September, 2017

UNIT 1: ROOTS AND POWERS

SECTION 3.1: FACTORS AND MULTIPLES OF WHOLE NUMBERS

K. Sears
NUMBERS, RELATIONS AND FUNCTIONS 10

WHAT'S THE POINT OF TODAY'S LESSON?

We will begin working on the NRF 10 Specific Curriculum Outcome (SCO) "Algebra and Numbers 1" OR "AN1" which states:

"Demonstrate an understanding of factors of whole numbers by determining the prime factors, greatest common factor, least common multiple, square root and cube root."



What does THAT mean???

SCO AN1 means that we will:

- * find the prime factors of whole numbers like 8 (2^3 or $2 \cdot 2 \cdot 2$)
- * determine the greatest common factor (GCF) of numbers like 28 and 49 (GCF = 7)
- * determine the least common multiple (LCM) of numbers like 6 and 9 (LCM = 18)
- * determine if a given whole number is a perfect square, like 25 (5.5) or a perfect cube, like 8 (2.2.2)
- * determine the square root of perfect squares, like 36 ($\sqrt{36}$ = 6), and the cube root of perfect cubes, like 64 ($\sqrt[3]{64}$ = 4)

Use prime factorization to determine the

- a) GCF of 856, 1200 and 1368
- b) LCM of 28, 42 and 63

10 X 12

a) GCF of 856, 1200 and 1368:

GCF = Greatest	
Method 856	1200
I 1x 856	1×1200
2 × 428	2 x 600
4x214	3 x 400
8 x 107	4 x 300 5 x 240
	6 x 200
: •	8 x 150
continued	10 K 12 D

1368 1x 1368
2x 684 3x 456 4x 342
6x228 8x171 9x152

Method IL 4x214 2x2x2x107 23x107

8×171 2×4×3×57 2×2×2×3×57 2³×3×57

b) LCM of 28, 42 and 63:

LCM = Least Common Multiple

28
42
63

Method I

28 56 84 112 140 168 196 224 252

42 84 126 168 210 252

63 126 149 252

Method II

28 56 87
789
28287
28387
3287

CM =
$$2^2 \times 3^2 \times 7$$

Choose higher power for each number = 252

- a) What is the GCF of 340 and 380?
- b) Reduce the fraction $\frac{340}{380}$ to its simplest form.
- c) What is the <u>LCM</u> of 340 and 380?
- d) What is $\frac{15}{340} + \frac{10}{380}$?

$$G(F = \lambda^2 \times 5)$$

$$= 4 \times 5$$

$$= 20$$

$$Lcm = 2^2 \times 5 \times 17 \times 19$$

= 6460

a)
$$GCF$$
 340
 380
 38.10
 38.10
 38.10
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$$\frac{340}{380} \stackrel{?}{-} \stackrel{?}{-} \stackrel{?}{20}$$

$$= \frac{17}{19}$$

c) LCM
$$\frac{340}{34.10}$$
 $\frac{380}{34.10}$ $\frac{34.10}{38.10}$ $\frac{38.10}{34.10}$ $\frac{38.10}{34.10}$ $\frac{38.10}{340.19}$ $\frac{38.5.17}{340.19}$ $\frac{380}{340.19}$ $\frac{15}{340}$ $\frac{17}{400}$ $\frac{15}{340}$ $\frac{170}{400}$ $\frac{15}{340}$ $\frac{170}{400}$ $\frac{15}{340}$ $\frac{170}{400}$ $\frac{15}{340}$ $\frac{170}{400}$ $\frac{15}{340}$ $\frac{170}{400}$ $\frac{170}$ $\frac{170}{400}$ $\frac{170}{400}$ $\frac{170}{400}$ $\frac{170}{400}$ $\frac{$

VOCABULARY:

prime number: a whole number with exactly two factors,

itself and 1.

EX.: 2, 3, 5, 7, 11, 13, 17, 19, 23, and 29 are the first 10 prime numbers.

composite number: a number with three or more factors.

EX.: 8 is a composite number; it has four factors (1, 2, 4 and 8).

prime factor: a prime number that is a factor of a

number.

EX.: The prime factors of 30 are 2, 3, and 5.

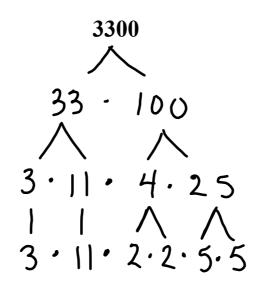
prime factorization: writing a number as a product of its

prime factors.

EX.: The prime factorization of

20 is 2.2.5 or $2^2.5$.

USING FACTOR TREES FOR PRIME FACTORIZATION:



P. F. =
$$2 \cdot 2 \cdot 3 \cdot 5 \cdot 5 \cdot 11$$

OR

 $2^{2} \cdot 3 \cdot 5^{2} \cdot 11$

#2 - 3.1 Factors and Multiples of Whole Numbers Solutions.notebook	September 07	, 2017
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USING FACTOR TREES FOR PRIME FACTORIZATION:

YOU TRY! :)

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DETERMINING THE GREATEST COMMON FACTOR:

EX.: Determine the GCF of 12 and 15.

DETERMINING THE GREATEST COMMON FACTOR:

EX.: You try! Determine the GCF of 18 and 24.

DETERMINING THE GREATEST COMMON FACTOR FOR LARGER NUMBERS: PRIME FACTORIZATION

EX.: Determine the GCF of 138 and 198.

Once you have the prime factorization of the numbers, multiply all the prime factors they have in common to determine their GCF.

DETERMINING THE GREATEST COMMON FACTOR FOR LARGER NUMBERS: PRIME FACTORIZATION

EX.: You try! Determine the GCF of 126 and 144.

DETERMINING THE LOWEST COMMON MULTIPLE:

EX.: Determine the LCM of 8 and 12.

September 07, 2017

DETERMINING THE LOWEST COMMON MULTIPLE:

EX.: You try! Determine the LCM of 6 and 10.

DETERMINING THE LOWEST COMMON MULTIPLE FOR LARGER NUMBERS OR GROUPS OF NUMBERS: PRIME FACTORIZATION

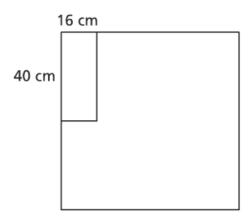
EX.: Determine the LCM of 18, 20 and 30.

Once you have the prime factorization of the numbers, multiply the greatest power of each of the prime factors to determine the LCM.

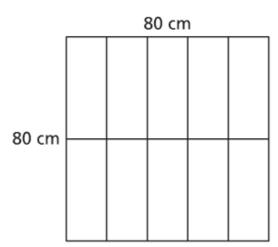
DETERMINING THE LOWEST COMMON MULTIPLE FOR LARGER NUMBERS OR GROUPS OF NUMBERS: PRIME FACTORIZATION

EX.: You try! Determine the LCM of 28, 42 and 63.

EX.: What is the side length of the SMALLEST square that could be tiled with rectangles that measure 16 cm by 40 cm? (Assume the tiles cannot be cut.) Sketch the square and the rectangular tiles.



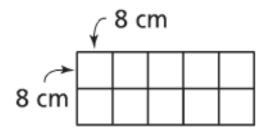
EX.: What is the side length of the SMALLEST square that could be tiled with rectangles that measure 16 cm by 40 cm? (Assume the tiles cannot be cut.) Sketch the square and the rectangular tiles.



EX.: What is the side length of the LARGEST square that could be used to tile a rectangle that measures 16 cm by 40 cm? (Assume the tiles cannot be cut.) Sketch the rectangle and the square tiles.

	40 cm	
16 cm		

EX.: What is the side length of the LARGEST square that could be used to tile a rectangle that measures 16 cm by 40 cm? (Assume the tiles cannot be cut.) Sketch the rectangle and the square tiles.



CONCEPT REINFORCMENT:

"FOUNDATIONS AND PRE-CALCULUS - MATHEMATICS 10" (FPCM 10)

pages 140 / 141: #3 TO #13, #15 TO #19a and #20