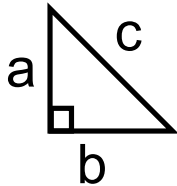


## Chapter 8: Notes

### Pythagorean theorem

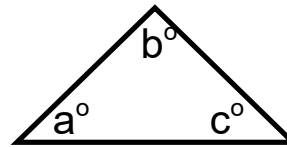


Hyp = ?  
 $c^2 = a^2 + b^2$

Leg = ?  
 $a^2 = c^2 - b^2$

### Angle Sum of Triangle Theorem

**(SATT)**

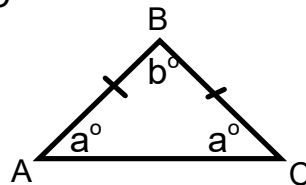


$$a^\circ + b^\circ + c^\circ = 180^\circ$$

### Isosceles Triangle Theorem **(ITT)**

Two sides are equal :  $AB = BC$

Base angles are equal:  
 $\angle A = \angle C$



If  $a^\circ = ?$

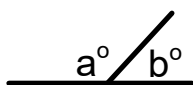
$$a^\circ = \frac{180 - b}{2}$$

If  $b^\circ = ?$

$$b^\circ = 180 - a^\circ - a^\circ$$

### Angle Properties

#### Supplementary Angle Theorem **(SAT)**



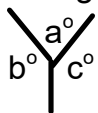
$$a^\circ + b^\circ = 180^\circ$$

#### Complimentary Angle Theorem **(CAT)**



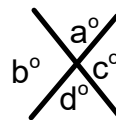
$$a^\circ + b^\circ = 90^\circ$$

#### Cyclic Angle Theorem **(CyAT)**



$$a^\circ + b^\circ + c^\circ = 360^\circ$$

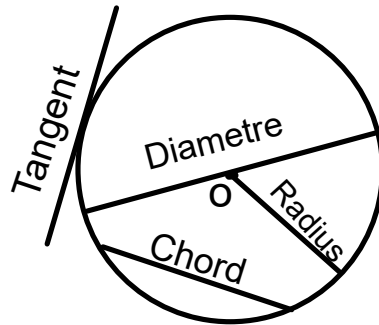
#### Opposite Angle Theorem **(OAT)**



$$a^\circ = d^\circ$$

$$b^\circ = c^\circ$$

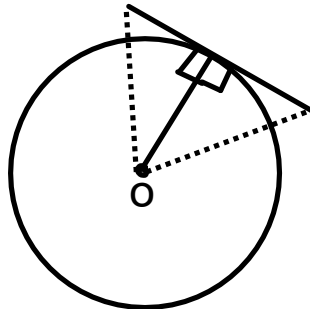
### Information about circles



### Tangent Property

$$\angle \text{---} = 90^\circ \text{ (Tang P)}$$

- a radius hits a tangent at  $90^\circ$



To solve unknown sides :  
Pythagorean Theorem

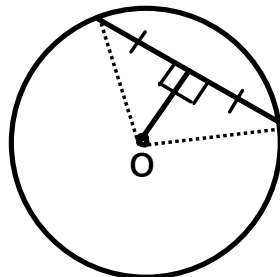
To solve unknown angles :  
SATT

### Chord Property

$$\text{If chord lengths are indicated} \\ \angle \text{---} = \angle \text{---} = 90^\circ \text{ (Chord P)}$$

a line coming from the centre of the circle

- hits chord at a  $90^\circ$  angle
- cuts the chord into two equal pieces



$$\text{If } 90^\circ \text{ is indicated} \\ \text{---} = \text{---} \text{ (Chord P)}$$

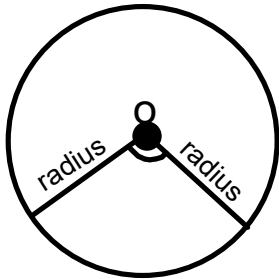
To solve unknown sides :  
Pythagorean Theorem

To solve unknown angles :  
SATT  
ITT

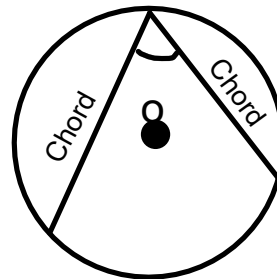
$$\text{Identify radii} \\ \text{---} = \text{---} = \text{---} \text{ (Radii)}$$

# Circle Properties

## Central Angle

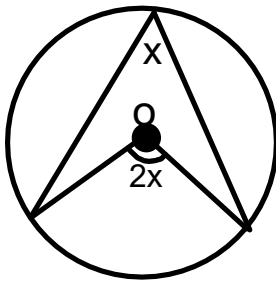


## Inscribed Angle



### Property # 1: Central & Inscribed Angles

$$\angle \text{___} = \text{___}^\circ \text{ ( ins/cent } \angle \text{, } \overset{\frown}{\text{___}})$$

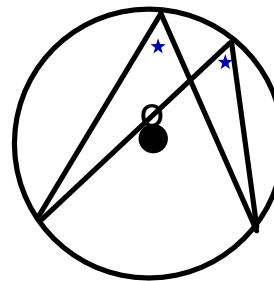


- The central angle is double the inscribed angle

- The inscribed angle is half the central angle

### Property # 2: Inscribed Angles

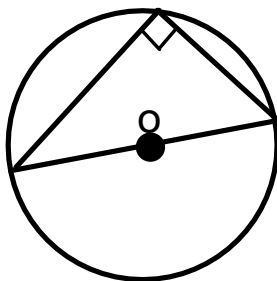
$$\angle \text{___} = \text{___}^\circ \text{ ( ins } \angle \text{, } \overset{\frown}{\text{___}})$$



- Inscribed angles coming from the same arc are equal

### Property # 3: Inscribed from Diameter

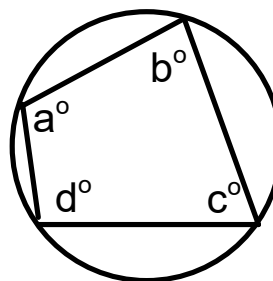
$$\angle \text{___} = \text{___}^\circ \text{ ( ins } \angle \text{, diam)}$$



- Inscribed angles coming from the diameter are  $90^\circ$

### Property # 4: Cyclic Quadrilateral

$$\angle \text{___} = \text{___}^\circ \text{ (CyQuad)}$$



- Opposite angles in a cyclic quad must add up to  $180^\circ$

$$a^\circ + c^\circ = 180^\circ$$

$$b^\circ + d^\circ = 180^\circ$$

<p>(SATT) (ITT) (SAT) (CAT) (OAT) (CyAT)</p>	<p><math>\angle \text{---} = 90^\circ</math> (Tang P)   <math>\angle \text{---} = \angle \text{---} = 90^\circ</math> (Chord P)   <math>\text{---} = \text{---}</math> (Chord P)   <math>\text{---} = \text{---} = \text{---}</math> (Radii)</p>	<p><math>\angle \text{---} = \text{---}^\circ</math> ( ins/cent &gt;, <math>\widehat{\text{---}}</math>)   <math>\angle \text{---} = \text{---}^\circ</math> ( ins &gt;, <math>\widehat{\text{---}}</math>)   <math>\angle \text{---} = \text{---}^\circ</math> ( ins &gt;, diam)   <math>\angle \text{---} = \text{---}^\circ</math> (CyQuad)</p>
--	--	--