February, 2018

UNIT 1: ROOTS AND POWERS

SECTION 3.2:
PERFECT SQUARES,
PERFECT CUBES, AND
THEIR ROOTS



K. SEARS

NUMBERS, RELATIONS AND FUNCTIONS 10

WHAT'S THE POINT OF TODAY'S LESSON?

We will continue working on the NRF 10 Specific Curriculum Outcome (SCO) "Algebra and Numbers 1" OR "AN1" which states:

"Demonstrate an understanding of factors of whole numbers by determining the prime factors, greatest common factor, least common multiple, square root and cube root."



What does THAT mean???

SCO AN1 means that we will:

* find the prime factors of whole numbers like 8 (2³ or 2.2.2)

* determine the greatest common factor (GCF) of numbers like 28 and 49 (GCF = 7)

- * determine the least common multiple (LCM) of numbers like 6 and 9 (LCM = 18)
- * determine if a given whole number is a perfect square, like 25 (5.5) or a perfect cube, like 8 (2.2.2)
- * determine the square root of perfect squares, like 36 ($\sqrt{36} = 6$), and the cube root of perfect cubes, like 64 ($\sqrt[3]{64} = 4$)



WARM-UP:

- 1. Determine the GCF of 81 and 216.
- 2. Determine the LCM of 21 and 45.

1.
$$\frac{81}{9 \times 9}$$
 $\frac{2 \times 108}{2 \times 108}$ $\frac{6CF}{3}$ = 27 $\frac{3 \times 3 \times 3}{3}$ $\frac{2 \times 2 \times 3 \times 3}{2 \times 2 \times 3 \times 9}$ $\frac{2 \times 2 \times 2 \times 3 \times 9}{2 \times 2 \times 3 \times 3}$ $\frac{2 \times 2 \times 3 \times 3}{2 \times 3 \times 3}$

WARM-UP:



1. Determine the GCF of 120, 960 and 1400.



2. Determine the LCM of 15, 32 and 44.



- 1. 120
 - 960 16 x 60 4x4 x 6x10 2x2 2x21 2x3 2x5 2x3 x5
- 70x20 7x10x4x5 7x2x5x3x2x5 23x5xx7
- 2. 15 32 44 3x5 4x6 4x1 2x2x2x2 2x2 2x2x2x2x2 2xx1
- LCM=25x3x5x11 = 5280

Homework questions

WARM-UP:



Determine whether each number is a perfect square, a perfect cube or neither:

- a) 3136
- b) 4096
- c) 5832
- d) 2808

P.S. P.C. Both **Neither**

3136 156 x 14.63... X

4096 64 616

5832 x 76.36... 18

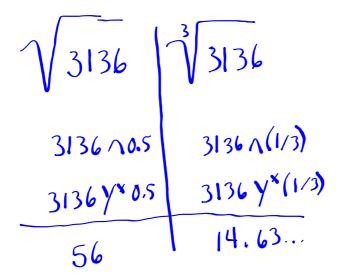
2808 x 52.77... X14.1...

X

5th root?

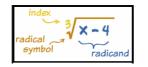
7776

√y 7776 Λ(1/5) 7776 √y 5



HOMEWORK QUESTIONS??? (pg 140, #6 TO #8, #15ad, #16af, #17 & #19)

VOCABULARY:



Cube root of "x-4"

1. Square Root: a number which, when multiplied by

itself, results in a given number. EX.: 5 is a square root of 25.

2. Cube Root: a number which, when raised to the

exponent 3, results in a given number.

EX.: 5 is the cube root of 125.

3. Radical: An expression consisting of a radical

sign, a radicand and an index.

EX.: 3/64

4. Radicand: The number under a radical sign.

EX.: 64 is the radicand in 3/64

5. Index: The number above the radical symbol

that indicates which root is to be taken. EX.: 3 is the index in $\sqrt[3]{64}$; if the index is not written, it is assumed to be 2.

GETTING STARTED:

Let's make a list on a separate sheet of loose-leaf of the first twenty perfect squares, perfect cubes and perfect fourth powers:

	Perfect Squares	Perfect Cubes	Perfect Fourth Powers
1	1	1	1
2	4	8	16
3	9	27	81
4	16	64	
5	25	125	
2 3 4 5 6	36	67=216	
7	49		
8 9	64		
9	8 l	1000	10 000
10	(00 121		•
11			
12	144		
13	169		
14	196		
15	225		
16			
17			
18			
19			
20	400		

GETTING STARTED:

Let's make a list on a separate sheet of loose-leaf of the first twenty perfect squares, perfect cubes and perfect fourth powers:

	Perfect Squares	Perfect Cubes	Perfect Fourth Powers
1	1	1	1
2	4	8	16
3	9	27	81
4	16	64	256
5	25	125	625
6	36	216	1296
7	49	343	2401
8	64	512	4096
9	81	729	6561
10	100	1 000	10 000
11	121	1 331	14 641
12	144	1 728	20 736
13	169	2 197	28 561
14	196	2 744	38 416
15	225	3 375	50 625
16	256	4 096	65 536
17	289	4 913	83 521
18	324	5 832	104 976
19	361	6 859	130 321
20	400	8 000	160 000

BUILDING ON WHAT WE KNOW:

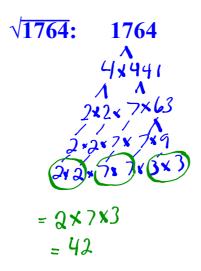
We can use PRIME FACTORIZATION now to help us determine square roots and cube roots.

Example: Use prime factorization to determine the square root of 1296.

$$\sqrt{1296}: 1296$$
= 4 · 324
= 2 · 2 · 4 · 81
= 2 · 2 · 2 · 2 · 9 · 9
= 2 · 2 · 2 · 2 · 3 · 3 · 3 · 3
= (2 · 2 · 3 · 3) (2 · 2 · 3 · 3)
= 36 · 36
$$36^{2} = 1296, \text{ so } \sqrt{1296} = 36.$$

BUILDING ON WHAT WE KNOW:

Example: YOU TRY! Use prime factorization to determine the square root of 1764.



CONCEPT REVIEW:

In grade 9, you explored the relationship between the area

of a square and its side length:

$$\sqrt{15} = 5$$

– Area = 25 square units –

BUILDING ON WHAT WE KNOW:

Example: Use prime factorization to determine the cube root of 1728.

$$\sqrt[3]{1728}$$
: 1728
= 4 ⋅ 432
= 2 ⋅ 2 ⋅ 4 ⋅ 108
= 2 ⋅ 2 ⋅ 2 ⋅ 2 ⋅ 4 ⋅ 27
= 2 ⋅ 2 ⋅ 2 ⋅ 2 ⋅ 2 ⋅ 2 ⋅ 3 ⋅ 9
= 2 ⋅ 2 ⋅ 2 ⋅ 2 ⋅ 2 ⋅ 2 ⋅ 3 ⋅ 3 ⋅ 3
= (2 ⋅ 2 ⋅ 3)(2 ⋅ 2 ⋅ 3)(2 ⋅ 2 ⋅ 3)
= 12 ⋅ 12 ⋅ 12
12³ = 1728, so $\sqrt[3]{1728}$ = 12.

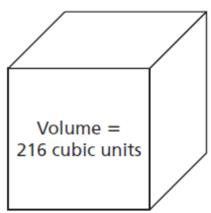
BUILDING ON WHAT WE KNOW:

Example: YOU TRY! Use prime factorization to determine the cube root of 2744.

NEW CONCEPT:

Based on what you know about squares, their area and their side length along with cube roots, can you now determine the edge length of a cube? What about its surface area?

$$3\sqrt{216} = 6$$
 $216 \wedge (1/3)$
 $3\sqrt{216}$
 $216 \sqrt{1 + 3}$



YOU TRY!

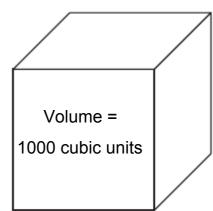
Based on what you know about squares, their area and their side length along with cube roots, can you now determine the edge length of this cube? What about its surface area?

$$X = \frac{3}{1000} = 10$$

$$SA = Arca side \times 6$$

$$= (10)(10) \times 6$$

$$= 600 \text{ square units}$$



CONCEPT REINFORCEMENT:

FPCM 10

QUIZ PREPARATION / PRACTICE:

FPCM 10:

page 149: 1 - 8, 10

page 140: Revisit #17 and #19a page 147: Revisit #7 and #8

QUIZ on sections 3.1 and 3.2

QUIZ PREPARATION / PRACTICE:

FPCM 10:

page 149: #1 to #8 and #10

page 140: Revisit #17 and #19a

page 147: Revisit #7 and #8

QUIZ on sections 3.1 and 3.2