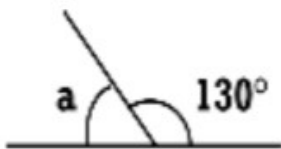


Curriculum Outcomes:

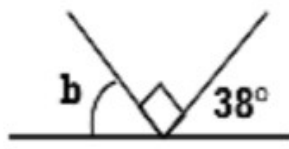
(SS1) Solve problems and justify the solution strategy using circle properties, including: the perpendicular from the centre of a circle to a chord bisects the chord; the measure of the central angle is equal to twice the measure of the inscribed angle subtended by the same arc; the inscribed angles subtended by the same arc are congruent; a tangent to a circle is perpendicular to the radius at the point of tangency.

Student Friendly:

How we can use the tangent properties to solve for unknown lengths. (Tangent properties go hand and hand with Pythagorean theorem)



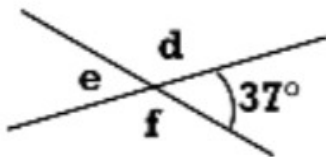
$a = 50^\circ$ (SAT)



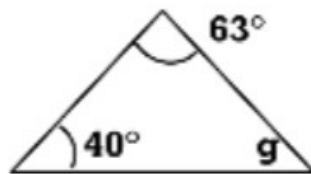
$b = 52^\circ$ (SAT)



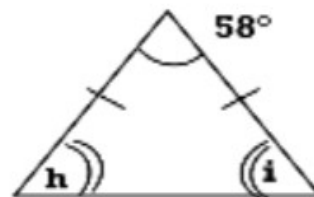
$c = 33^\circ$ (CyAT)



$e = 37^\circ$ (OAT)
 $d = 143^\circ$ (SAT)
 $f = 143^\circ$ (OAT)



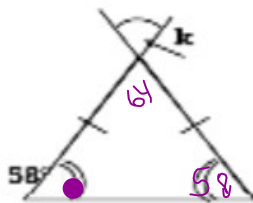
$g = 77^\circ$ (SATT)



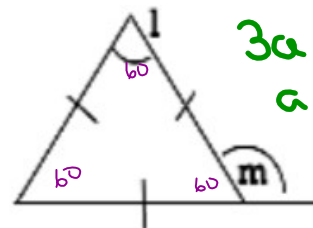
$h = i = 61^\circ$ (ITT)



$j = 133^\circ$ (EAT)
 or
 (SAT)

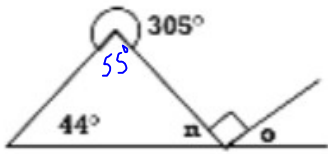


$k = 64^\circ$ (OAT)

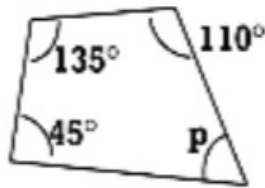


$3a = 180$
 $a = 60^\circ$

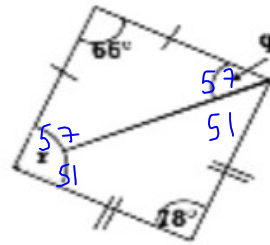
$l = 60^\circ$ (SATT)
 $m = 120^\circ$ (SAT or EAT)



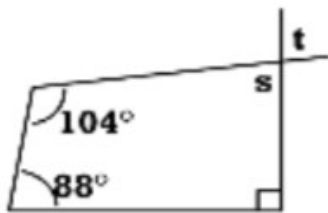
$n = 81^\circ$ (SATT)
 $o = 9^\circ$ (SAT)



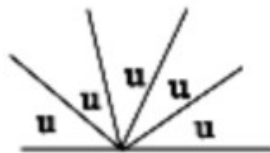
$p = 70^\circ$ (QuadT)



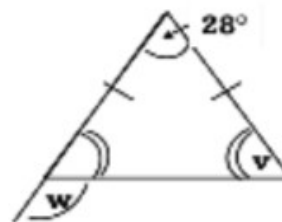
$q = 57^\circ$ (ITT)
 $x = 108^\circ$ (ITT)



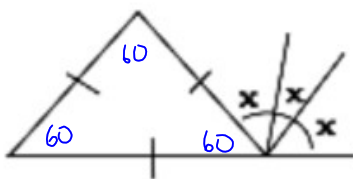
$s = 78^\circ$ (QuadT)
 $t = 78^\circ$ (OAT)



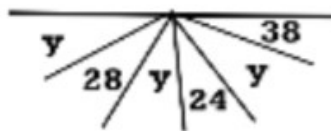
$5u = 180^\circ$ (SAT)
 $u = 36^\circ$



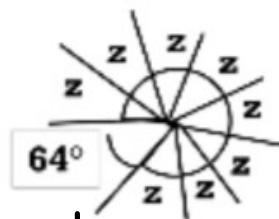
$v = 76^\circ$ (ITT)
 $w = 104^\circ$ (EAT)



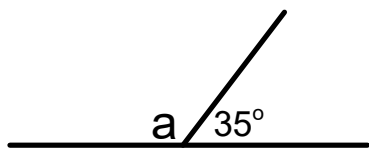
$3x = 120$ (EAT)
 $x = 40^\circ$



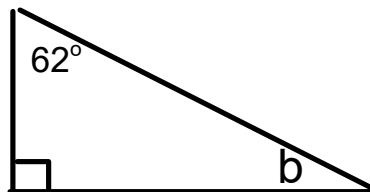
$3y + 28 + 38 = 180$ (SAT)
 $3y + 90 = 180$
 $3y = 90$
 $y = 30^\circ$



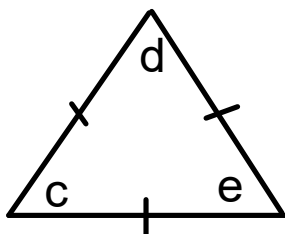
$8z + 64 = 360$ (CyAT)
 $8z = 296$
 $z = 37^\circ$



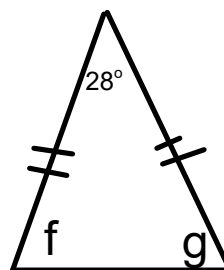
$y = 145^\circ$ (SAT)



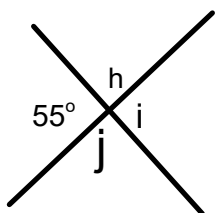
$b = 28^\circ$ (SATT)



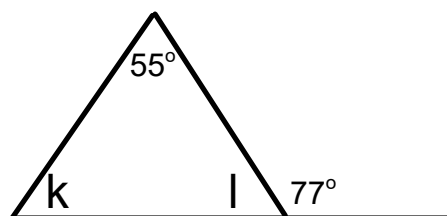
$c = d = e = 60$ (SATT)



$f = g = 76^\circ$ (ITT)

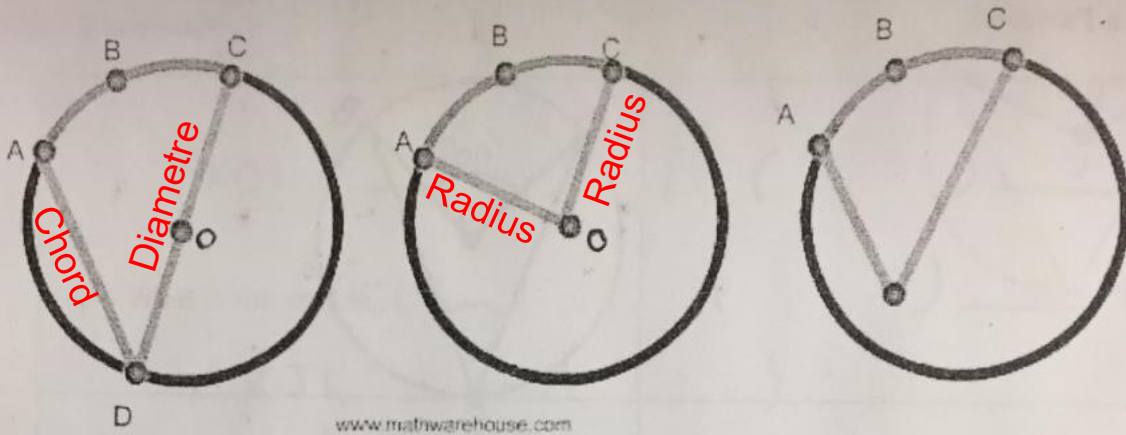


$i = 55^\circ$ (OAT)
 $h = 125^\circ$ (SAT)
 $j = 125^\circ$ (OAT)



$l = 103^\circ$ (SAT)
 $k = 22^\circ$ (SATT or EAT)

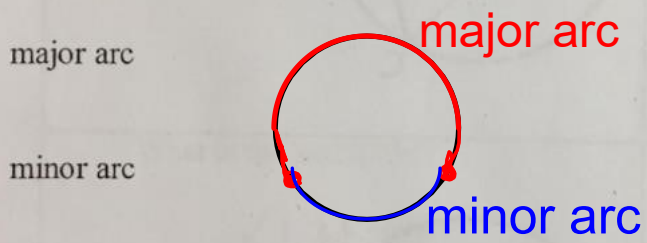
Inscribed and Central Angles in a Circle



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Vocabulary : (Your own words)

chord:
 - found inside a circle
 - line coming from the center of the circle hits the chord at 90 degrees and cuts it into two equal pieces



major arc

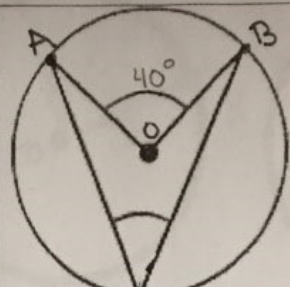
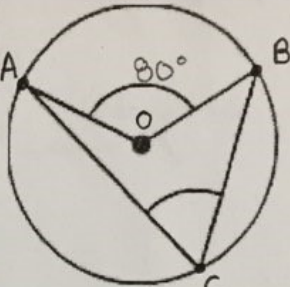
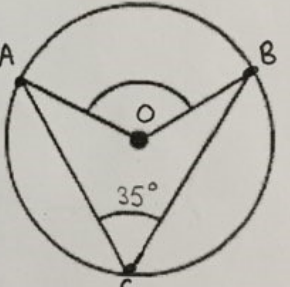
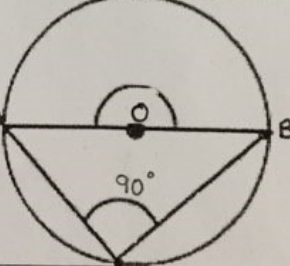
minor arc

tangent
 - found outside a circle
 - touches a circle at one point (at the point of tangency)
 - the radius hits the tangent at 90 degrees

inscribed angle
 - made up of two chords
 - half the central angle
 - equal to other inscribed angles coming from the same arc

central angle
 - made up of two radii (goes to the centre)
 - double the inscribed angle

Discover a Pattern

$\angle AOB = \underline{40^\circ}$ (cent) $\angle ACB = \underline{20^\circ}$ (ins/cent>, AB)	
$\angle AOB = \underline{80^\circ}$ (cent) $\angle ACB = \underline{40^\circ}$ (ins/cent>, AB)	
$\angle AOB = \underline{70^\circ}$ (ins/cent>, AB) $\angle ACB = \underline{35^\circ}$ (ins)	
$\angle AOB = \underline{180^\circ}$ (ins/cent>, AB) $\angle ACB = \underline{90^\circ}$ (ins)	

What is the relationship between central and inscribed angle?

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The central angle is double the inscribed angle

The inscribed angle is half the central angle

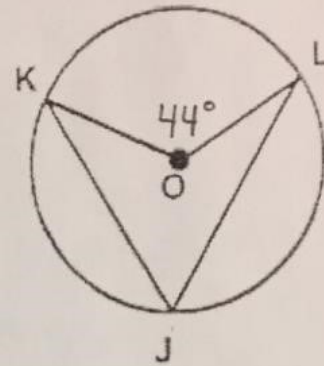
Model Problems

1)

$$\angle KOH = \underline{44^\circ} \text{ (cent)}$$

What is the $m\angle KJL$?

$$\angle KJL = \underline{22^\circ} \text{ (ins/cent, } \widehat{KL})$$

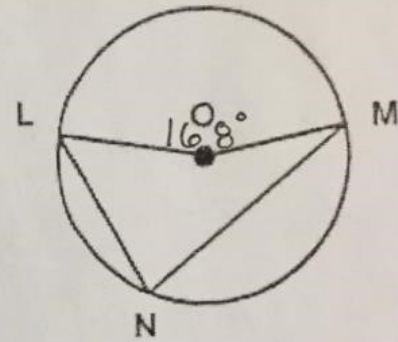


2)

$$\angle LOM = \underline{168^\circ} \text{ (cent)}$$

What is the $m\angle LNM$?

$$\angle LNM = \underline{84^\circ} \text{ (ins/cent, } \widehat{LM})$$

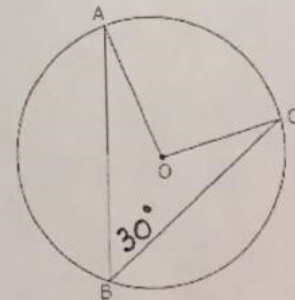


3)

$$\angle ABC = \underline{30^\circ} \text{ (ins)}$$

then

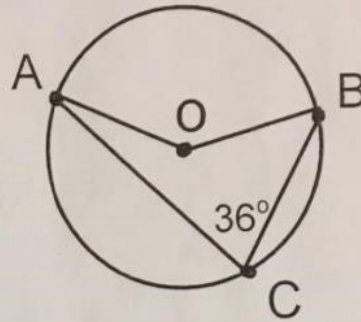
$$\angle AOC = \underline{60^\circ} \text{ (ins/cent, } \widehat{AC})$$



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$\angle ACB = \underline{36^\circ}$ (ins)

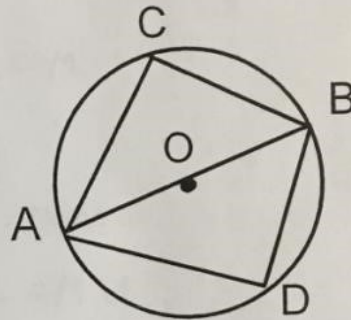
$\angle AOB = \underline{72^\circ}$ (Ins/cent, \widehat{AB})



$\angle AOB = \underline{180^\circ}$ (Diametre)

$\angle ACB = \underline{90^\circ}$ (Ins>, Diam)

$\angle ADB = \underline{90^\circ}$ (Ins>, Diam)



$\angle BAC = \underline{125^\circ}$ (CyQuad)

$\angle ACD = \underline{112^\circ}$ (CyQuad)

$\angle ABD = \underline{68^\circ}$ (CyQuad)

$\angle BDC = \underline{55^\circ}$ (CyQuad)

