(30 + 2x)$  by  $(20 + 2x)$ .

$$(30 + 2x)(20 + 2x) = 3000$$

$$600 + 60x + 40x + 4x^2 = 3000$$

$$4x^2 + 100x - 2400 = 0$$

$$4(x^2 + 25x - 600) = 0$$

$$(x + 40)(x - 15) = 0$$

$$x = -40 \text{ or } x = 15$$

The zeros are at  $x = -40$  and  $x = 15$ . Discard the negative zero.

The width of the border is 15 cm.

The outside dimensions of the border are 60 cm by 50 cm.

PTS: 1

DIF: Average

OBJ: Section 4.2 NAT: RF 5

TOP: Factoring Quadratic Equations

KEY: roots of quadratic equation

Let  $x$  centimetres be the length of edging cut off.

The measures of the cut pieces of edging are  $20 - x$ ,  $41 - x$ , and  $44 - x$ .

Since they form a right triangle, use the Pythagorean theorem.

$$(44 - x)^2 = (20 - x)^2 + (41 - x)^2$$

$$1936 - 88x + x^2 = (400 - 40x + x^2) + (1681 - 82x + x^2)$$

$$x^2 - 34x + 145 = 0$$

Factor the trinomial to find the zeros of the quadratic relation.

$$x^2 - 34x + 145 = 0$$

$$(x - 29)(x - 5) = 0$$

The zeros are  $x = 29$  and  $x = 5$ .

Since the shortest piece of edging is less than 29 cm long, the amount to be cut off must be 5 cm.

The new rods are 15 cm, 36 cm, and 39 cm long.

PTS: 1

DIF: Average

OBJ: Section 4.2 NAT: RF 5

TOP: Factoring Quadratic Equations

KEY: factor trinomial

8. ANS:

Set  $h = 0$  and solve for  $d$ .

$$d = \frac{-24 \pm \sqrt{(24)^2 - 4(-5)(30)}}{2(-5)}$$

$$= \frac{-24 \pm \sqrt{576 + 600}}{-10}$$

$$= \frac{-24 \pm \sqrt{1176}}{-10}$$

$$d = -1.03 \text{ or } d = 5.83$$

