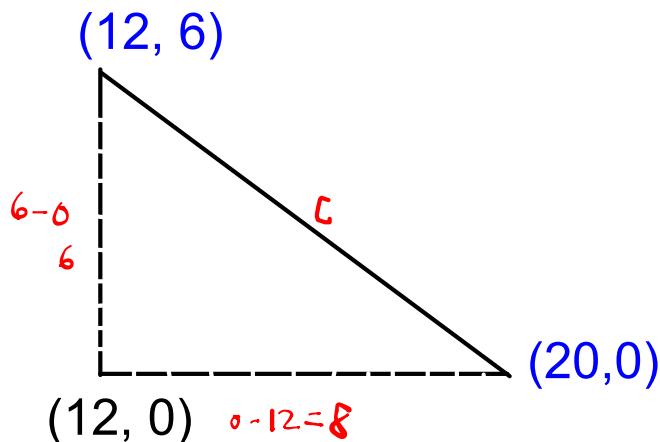
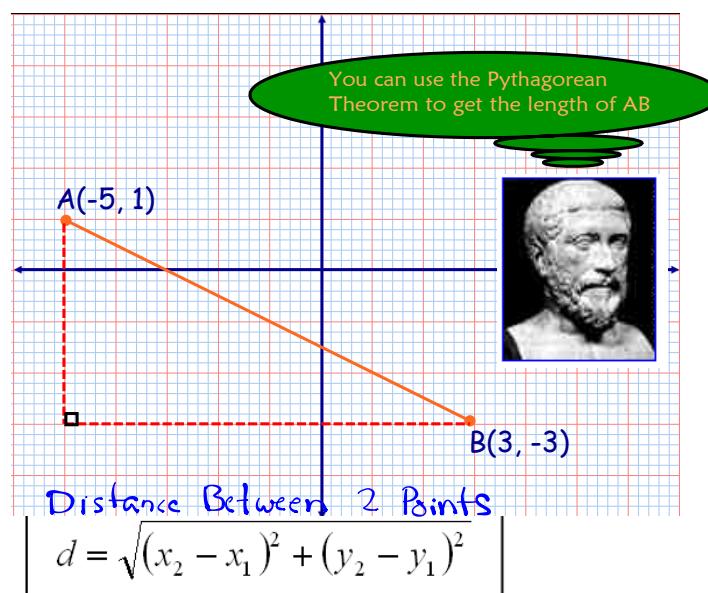


Find the distance between (12, 6) and (20, 0).



$$\begin{aligned}
 c^2 &= a^2 + b^2 \\
 &= 6^2 + 8^2 \\
 &= 36 + 64 \\
 &= 100 \\
 c &= \sqrt{100} \\
 &\approx 10
 \end{aligned}$$

Distance between two points



Example:

$$\begin{aligned}
 d(AB) &= \sqrt{(-5-3)^2 + (1-(-3))^2} \\
 &= \sqrt{(-8)^2 + 4^2} \\
 &= \sqrt{64+16} \\
 &= \sqrt{80} \\
 &\approx 8.9 \quad 4\sqrt{5}
 \end{aligned}$$

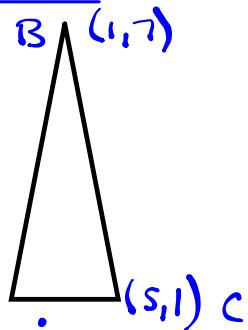
Examples...

#1. Use the distance formula to show that the triangle with vertices $A(-3, 1)$; $B(1, 7)$ & $C(5, 1)$ is isosceles.

$$\overline{AC} = \sqrt{(-3-5)^2 + (1-1)^2} = 8$$

$$\begin{aligned} d_{AB} &= \sqrt{(-3-1)^2 + (1-7)^2} \\ &= \sqrt{(-4)^2 + (-6)^2} \\ &= \sqrt{16+36} \\ &= \sqrt{52} \\ &= 2\sqrt{13} \\ &\approx 7.2 \end{aligned}$$

$$\begin{aligned} d_{BC} &= \sqrt{(1-5)^2 + (7-1)^2} \\ &= \sqrt{(-4)^2 + (6)^2} \\ &= \sqrt{16+36} \\ &= \sqrt{52} \\ &= 7.2 \end{aligned}$$

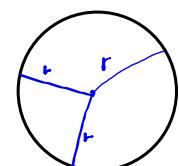


The Δ is isosceles.

#2. Find the distance between $A(-2, 1)$ & $B(8, 3)$

$$\begin{aligned} d &= \sqrt{(x_2-x_1)^2 + (y_2-y_1)^2} \\ d_{AB} &= \sqrt{(8-(-2))^2 + (3-1)^2} \\ &= \sqrt{10^2 + 2^2} \\ &= \sqrt{100+4} \\ &= \sqrt{104} \\ &= \sqrt{104} \\ &= \sqrt{4 \times 26} \\ &= 2\sqrt{26} \end{aligned}$$

#3. Show that the points $(5, -1)$; $(2, 8)$ & $(-2, 0)$ lie on a circle whose center is $(2, 3)$



$$\begin{aligned} d &= \sqrt{(x_2-x_1)^2 + (y_2-y_1)^2} \\ d_{AO} &= \sqrt{(5-2)^2 + (-1-3)^2} \\ &= \sqrt{3^2 + (-4)^2} \\ &= \sqrt{9+16} \\ &= \sqrt{25} \\ &= 5 \\ d_{CO} &= \sqrt{(-2-2)^2 + (0-3)^2} \\ &= \sqrt{(-4)^2 + (-3)^2} \\ &= \sqrt{16+9} \\ &= \sqrt{25} \\ &= 5 \\ d_{BO} &= \sqrt{(2-2)^2 + (3-8)^2} \\ &= \sqrt{0^2 + (-5)^2} \\ &= \sqrt{25} \\ &= 5 \end{aligned}$$

Homework...

Worksheet - Distance_Midpoint(2).pdf



Sec. 6.6 - LEFT SIDE

- # 2 (a) , (b), (d) 2. Distance from the origin
#4 a) $(6, 8)$ b) $(-1, 8)$ d) $\sqrt{3}, 1$

- # 6 4. Distance from $(1, 4)$
a) $(-1, 7)$ b) $(-2, 6)$ c) $(4, 6)$

6. $\Delta P(-1, 2) Q(2, 6) R(-4, 4)$
a) Find the perimeter
b) Classify the Δ .

Attachments

[Worksheet - Distance_Midpoint\(2\).pdf](#)