

WARM-UP: Graph each of the following...

1) $y \leq -\frac{8}{3}x - 3$

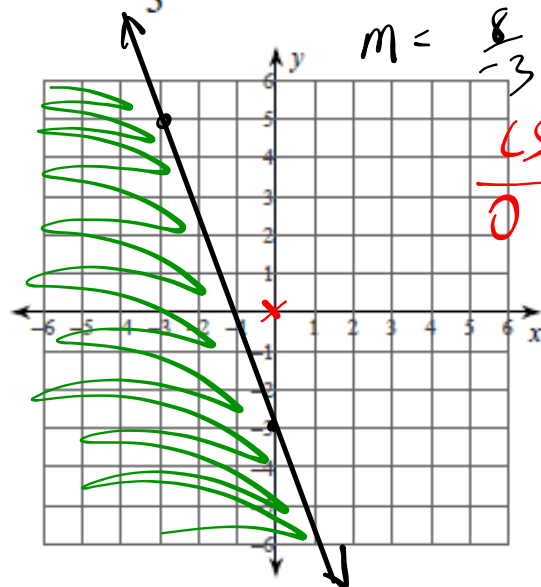
$m = -\frac{8}{3}$

$m = \frac{8}{-3}$ Test (3, 0)

$LS \leq RS$

| | |
|--------|-----------------------|
| 0 | $-\frac{8}{3}(3) - 3$ |
| \leq | -3 |
| | -3 |

$2 \leq 2$



$$2x + 5y - 20 > 0$$

Test (0,0)
 LS > RS $2x + 5y - 20 = 0$

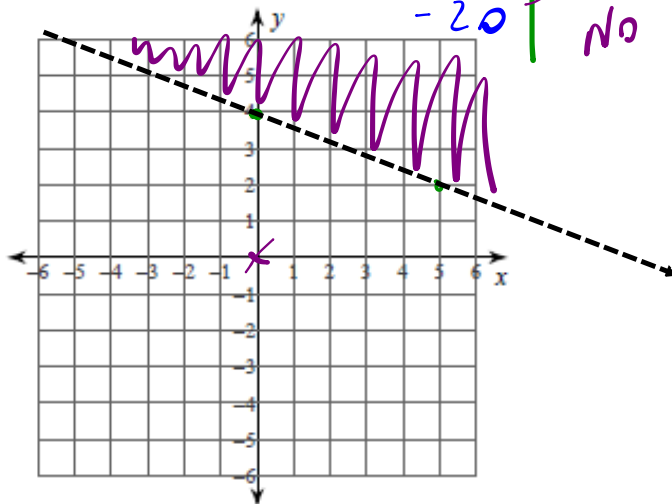
2)

$$\begin{array}{r|l} 2(0) + 5(0) - 20 & 0 \\ \hline -20 & > \end{array} \quad \begin{array}{l} \text{No} \\ \text{No} \end{array}$$

$$5y = -2x + 20$$

$$y = -\frac{2}{5}x + 4$$

$$y = -\frac{2}{5}x + 4$$



HOMEWORK Questions...

④ $3x + 2y < 6$

C Quadrants II, III, IV; excludes boundary line.
 M Quadrants I, II, IV; includes boundary line.
 O All four quadrants; excludes boundary line.

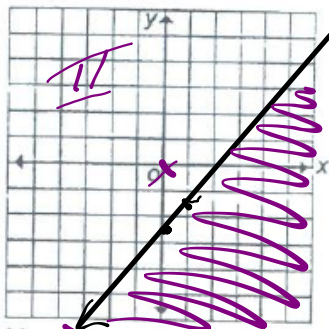
SAB Test (0,0)
 LS < RS
 $3(0) + 2(0) < 6$
 $0 < 6$
 yes

$$3x + 2y = 6$$

$$2y = -\frac{3x}{2} + \frac{6}{2}$$

$$y = -\frac{3}{2}x + 3$$

10 $2(x - y) \geq 5$



- ~~Y~~ All four quadrants; excludes boundary line.
- U Quadrants II, III, IV; includes boundary line.
- A** Quadrants I, III, IV; includes boundary line.

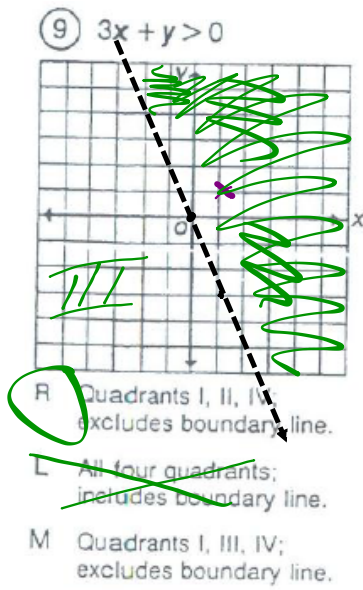
| | |
|-----------|------|
| $LS \geq$ | RS |
| $2(0-0)$ | 5 |
| 0 | No |

$$2(x - y) = 5$$

$$2x - 2y = 5$$

$$-2y = -2x + 5$$

$$y = \frac{1}{1}x - 2.5$$

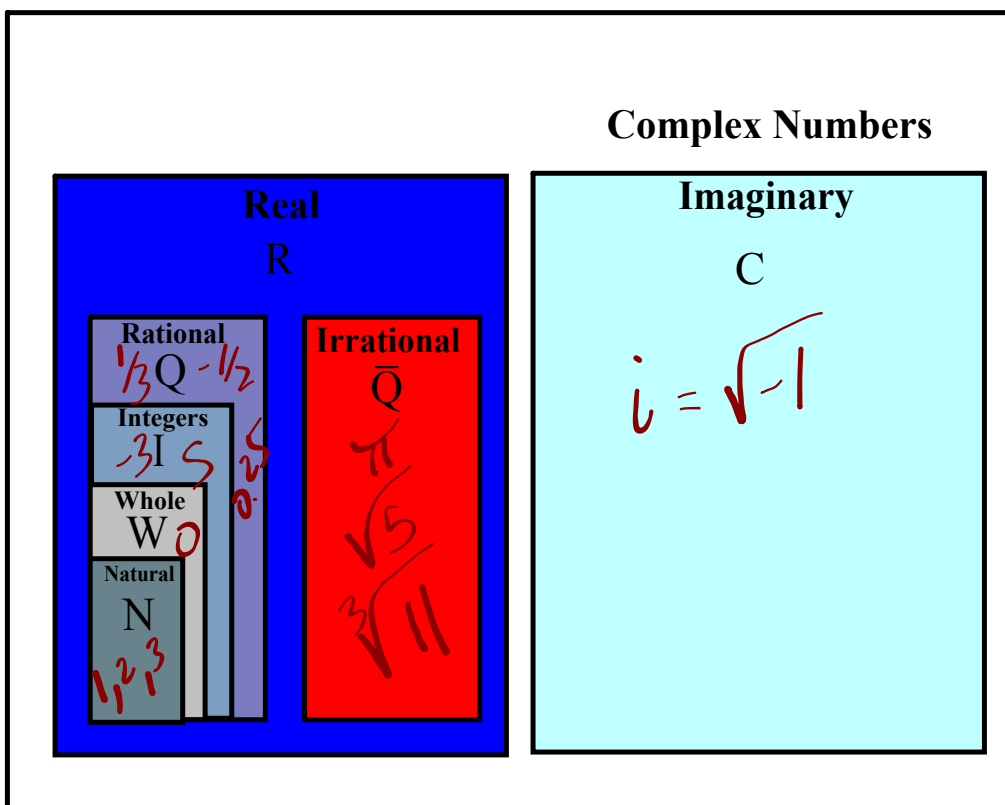


Test (1, 1)
 $LS > RS$

| | | |
|------------|-----|-------|
| $3(1) + 1$ | $>$ | 0 |
| 4 | $>$ | 0 |
| | | yes |

$3x + y = 0$
 $y = -\frac{3}{1}x$

STORYTIME: "The Complete Number System"



5.1

Graphing Linear Inequalities in Two Variables

GOAL

Solve problems by modelling linear inequalities in two variables.

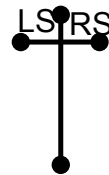
EXPLORE...

• For which inequalities is (3, 1) a possible solution? How do you know?

- a) $13 - 3x > 4y$
- b) $2y - 5 \leq x$
- c) $y + x < 10$
- d) $y \geq 9$

← sub

VERIFY



Let's VERIFY...

a) $LS > RS$

$$\begin{array}{r|l} 13 - 3(3) & 4(1) \\ \hline 13 - 9 & 4 \\ 4 & > 4 \\ & \text{No} \end{array}$$

b) $LS \leq RS$

$$\begin{array}{r|l} 2(1) - 5 & 3 \\ \hline -3 & \leq 3 \\ & \text{Yes} \end{array}$$

c) $LS < RS$

$$\begin{array}{r|l} 1 + 3 & 10 \\ \hline 4 & < 10 \\ & \text{Yes} \end{array}$$

d) $LS \geq RS$

$$\begin{array}{r|l} 1 & 9 \\ \hline 1 & \geq 9 \\ & \text{No} \end{array}$$

Graphs of Linear In-Equalities

Sometimes the domain and range are stated as being in the set of integers. This means that the solution set is **discrete** and consists of separate or distinct parts. Discrete variables represent things that can be counted, such as people in a room. This means that the solution region is not shaded but rather stippled with points.

So when interpreting the solution region for a linear inequality, consider the restriction on the domain and range of the variables.

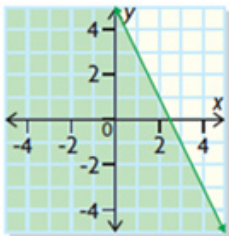
If the solution set is **continuous**, all the points in the solution region are in the solution set. (Shaded)

If the solution set is **discrete**, only specific point in the solution region are in the solution set. This is represented graphically by stippling. (dots) $\rightarrow N, W, I$

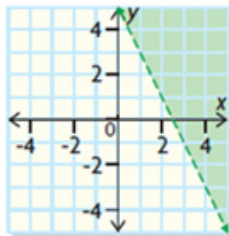
Some solution sets may be restricted to specific quadrants. For example, most linear inequalities representing real-world problem situations have graphs that are restricted to the first quadrant.

Here are some examples:

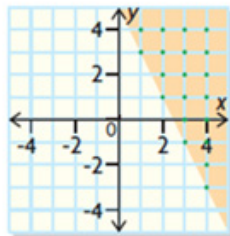
$$\{(x, y) \mid y \leq -2x + 5, x \in \mathbb{R}, y \in \mathbb{R}\}$$



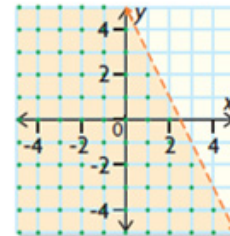
$$\{(x, y) \mid y > -2x + 5, x \in \mathbb{R}, y \in \mathbb{R}\}$$



$$\{(x, y) \mid y \geq -2x + 5, x \in \mathbb{I}, y \in \mathbb{I}\}$$



$$\{(x, y) \mid y < -2x + 5, x \in \mathbb{I}, y \in \mathbb{I}\}$$



Let's do a couple more...

1) $\{(x,y) \mid 2x + 5y \leq -20, x \in I, y \in I\}$

$LS \leq RS$

$2(0) + 5(0) \leq -20$
 $0 \leq -20$ NO

→ stipple

} → Set #'s

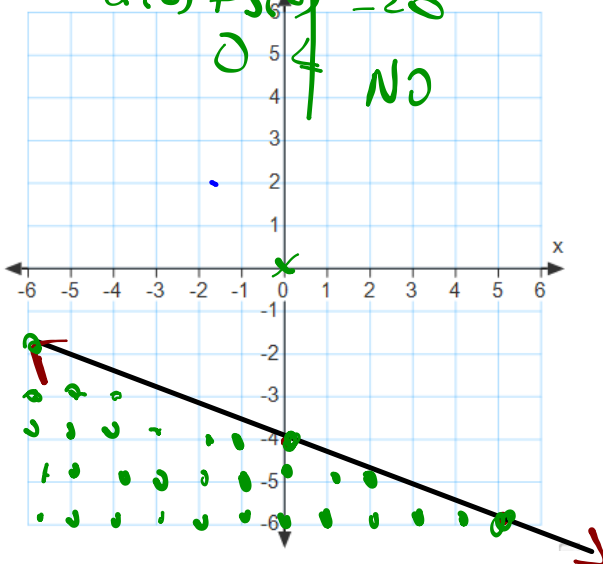
$2x + 5y = -20$

$y = -\frac{2}{5}x - \frac{20}{5}$

$y = -\frac{2}{5}x - 4$

| → such that

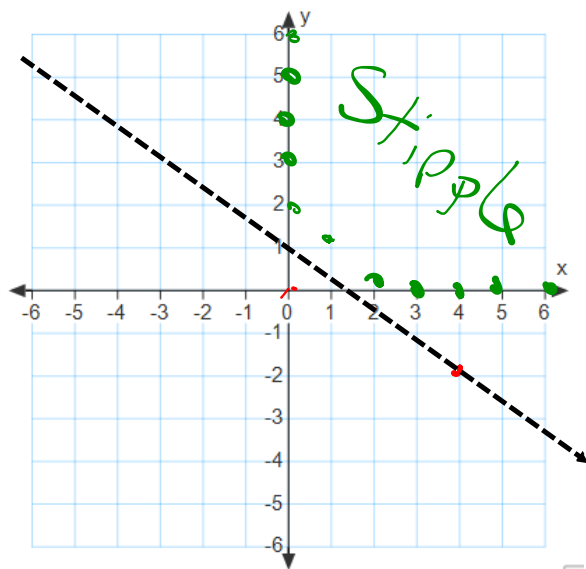
∈ → belongs to



2) $\{(x,y) \mid 3x+4y > 4, x \in W, y \in W\}$

dashed

Stipple Q1



$$3x + 4y = 4$$

$$4y = -3x + 4$$

$$y = -\frac{3}{4}x + 1$$

LS > RS

| | | |
|---------------|-----|------|
| $3(0) + 4(0)$ | 4 | 4 |
| 0 | 7 | NO |

HOMework... Questions?

p. 221: #1, #2, #4 and #6