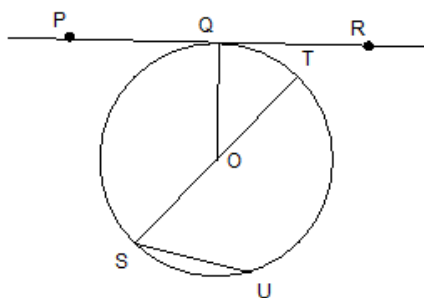


Section 8.1 & 8.2 Review

Multiple Choice

Identify the choice that best completes the statement or answers the question.

- 1. O is the centre of this circle.
Which line is a tangent?



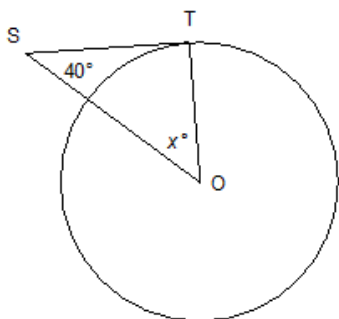
a. OQ

b. ST

c. PR

d. SU

2. O is the centre of this circle and point T is a point of tangency.
Determine the value of x° .



$$\left[\begin{array}{l} \angle OTS = 90^\circ \text{ (Tang P)} \\ x^\circ = 50^\circ \text{ (SATT)} \end{array} \right.$$

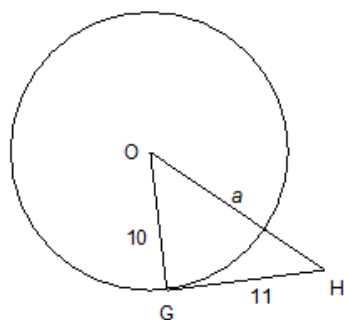
a. 90°

b. 50°

c. 130°

d. 40°

3. O is the centre of this circle and point G is a point of tangency.
Determine the value of a . If necessary, give your answer to the nearest tenth.



a. 11.3

b. 22.5

c. 4.6

d. 14.9

$$\angle OGH = 90^\circ \text{ (Tang P)}$$

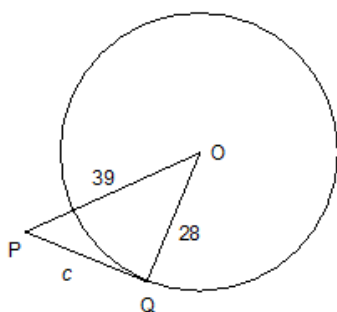
$$a \Rightarrow \text{hyp}$$

$$c^2 = a^2 + b^2$$

$$c^2 = 11^2 + 10^2$$

$$c = 14.9$$

4. O is the centre of this circle and point Q is a point of tangency.
Determine the value of c . If necessary, give your answer to the nearest tenth.



$$\angle OQP = 90^\circ (\text{Tang P})$$

$$c \Rightarrow \text{leg} \quad a^2 = c^2 - b^2$$

$$a^2 = 39^2 - 28^2$$

$$a = 27.1$$



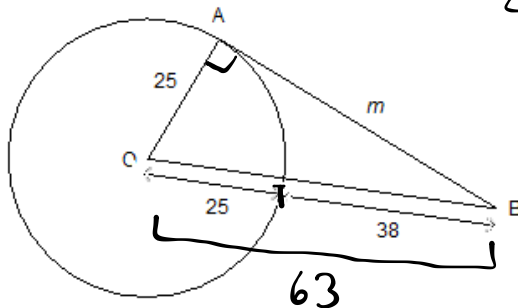
a. 48

b. 27.1

c. 11

d. 5.5

5. O is the centre of this circle and point A is a point of tangency.
Determine the value of m . If necessary, give your answer to the nearest tenth.



$$\angle OAB = 90^\circ \text{ (Tang P)}$$

$m \Rightarrow \text{leg}$

$$a^2 = c^2 - a^2$$

$$a^2 = 63^2 - 25^2$$

$$a = 57.8$$

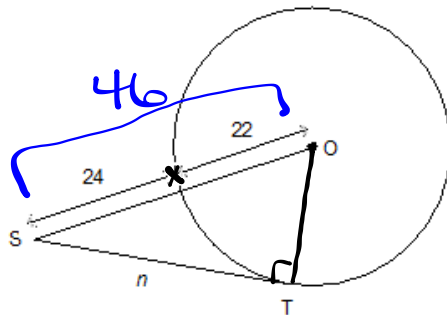
a. 38

b. 7.2

c. 67.8

d. 57.8

-6. O is the centre of this circle and point T is a point of tangency.
Determine the value of n . If necessary, give your answer to the nearest tenth.



a. 5.7

b. 51

c. 24

d. 40.4 $a = 40.4$

$$OT = OX = 22 \text{ (radii)}$$

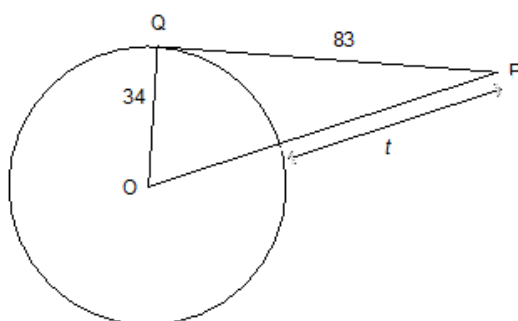
$$\angle OTS = 90^\circ \text{ (Tang P)}$$

$$n \Rightarrow \text{leg } a^2 = c^2 - b^2$$

$$a^2 = 46^2 - 22^2$$

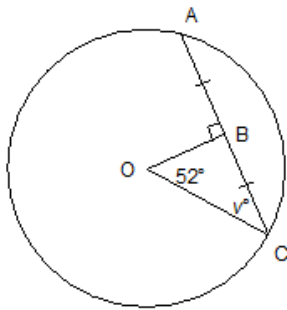
$$\boxed{d. 40.4} \quad a = 40.4$$

7. O is the centre of this circle and point Q is a point of tangency. Determine the value of t . If necessary, give your answer to the nearest tenth.



- a. 61.3 b. 55.7 c. 55 d. 82.2

8. O is the centre of the circle.
Determine the value of v° .



a. 19°

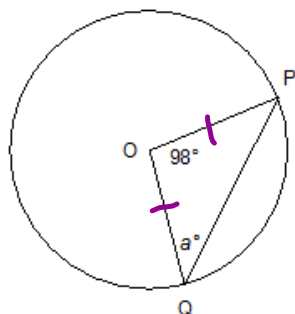
b. 71°

c. 52°

d. 38°

$$\begin{aligned} \angle OBC &= \angle OBA = 90^\circ \text{ (ChP)} \\ AB &= BC = \# \text{ (ChP)} \\ OC &= OA \text{ (radii)} \\ \boxed{y} &= 38^\circ \text{ (SA } \perp \text{)} \end{aligned}$$

9. O is the centre of the circle.
Determine the value of a° .



a. 49°

b. 20.5°

c. 41°

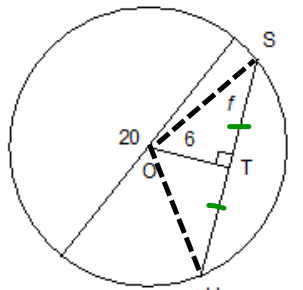
d. 69.5°

$$OP = OQ \text{ (radii)}$$

$$a^\circ = \frac{180 - 98}{2}$$

$$a^\circ = 41^\circ \text{ (I b t)}$$

10. O is the centre of the circle.
Determine the value of f to the nearest tenth, if necessary.



a.

4

b. 8

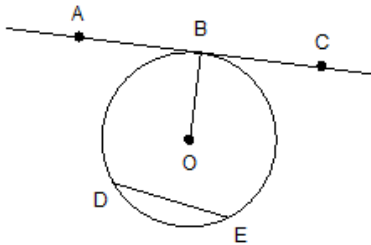
c. 64

d. 11.7

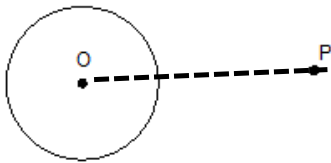
$$\begin{aligned}
 OU = OS &= 10 \text{ (radii)} \\
 \angle OTS = \angle OTU &= 90^\circ \text{ (chP)} \\
 UT = ST &= \text{---} \text{ (chP)} \\
 \begin{array}{c} \text{6} \\ \text{10} \\ \text{X} \end{array} & \quad \begin{aligned} a^2 &= c^2 - b^2 \\ a^2 &= 10^2 - 6^2 \\ a &= 8 \end{aligned}
 \end{aligned}$$

Short Answer

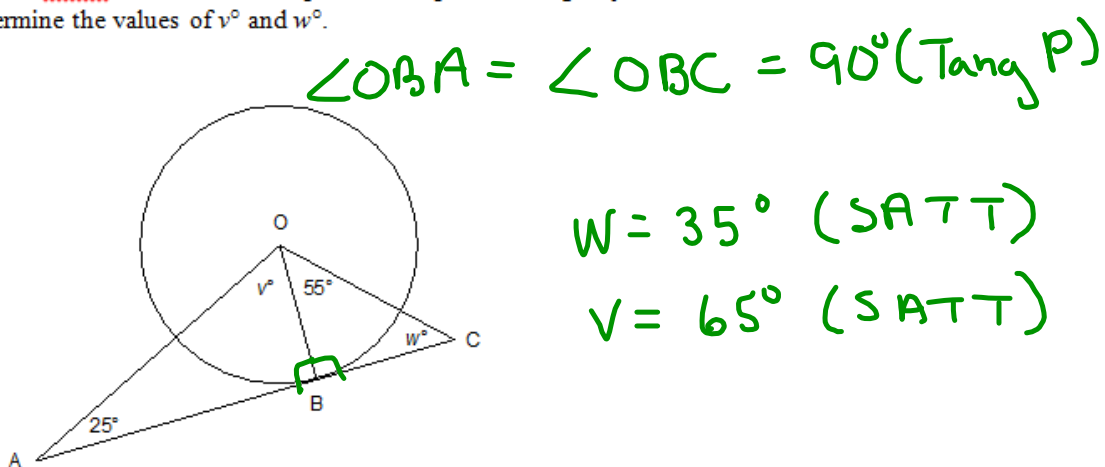
11. O is the centre of this circle.
Which line is a tangent?



12. Draw a line through point P that is NOT a tangent to the circle.

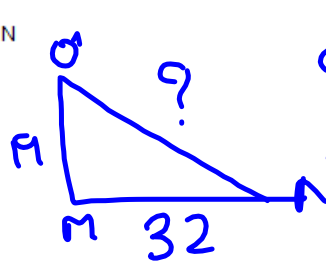
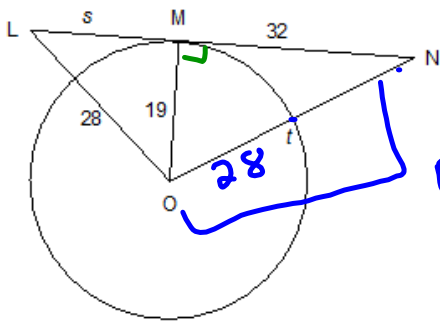


13. O is the centre of this circle and point B is a point of tangency.
Determine the values of v° and w° .



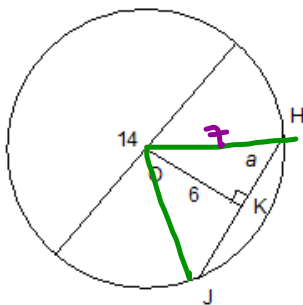
14. O is the centre of this circle and point Q is a point of tangency.
 Determine the values of s and t . If necessary, give your answers to the nearest tenth.

$\angle OML = \angle OMN = 90^\circ$ (tang^P)



$c^2 = a^2 + b^2$

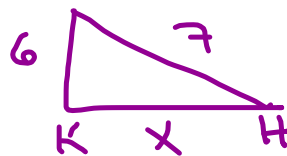
15. Point O is the centre of this circle. Without solving for a , sketch and label the length of any extra line segments you need to draw to determine the value of a .



$$OH = OJ = 7 \text{ (radii)}$$

$$\angle OKH = \angle OKJ = 90^\circ \text{ (chP)}$$

$$HK = JK = \text{---} \text{ (chP)}$$



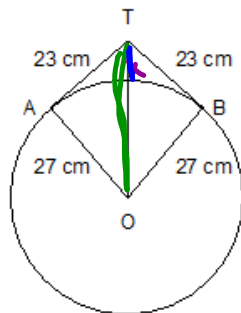
$$a^2 = c^2 - b^2$$

$$a^2 = 7^2 - 6^2$$

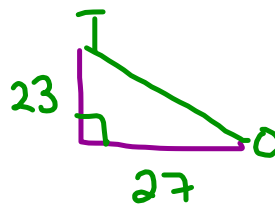
$$a^2 = 49 - 36$$

Problem

16. A circular mirror with radius 27 cm hangs from a hook. The wire is 46 cm long and is a tangent to the circle at points A and B. How far, to the nearest tenth, above the top of the mirror is the hook?



$$\angle OBT = \angle OAT = 90^\circ \text{ (Tang)} \text{ } \textcircled{P}$$



$$c^2 = a^2 + b^2$$

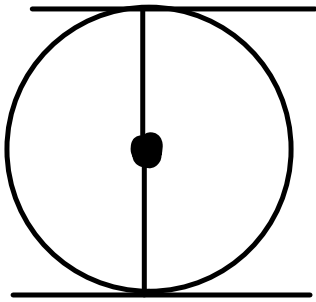
$$c^2 = 27^2 + 23^2$$

$$c = 35.5$$

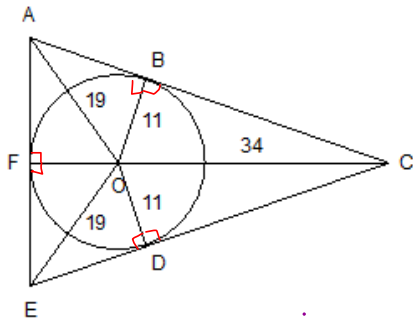
$$x = 35.5 - 27$$

$$x = 12.6$$

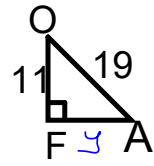
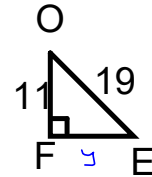
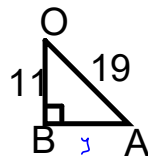
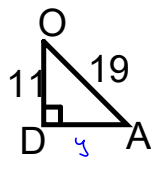
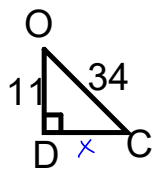
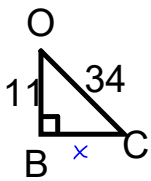
17. When are two tangent lines to a circle parallel?
Draw a sketch to support your answer.



18. AC, AE, and CE are tangents to this circle. The points of tangency are: B, F, and D. The circle has radius 11. The distance from the centre of the circle to each vertex of the triangle is: $OC = 34$, $OA = OE = 19$. Determine the side lengths of $\triangle ACE$, to the nearest tenth.



- $\angle OBC = 90^\circ$ (Tang P)
- $\angle OBA = 90^\circ$ (Tang P)
- $\angle ODC = 90^\circ$ (Tang P)
- $\angle ODE = 90^\circ$ (Tang P)
- $\angle OFA = 90^\circ$ (Tang P)
- $\angle OFE = 90^\circ$ (Tang P)



$$a^2 = c^2 - b^2$$

$$a^2 = 34^2 - 11^2$$

$$a^2 = 1156 - 121$$

$$a^2 = 1035$$

$$a = \sqrt{1035}$$

$$a = 32.2$$

$$a^2 = c^2 - b^2$$

$$a^2 = 19^2 - 11^2$$

$$a^2 = 361 - 121$$

$$a^2 = 240$$

$$a = \sqrt{240}$$

$$a = 15.5$$

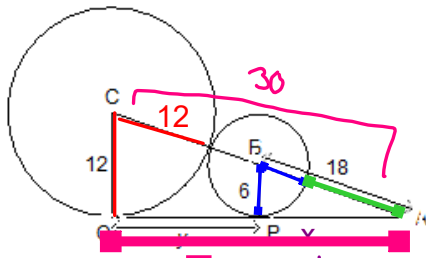
$$AC = 32.2 + 15.5 = 47.7$$

$$AE = 15.5 + 15.5 = 31$$

$$EC = 32.2 + 15.5 = \underline{47.7}$$

$$\underline{126.4}$$

19. AQ is a tangent to the circle with centre B and to the circle with centre C. The points of tangency are P and Q. Determine the value of y to the nearest tenth.



$\angle OQA = 90^\circ$ (Tang P)

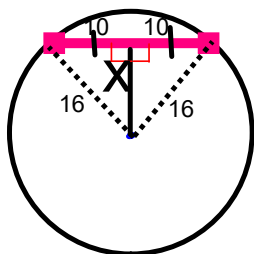
$\angle BPA = 90^\circ$ (Tang P)

$$\begin{aligned}
 a^2 &= c^2 - b^2 \\
 a^2 &= 30^2 - 12^2 \\
 a^2 &= 900 - 144 \\
 \sqrt{a^2} &= \sqrt{756} \\
 a &= 27.5
 \end{aligned}$$

$$\begin{aligned}
 a^2 &= c^2 - b^2 \\
 a^2 &= 18^2 - 6^2 \\
 a^2 &= 324 - 36 \\
 a^2 &= 288 \\
 a &= \sqrt{288} \\
 a &= 16.97 \rightarrow 17
 \end{aligned}$$

$$\begin{aligned}
 y &= z - x \\
 y &= 27.5 - 17 \\
 y &= 10.5
 \end{aligned}$$

20. A circle has diameter 32 cm. How far from the centre of the circle, to the nearest centimetre, is a chord 20 cm long?



$$\begin{aligned}x &\Rightarrow a^2 = c^2 - b^2 \\a^2 &= 16^2 - 10^2 \\a^2 &= 256 - 100 \\a^2 &= 156 \\a &= \sqrt{156} \\a &= 12.5 \\&= 13\text{ cm}\end{aligned}$$