

Quiz...

Review:

(d) $5b - 4(2b + 8)$

* $5b - 8b - 32$
 $= -3b - 32$

(e) $3a^2b(5a^2b^2 - 2ab) - 4ab^2(a^2 - 6a^2b)$

$15a^3b^3 - 6a^3b^2 - 4a^3b^2 + 24a^3b^3$
 $= 39a^3b^3 - 10a^3b^2$

2. $(3x - 5)(3x - 5)$

$9x^2 - 30x + 25 - (4x^2 - 3x + 28x - 21)$

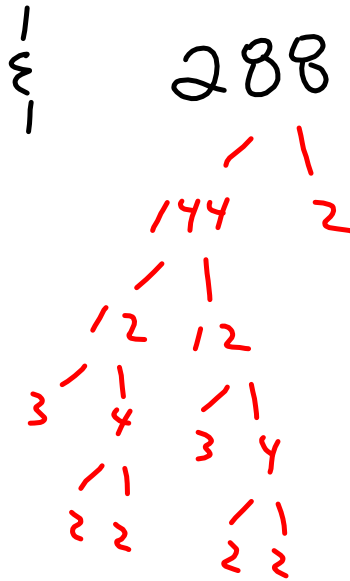
$= 2x^3 + 10x^2 - 50x + 88$

$+ (x^2 - 2x^2 + 12x + 7x^2 - 7x + 12)$



$= 5 \times 2 \times 3^2$

$GCF = 2 \times 3^2$
 $= 18$



$= 2^5 \times 3^2$

$LCM = 5 \times 2^5 \times 3^2$
 $= 1440$

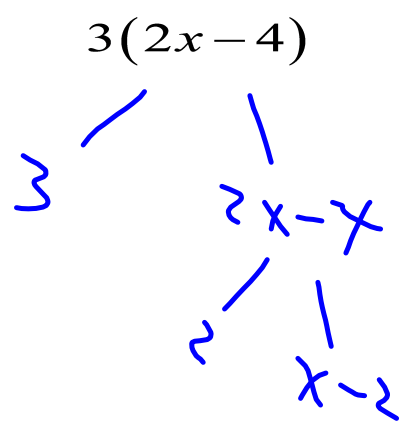
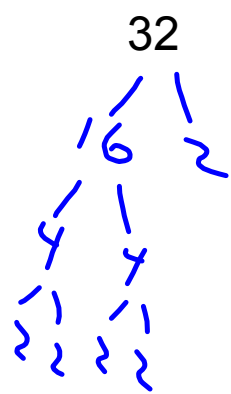
Find GCF (18)
LCM
1440

Factoring is the same as the process of PRIME FACTORIZATION...
 Only it is done using algebra skills!!

Determine the prime factorization for each of the following...

$$2x - 4$$

$$2(x - 2)$$



Factoring



There are 5 different kinds of Factoring:

- Greatest common factor (GCF)
- Factor by grouping ("Pair them up")
- Simple Trinomials (Factor by Inspection)
- Hard Trinomials (Factor by Decomposition)
- Special Factors
 - Difference of Squares
 - Perfect Square Trinomials

Greatest Common Factor - there is a **G**reatest **C**ommon **F**actor amongst any number of terms in a polynomial

- factor out the GCF from the polynomial and multiply it against the remainder.
- sometimes the GCF may be a polynomial.
ex: common binomial

EXAMPLES...

Factor

1) $\frac{5x^2}{5x^2} + \frac{25x^3}{5x^2} - \frac{30x^4}{5x^2}$ 2) $36x^7y^4 - 16x^3y^5 - 24x^5y^3$ 3) $9x(a-b) - 14y(a-b)$

$\underline{5x^2}(1 + 5x - 6x^2)$

$\frac{x^3}{x^3} = x^0 = 1$

2) $\frac{36x^7y^4}{4x^3y^3} - \frac{16x^3y^5}{4x^3y^3} - \frac{24x^5y^3}{4x^3y^3}$
 $4x^3y^3(9x^4y - 4y^2 - 6x^2)$

extra: $3 \text{ ☺}^3 - 9 \text{ ☺}^7$
 $3 \text{ ☺}^3 (1 - 3 \text{ ☺}^4)$

3) $\frac{9x(a-b)}{a-b} - \frac{14y(a-b)}{a-b}$
 $(a-b)(9x - 14y)$

$9x \frac{a-b}{a-b} - 14y \frac{a-b}{a-b}$
 $\frac{a-b}{a-b} (9x - 14y)$

EXERCISE: Factor each of the following...

1) $20x+15y-30z$

$$5(4x+3y-6z)$$

$$\begin{array}{c} 6 \\ \swarrow \quad \searrow \\ 3 \quad 2 \end{array}$$

3) $12x^3y^2 - 18xy$

$$6xy(2x^2y - 3)$$

2) $25x^7 - 50x^4$

$$25x^4(x^3 - 2)$$

4) $3x(\underline{2x-1}) + 5(\underline{2x-1})$

$$(2x-1)(3x+5)$$

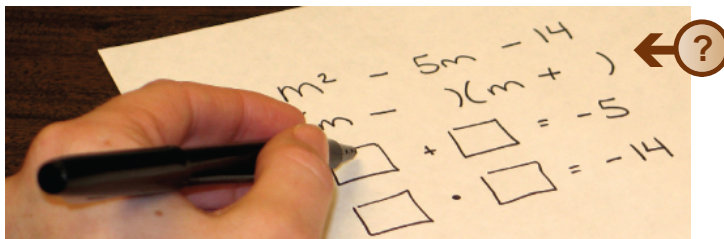
Simple Trinomials

Look at the numbers in the trinomial and the binomial.

$$v^2 + 12v + 20 = (v + 2)(v + 10)$$

12 is the sum of 2 and 10.

20 is the product of 2 and 10.



How could you complete this factorization?



3.5 Polynomials of the Form $x^2 + bx + c$

II. Factoring Trinomials:

Type 1: Polynomials of the form $x^2 + bx + c$

- Often referred to as "Simple Trinomials"

Expand each of the following:

(a) ~~$(w + 5)(w - 4)$~~
 $w^2 + w - 20$

(b) $(x - 8)(x - 6)$
 $x^2 - 14x + 48$

Expanding \longrightarrow

\longleftarrow Factoring

① $w^2 + w - 20$
 $(w - 4)(w + 5)$

$\xrightarrow{\text{green arrow}}$

$\frac{-4}{1} + \frac{5}{1} = 1$
 $\frac{-4}{1} \times \frac{5}{1} = -20$