

1) When is the particle speeding up? When is it slowing down?

$$s = f(t) = t^3 - 6t^2 + 9t$$

Speeding up

I. $v > 0 \wedge a > 0$

velocity > 0

$$\frac{3t^2}{3} - \frac{12t}{3} + \frac{9}{3} > 0$$

$$t^2 - 4t + 3 > 0$$

$$(t-3)(t-1) > 0$$

$$t < 1, 3$$

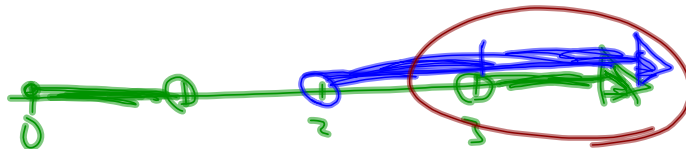
AND

Accel. > 0

$$6t - 12 > 0$$

$$6t > 12$$

$$t > 2$$



speeding up: $\{t > 3\}$

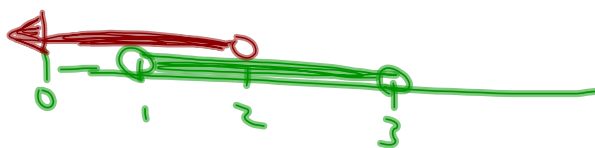
II. vel $< 0 \wedge$ accel < 0

$$1 < t < 3$$

$$6t - 12 < 0$$

$$6t < 12$$

$$t < 2$$



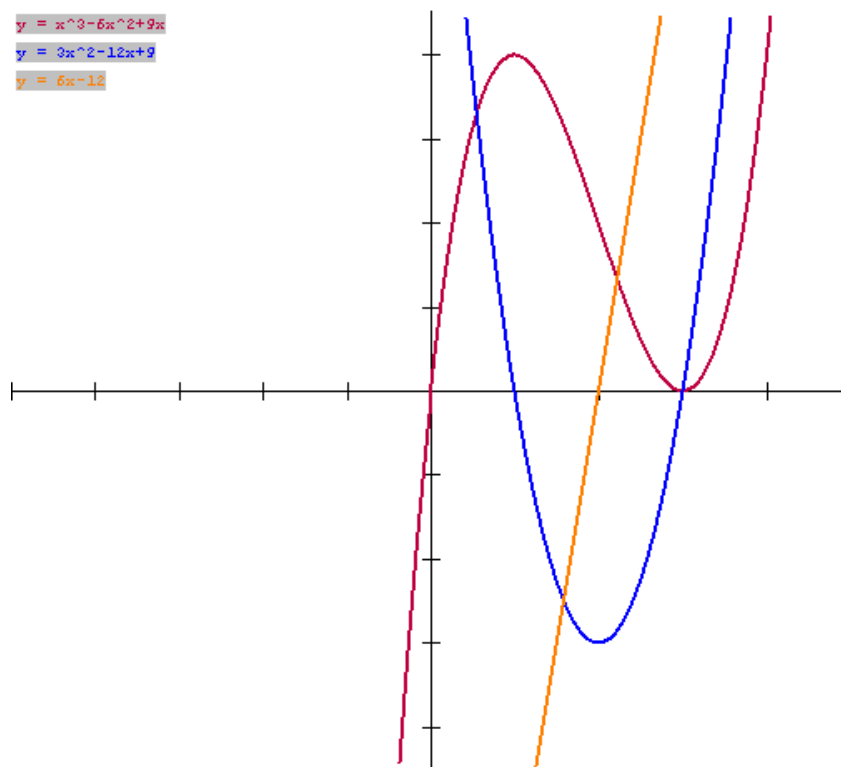
$\{1 < t < 2\}$

Speeding up: $\{t / 1 < t < 2 \text{ or } t > 3, t \in \mathbb{R}\}$

Slowing Down: $\{0 \leq t < 1 \text{ or } 2 < t < 3\}$

h) Graph the position, velocity, and acceleration functions for $0 \leq t \leq 5$.

$y = x^3 - 6x^2 + 9x$
 $y = 3x^2 - 12x + 9$
 $y = 6x - 12$



i) When is the particle speeding up? When is it slowing down?

Time to check your understanding...

A particle moves according to a law of motion $s(t) = 2t^3 - 9t^2 + 12t + 1$, $t \geq 0$.

- Determine the velocity of the particle when it has acceleration 2 units/s².
- When is this particle moving in a positive direction? ($s'(x) > 0$)
- Sketch the path of this particle, and determine how far it has traveled during the first 8 seconds.

$$(a) s'(t) = 6t^2 - 18t + 12$$

$$s''(t) = 12t - 18$$

$$12t - 18 = 2$$

$$12t = 20$$

$$t = \frac{20}{12} = \frac{5}{3}$$

$$s'\left(\frac{5}{3}\right) = 6\left(\frac{5}{3}\right)^2 - 18\left(\frac{5}{3}\right) + 12$$

$$= 6\left(\frac{25}{9}\right) - 30 + 12$$

$$= \frac{50}{3} - \frac{18}{1}$$

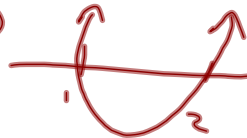
$$= -\frac{4}{3} \text{ units/sec}$$

$$(b) \frac{6t^2}{6} - \frac{18t}{6} + \frac{12}{6} > 0$$

$$t^2 - 3t + 2 > 0$$

$$(t-2)(t-1) > 0$$

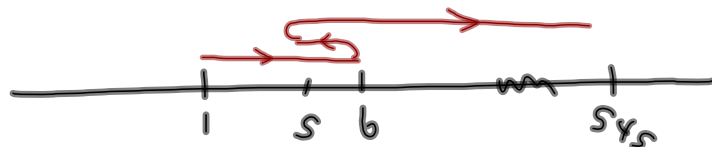
$$t = 1, 2$$



$$\{0 \leq t < 1 \text{ or } t > 2\}$$

t	s
0	1
1	6
2	5
4	5
8	45

X =



$$\text{Distance} = 5 + 1 + 54$$

$$= \underline{54 \text{ units}}$$

Practice exercises...

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#3, 4, 5, 8, 9

#6, 7, 8

Topics to Review:

- Power rule, product rule, quotient rule, chain rule
- Derivatives of trigonometric functions
- Applications of derivatives...
 - *slopes of tangent lines
 - *rectilinear motion
- Implicit differentiation
- Higher order derivatives

Review Questions...

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#1 c, d

#7 b, d

#8 b, d

#9 a, b, d, f

#11

#12

Bonus #13

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#1 (ii)

#3

#4

#5

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#2

#3