

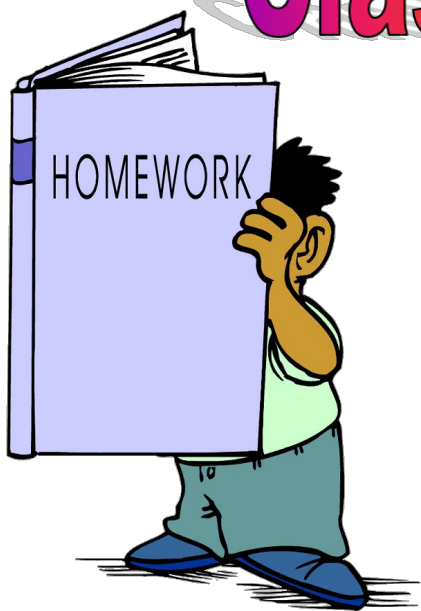
Curriculum Outcomes:

(SS1) Solve problems and justify the solution strategy using circle properties, including: the perpendicular from the centre of a circle to a chord bisects the chord; the measure of the central angle is equal to twice the measure of the inscribed angle subtended by the same arc; the inscribed angles subtended by the same arc are congruent; a tangent to a circle is perpendicular to the radius at the point of tangency.

Student Friendly:

How we can use the Chord properties to solve for unknown lengths. (Chord properties go hand and hand with Pythagorean theorem, angle sum of a triangle and isosceles triangles)

Class/Homework



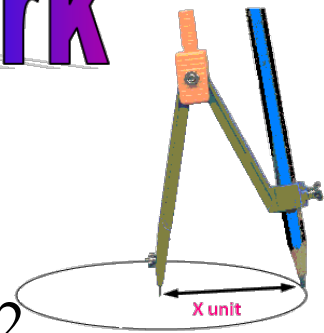
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Day 1

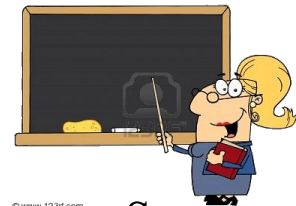
- 3 ab
- 4a
- 5abc sketch
- 6abc sketch
- 7ab sketch

Day 2

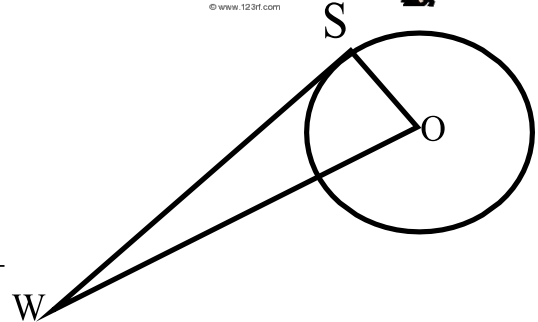
- 8
- 9
- 13
- 14
- 16 c
- 17
- 20 (try)



Warm Up



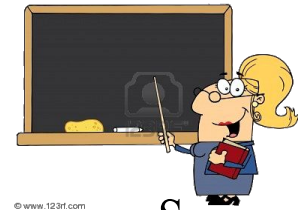
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Fill in the blanks

- 1) The Tangent is _____
- 2) The center is labeled with the letter _____
- 3) The point of tangency is labeled with the letter _____
- 4) The radius is the line _____
- 5) Find the length of the radius if $OW = 17$ and $SW = 9$

Warm Up



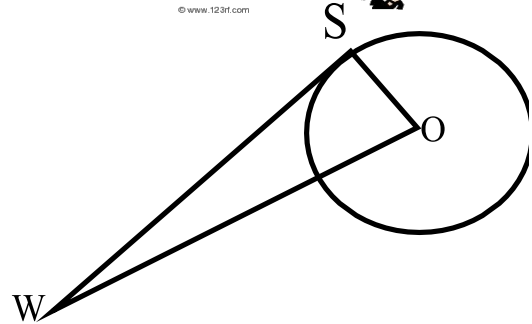
Fill in the blanks

1) The Tangent is sw

2) The center is labeled with the letter O

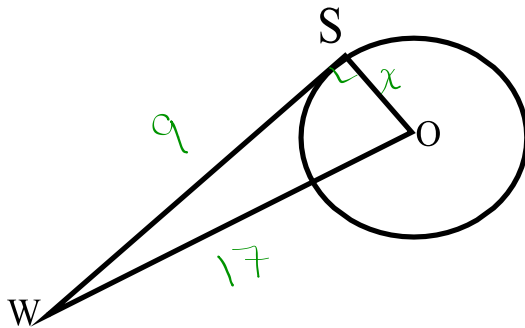
3) The point of tangency is labeled with the letter S

4) The radius is the line OS



SHOW YOUR WORK

5) Find the length of the radius if $OW = 17$ and $SW = 9$



[Redacted]

$OS \Rightarrow \text{radius} \Rightarrow \text{leg}$

[Redacted]

[Redacted]

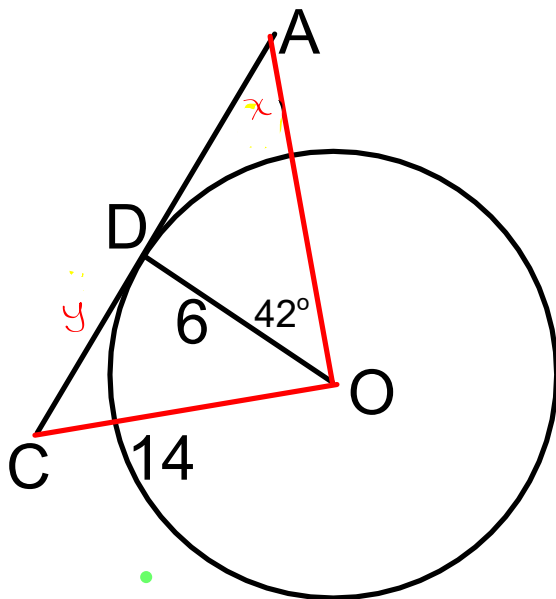
$$a^2 = 289 - 81$$

$$a^2 = 208$$

[Redacted]

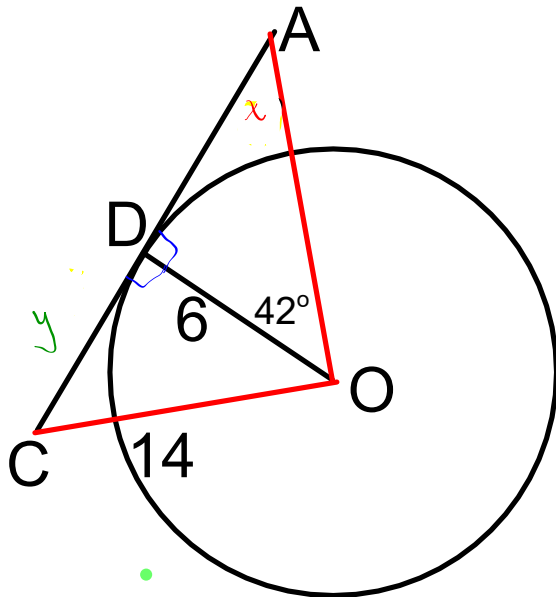
Warm Up

Determine the unknowns:



Warm Up

Determine the unknowns:



[Redacted]

[Redacted]

[Redacted]

[Redacted]

[Redacted]

[Redacted]

[Redacted]

[Redacted]

$a^2 = 196 - 36$

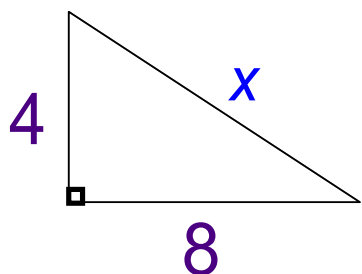
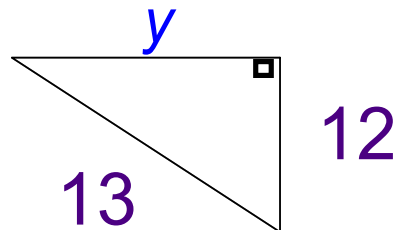
$a^2 = 160$

$a = 12.6$

[Redacted]

Calculating with Tangents We Only Use ...

1) Pythagorean Theorem

finding the hypotenuse $\rightarrow c^2 = a^2 + b^2$ finding a side $\rightarrow a^2 = c^2 - b^2$ 

or

2) Angle Sum of Triangle (SATT)

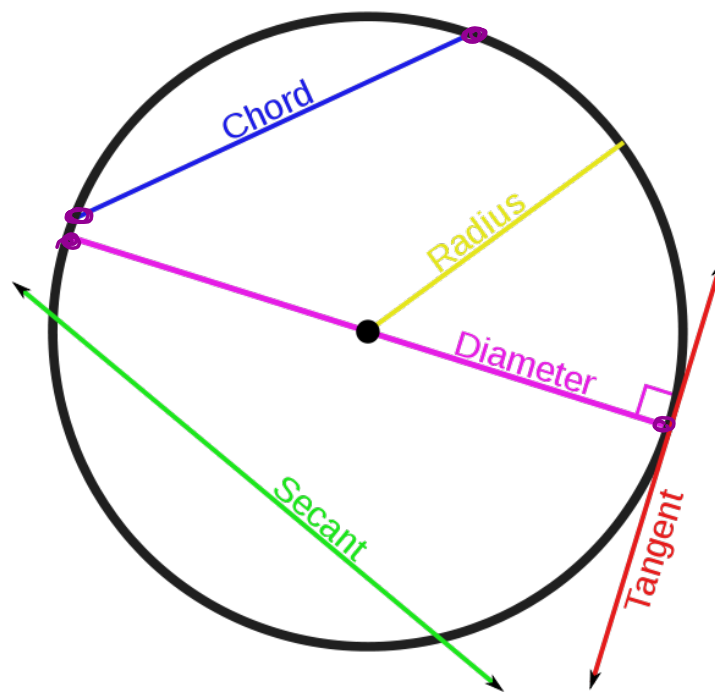
Unknown Angle = $180^\circ - 90^\circ - \text{known angle}$



Section 8.2

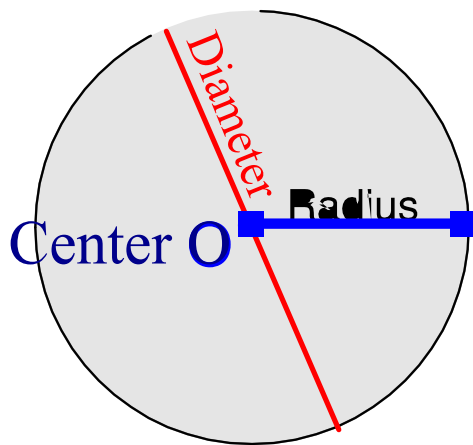


Properties of Chords in Circles



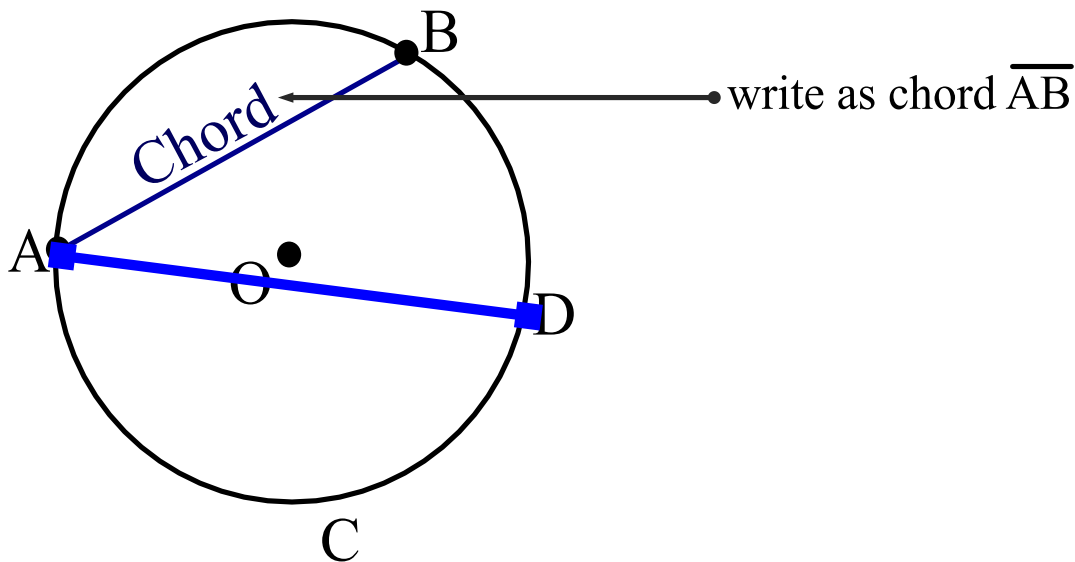
Properties of Circles & Terminology:

Circle - the set of all points that are equidistant from a fixed point.

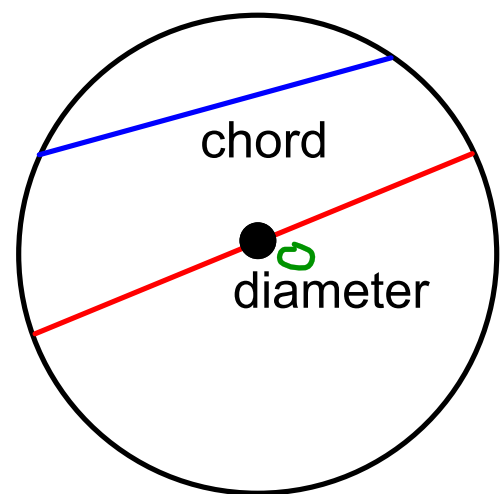


$$\text{radius} = \frac{1}{2} (\text{diameter})$$

$$\text{diameter} = 2 (\text{radius})$$



- A line segment that joins two points on a circle is a chord.
- A diameter of a circle is a chord through the centre of the circle. It's the longest Chord.



Perpendicular bisector:

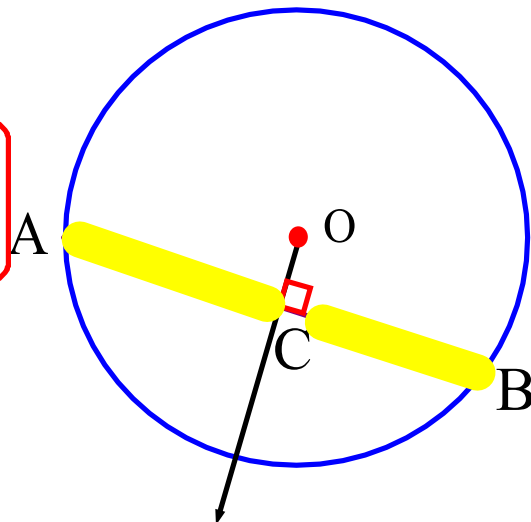
→ line that cuts a chord into two equal pieces at 90° angle

Chord Property 1

- A line drawn from the centre of a circle that is perpendicular to a chord bisects the chord. (It cuts the chord into two equal parts.)

If OC is perpendicular to AB

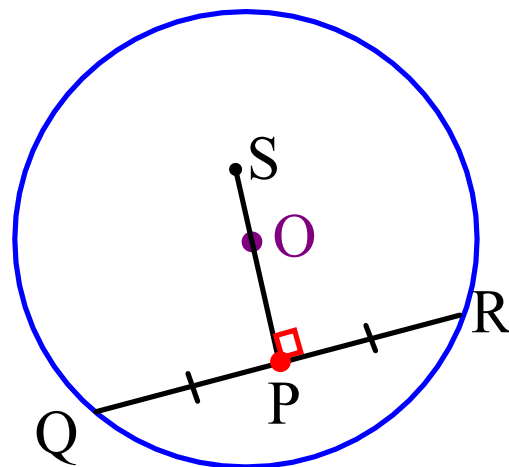
Then



Chord Property 2

- The perpendicular bisector of a chord in a circle passes through the centre of the circle.

A perpendicular bisector of a chord must go through the centre.

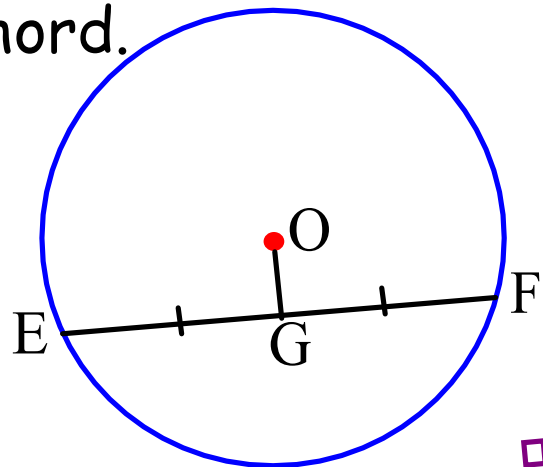


Perpendicular to a Chord Property 3

- A line that joins the centre of a circle and the midpoint of a chord is perpendicular to the chord.

If O is the centre and
 $EG = GF$, then

(Chord P3)



A line that comes from the centre of the circle and cuts the chord into two equal pieces is the perpendicular bisector

STOP!

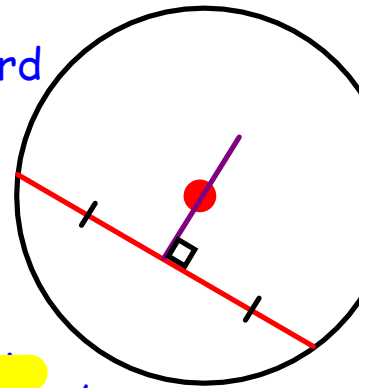


Yes!
We know
that a

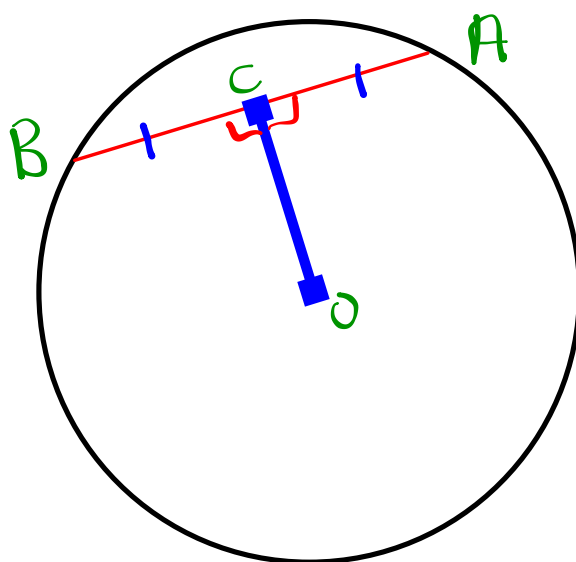
Aren't they
all saying the
same thing?



perpendicular bisector of a chord



hits the chord at a **right angle**,
the chord is cut in **two equal parts**,
and passes through the **center**.



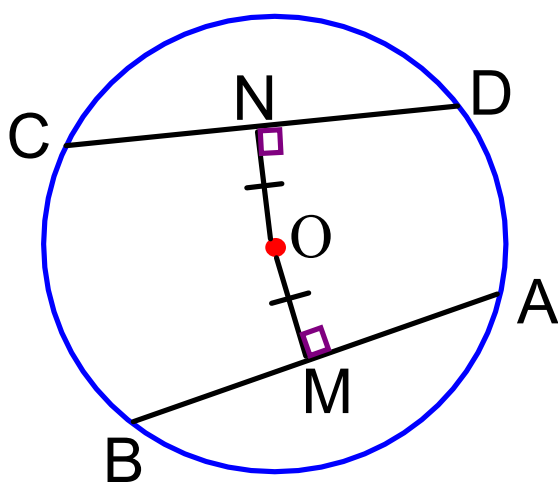
$$BC = CA \text{ (Chord PD)}$$

$$\angle OCA = 90^\circ \text{ (Chord P3)}$$

$$\angle OCB = 90^\circ$$

Perpendicular to a Chord Property 4

- Two chords that are equal distance from the center must be the same



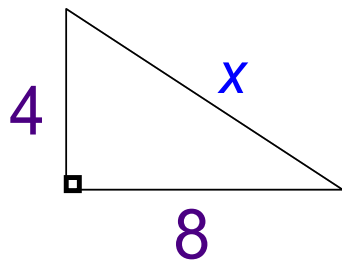
If $OM = ON$,
then $AB = CD$
OR
If $AB = CD$,
then $OM = ON$

Working With Chords Lengths We Only Use ...

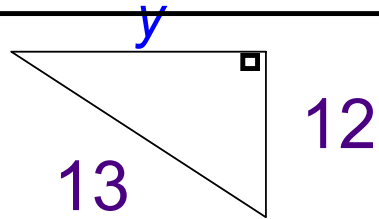
Note: the only reason they give you diameter is so you can use the radius

1) Pythagorean Theorem

finding the hypotenuse $\rightarrow c^2 = a^2 + b^2$



finding a side $\rightarrow a^2 = c^2 - b^2$



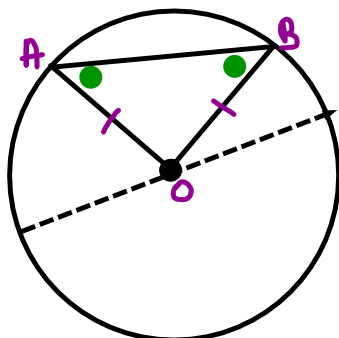
or

2) Angle Sum of Triangle (SATT)

Unknown Angle = $180^\circ - 90^\circ - \text{known angle}$

or

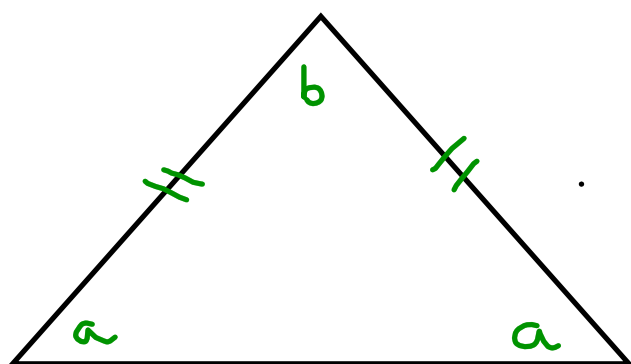
3) Isosceles Triangle (ITT)



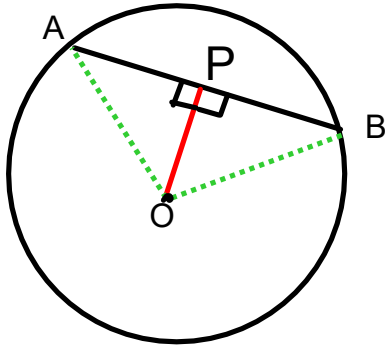
$OA=OB \Rightarrow$ radii

$\angle OAB = \angle OBA$ (Iso Δ)

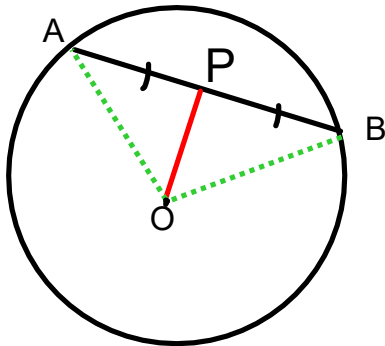
Itt



Chord Properties:

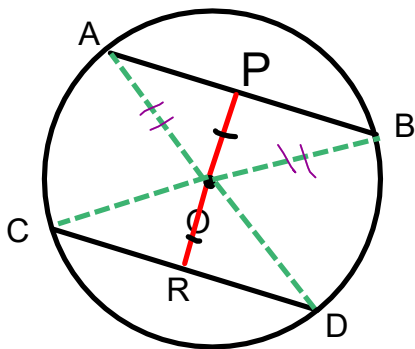


$$AP = PB \text{ (Chord P 1)}$$



$$\angle APO = 90^\circ \text{ (Chord P 3)}$$

$$\angle BPO = 90^\circ \text{ (Chord P 3)}$$



$$AB = CD \text{ (Chord P 4)}$$

To Solve use:

$$\text{Angle} = \underline{\quad}^\circ \text{ (SATT) or (ITT)}$$

$$\text{Side} = \underline{\quad} \text{ cm (Pythagorean theorem)}$$