

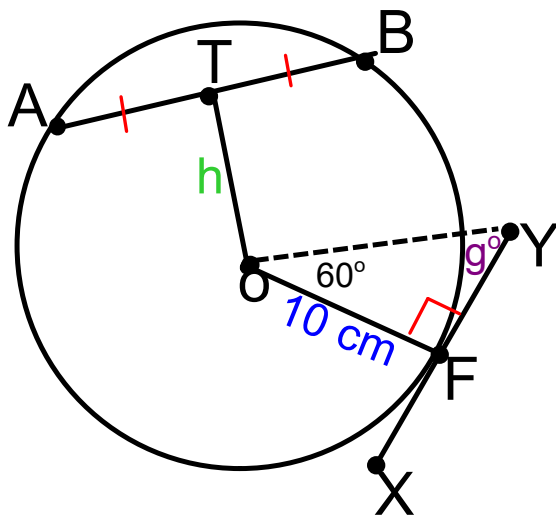
Curriculum Outcomes:

(SS1) Solve problems and justify the solution strategy using circle properties, including: the perpendicular from the centre of a circle to a chord bisects the chord; the measure of the central angle is equal to twice the measure of the inscribed angle subtended by the same arc; the inscribed angles subtended by the same arc are congruent; a tangent to a circle is perpendicular to the radius at the point of tangency.

Student Friendly:

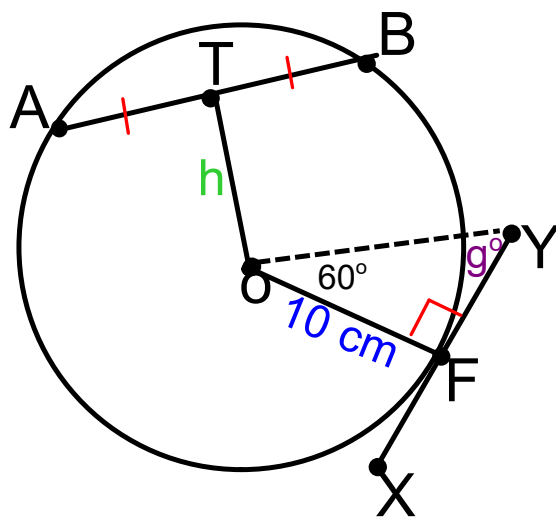
How angles found at the centre of a circle are related to angles formed by two chords found inside the circle.

Warm Up



If AB is 16 cm, calculate the length of OT and the $\angle OYF$.

Warm Up



If AB is 16 cm, calculate the length of OT and the $\angle OYF$.

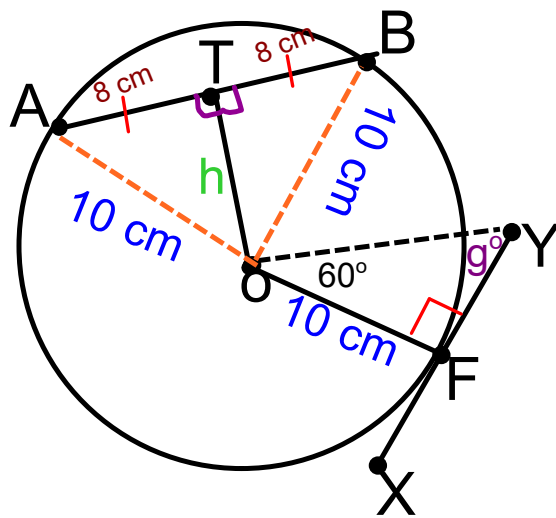
$$\angle OFY = 90^\circ \text{ (Tang P)}$$

$$g^\circ = \angle OYF = 180^\circ - 90^\circ - 30^\circ$$

$$g^\circ = \angle OYF = 30^\circ \text{ (SATT)}$$



Warm Up



If AB is 16 cm, calculate the length of **OT** and the $\angle OYF$.

$$AT = BT = 8 \text{ cm (given/Chord)}$$

$$\angle OTB = \angle OTA = 90^\circ \text{ (Chord P)}$$

$$OF = 6 \text{ cm (radius)}$$

$$OA = 6 \text{ cm (radius)}$$

$$OB = 6 \text{ cm (radius)}$$

OT \Rightarrow leg

$$a^2 = c^2 - b^2$$

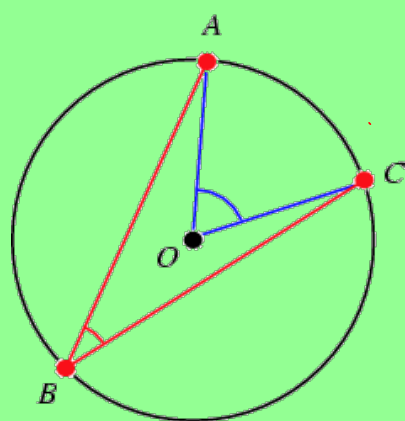
$$a^2 = 10^2 - 8^2$$

$$a^2 = 100 - 64$$

$$a^2 = 36$$

$$a = \sqrt{36}$$

$$a = 6$$



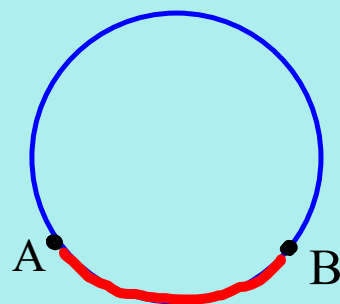
Section 8.3

Properties of Angles in Circles



- The longer arc AB is the major arc.

- The shorter arc AB is the minor arc.



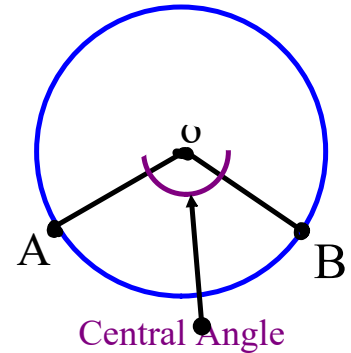
arc \widehat{AB}



Central Angle:

The angle formed by joining the endpoints of a arc to the centre of a circle
(Made with 2 radii)

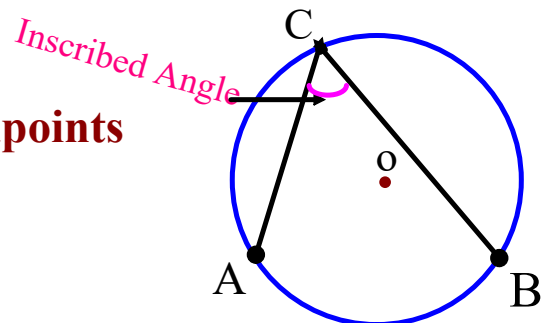
$\angle AOB$



Inscribed Angle:

The angle formed by joining the endpoints of a arc to a point on the circle
(Made with two chords)

$\angle ACB$



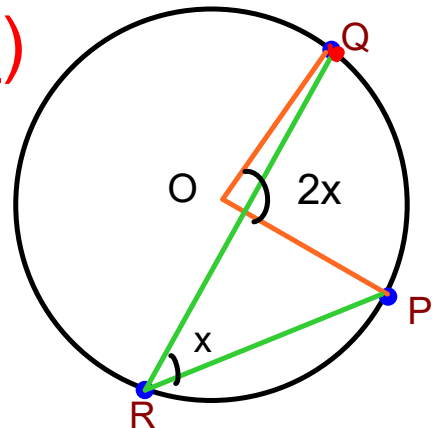
Inscribed and central angles are **SUBTENDED** by the **MINOR** arc

come from the same 'smaller arc'

Central Angle & Inscribed Angle Property

Property 1: (Ins/Cent <, \frown)

In a circle, the measure of a **central angle** coming from an arc is **TWICE** the measure of an **inscribed angle** coming from the same arc.



$$\angle POQ = 2 \angle PRQ$$

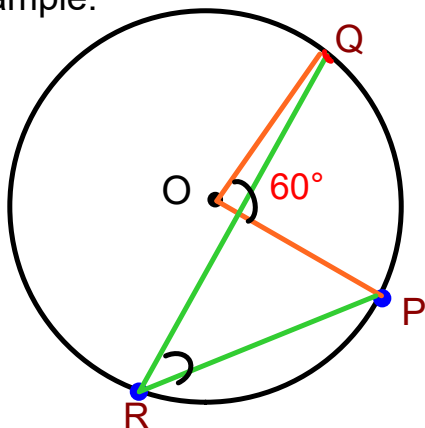
Central angle is twice the inscribed angle

or

$$\angle PRQ = \frac{1}{2} \angle POQ$$

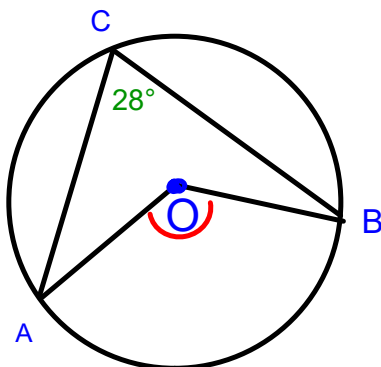
Inscribed angle is half the center angle

Example:



$$\angle QOP = 60^\circ \text{ (given/central)}$$

$$\angle QRP = 30^\circ \text{ (inc/cent } \angle, \widehat{QP})$$



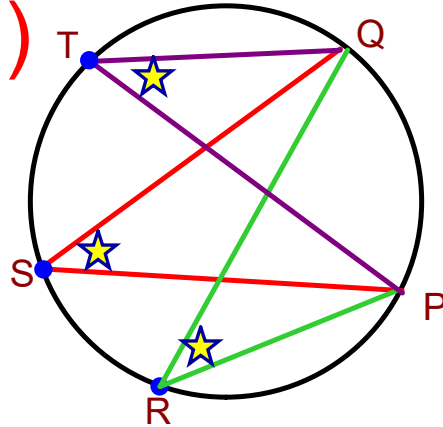
$$\angle ACB = 28^\circ \text{ (given/inc)}$$

$$\angle AOB = 56^\circ \text{ (inc/cent } \angle, \widehat{AB})$$

Inscribed Angle Property

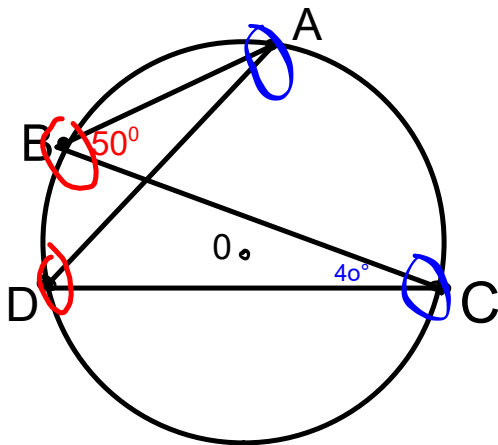
Property 2: (Ins<, $\widehat{\quad}$)

In a circle, all inscribed angles **coming from** the same arc are equal.



$$\angle PTQ = \angle PSQ = \angle PRQ$$

Example:



$$\angle ABC = 50^\circ \text{ (given/ ins)}$$

$$\angle ADC = 50^\circ \text{ (ins } \angle, \widehat{AC})$$

$$\angle BCD = 40^\circ \text{ (given/ ins)}$$

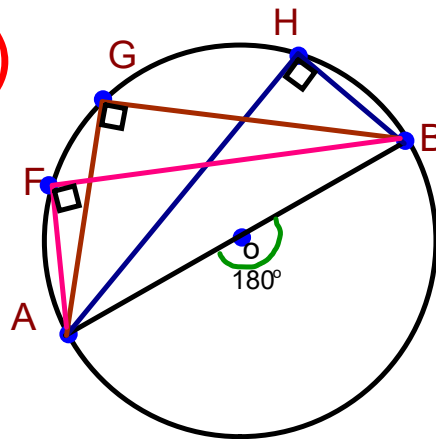
$$\angle BAD = 40^\circ \text{ (ins } \angle, \widehat{BD})$$



Angles is a Semicircle Property

Property 3: (Inc \angle , diam)

All inscribed angles subtended by a semicircle (diameter) are right angles



Makes sense

Inscribed angles are always half the centre

Center Angle = 180° (Straight Line)

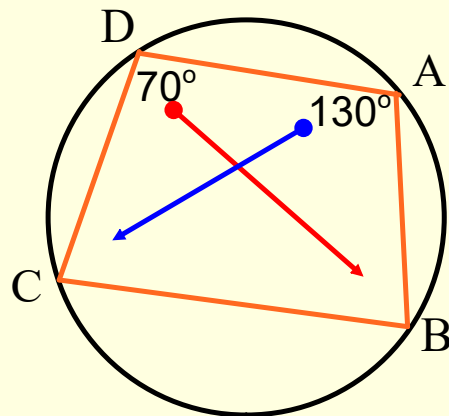
Inscribed angle is half the Central Angle

$$\begin{aligned} \text{Inscribed} &= (1/2) \text{ central} \\ &= (1/2) 180^\circ \\ &= 90^\circ \end{aligned}$$

Cyclic Quadrilateral Angle Properties:

Property 4: (Cy Quad)

__ The opposite angles of an inscribed **quadrilateral** are supplementary.
(add up to 180°)



$$\angle A + \angle C = 180^\circ$$

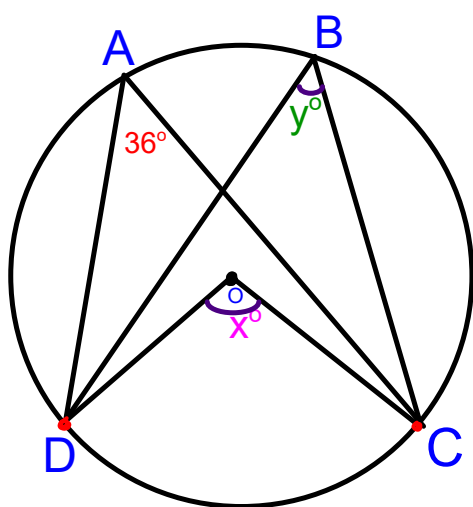
$$\angle B + \angle D = 180^\circ$$

$$\angle C = 50^\circ \text{ (Cy Quad)}$$

$$\angle B = 110^\circ \text{ (Cy Quad)}$$

Ever thing you have learned

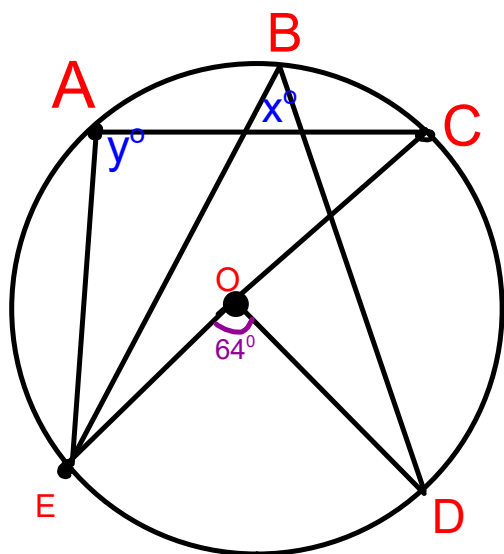
Angle Properties	Tangent & Chord Properties	Circle Properties
(SATT)	$\angle \text{---} = 90^\circ$ (Tang P)	$\angle \text{---} = \text{---}^\circ$ (ins/cent >, $\widehat{\text{---}}$)
(ITT)		
(SAT)	$\angle \text{---} = \angle \text{---} = 90^\circ$ (Chord P)	$\angle \text{---} = \text{---}^\circ$ (ins >, $\widehat{\text{---}}$)
(CAT)		
(OAT)	$\text{---} = \text{---}$ (Chord P)	$\angle \text{---} = \text{---}^\circ$ (ins >, diam)
(CyAT)		
(EAT)	$\text{---} = \text{---} = \text{---}$ (Radii)	$\angle \text{---} = \text{---}^\circ$ (CyQuad)



$$\angle DAC = 36^\circ \text{ (given/inc)}$$

$$y^\circ \angle DBC = 36^\circ \text{ (inc } \angle, \widehat{DC})$$

$$x^\circ \angle DOC = 72^\circ \text{ (inc/Cent, } \widehat{DC})$$



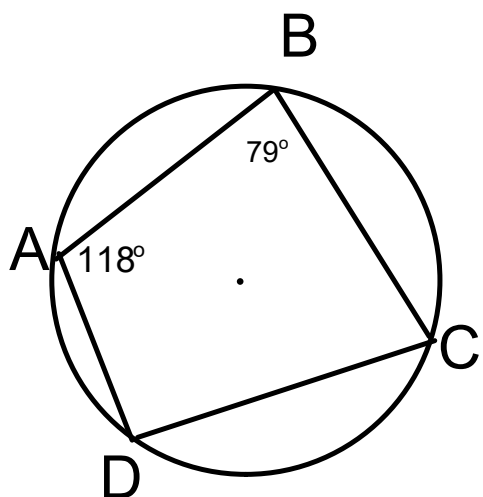
$\angle DOE = 64^\circ$ (given/cent)

$x^\circ \angle DBE = 32^\circ$ (inc/Cent, \widehat{ED})

$y^\circ \angle DBC = 90^\circ$ (inc $>$, dia)



Example:



$$\angle BCD = \underline{62^\circ} \text{ (CyQuad)}$$

$$\angle ADC = \underline{101^\circ} \text{ (CyQuad)}$$

Example 1

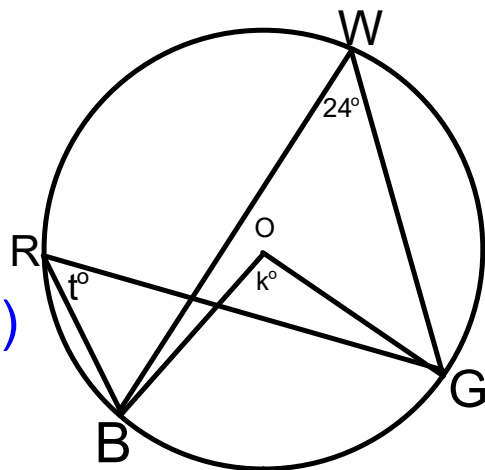
Using Inscribe and Central Angles

Point O is the center of a circle.
Determine the values of k and t .

$$\angle BWG = \underline{24^\circ} \text{ (given/ ins)}$$

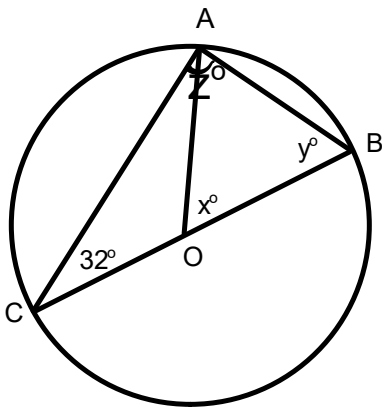
$$k \angle BOG = \underline{48^\circ} \text{ (Inc/Cent, } \widehat{BG} \text{)}$$

$$t \angle BRG = \underline{24^\circ} \text{ (Inc<, } \widehat{BG} \text{)}$$



Example 2

Applying the Property of an Angle Inscribed in a Semicircle



Point O is the center of the circle.
Determine the value of x° , y° and z°

$$\angle ACB = 32^\circ \text{ (given/ ins)}$$

$$x \angle AOB = \underline{64^\circ} \text{ (Inc/Cent } \angle, \widehat{AB} \text{)}$$

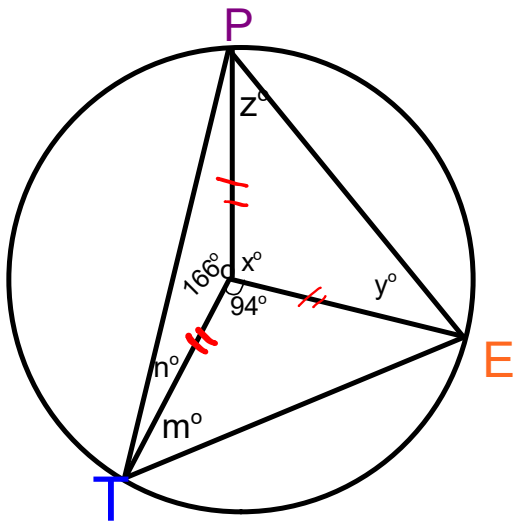
$$z \angle CAB = \underline{90^\circ} \text{ (Inc } \angle, \text{ Dia)}$$

$$y \angle ABC = \underline{58^\circ} \text{ (SATT)}$$

Example 3

Determining Angles in an Inscribed Triangle

Determining the values of x° , y° , z° , m° , n°



Hint: LOOK AT CENTER ANGLES and Complete the circle for x

$$x \angle POE = \underline{100^\circ} \text{ (CyAT)}$$

$$y \angle PEO = \underline{40^\circ} \text{ (ITT)}$$

$$z \angle EPO = \underline{40^\circ} \text{ (ITT)}$$

$$OT = OP = OE \text{ (Radii)}$$

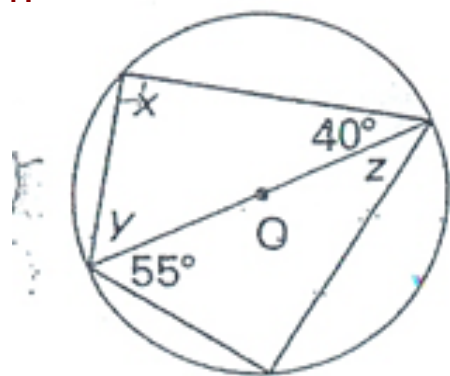
$$m \angle OTE = \underline{43^\circ} \text{ (ITT)}$$

$$n \angle OTP = \underline{7^\circ} \text{ (ITT)}$$

Angle Properties	Tangent & Chord Properties	Circle Properties
(SATT)	$\angle \text{---} = 90^\circ$ (Tang P)	$\angle \text{---} = \text{---}^\circ$ (ins/cent >, $\widehat{\text{---}}$)
(ITT)		
(SAT)	$\angle \text{---} = \angle \text{---} = 90^\circ$ (Chord P)	$\angle \text{---} = \text{---}^\circ$ (ins >, $\widehat{\text{---}}$)
(CAT)		$\angle \text{---} = \text{---}^\circ$ (ins >, diam)
(OAT)	$\text{---} = \text{---}$ (Chord P)	
(CyAT)	$\text{---} = \text{---} = \text{---}$ (Radii)	$\angle \text{---} = \text{---}^\circ$ (CyQuad)
(EAT)		

Examples

1.

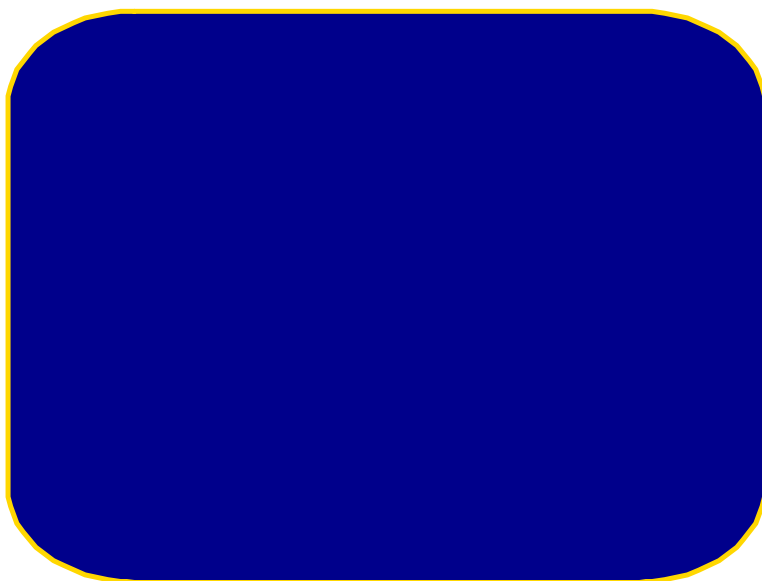


$$X = 90^\circ \text{ (ins } \angle, \text{ dia)}$$

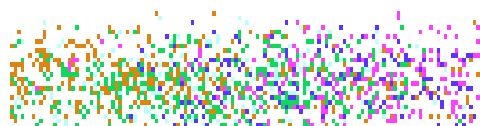
$$y = 50 \text{ (SATT)}$$

$$z = 35^\circ \text{ (SATT)}$$

(cyclic quad)



Class/Homework



-click on the "Homework" link on my teachers page for optional review questions

- If you have any questions you can contact me on the

Remind app

or

through email:

melanie.burns@nbed.nb.ca



Attachments

Worksheet - Angles in a Circle.doc