

Ex. $6 \sin^2 x - \sin x = 2, -2\pi \leq \theta \leq 4\pi$

$$6 \sin^2 x - \sin x - 2 = 0$$

$$6 \sin^2 x - 4 \sin x + 3 \sin x - 2 = 0$$

$$2 \sin x (3 \sin x - 2) + 1 (3 \sin x - 2) = 0$$

$$(2 \sin x + 1)(3 \sin x - 2) = 0$$

$$\sin x = -\frac{1}{2}$$

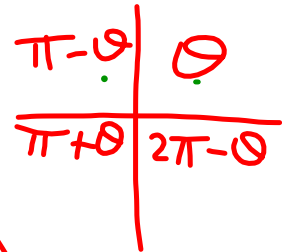
(y) (x, $\frac{1}{2}$)

Ref $\frac{\pi}{6}, Q 3, 4$
 $+2\pi \quad +2\pi$

$$\begin{aligned} x &= \frac{7\pi}{6}, \frac{11\pi}{6} \\ &= \frac{19\pi}{6}, \frac{23\pi}{6} \\ &= \frac{-5\pi}{6}, \frac{-\pi}{6} \end{aligned}$$

$$\sin x = \frac{2}{3}$$

(Ref $\approx 0.73, Q 1, 2$)



$$\begin{aligned} x &= 0.73, 2.41, 7.01, 8.69 \\ &= -5.55, -3.87 \end{aligned}$$

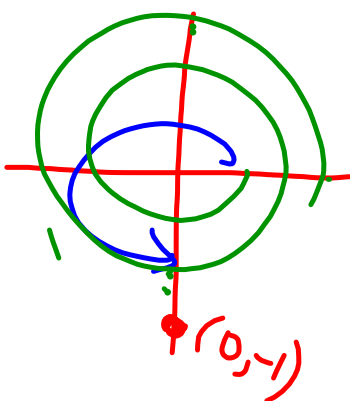
In-Class Asst:

$$(m + \frac{1}{2})(m + 1) = 0$$

$$\sin x = -\frac{1}{2}$$



$$\textcircled{4} \sin x = -1$$



$$-4\pi \leq x < 2\pi$$

$$x = \frac{3\pi}{2}, -\frac{\pi}{2}, -\frac{5\pi}{2}$$

$$\begin{aligned}\cos^3 \theta - 2\cos^2 \theta + \cos \theta &= 0 \\ \cos \theta (\cos^2 \theta - 2\cos \theta + 1) &= 0 \\ \cos \theta (\cos \theta - 1)(\cos \theta + 1) &= 0\end{aligned}$$

General Solution of a Trigonometric Equation

Solve: $3\cos^2\theta - \cos\theta = 2$; $\theta \in \mathbb{R}$ (degrees)

$$3\cos^2\theta - \cos\theta - 2 = 0$$

$$3\cos^2\theta - 3\cos\theta + 2\cos\theta - 2 = 0$$

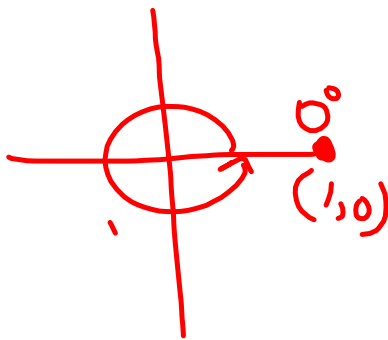
$$3\cos\theta(\cos\theta - 1) + 2(\cos\theta - 1) = 0$$

$$(\cos\theta - 1)(3\cos\theta + 2) = 0$$

$$\overset{(x)}{\cos\theta} = 1$$

$$\cos\theta = -\frac{2}{3}$$

(Ref $\approx 48^\circ$, Q2,3)



$$\theta = 132^\circ + 360k, k \in \mathbb{I}$$

$$\theta = 228^\circ + 360k, k \in \mathbb{I}$$

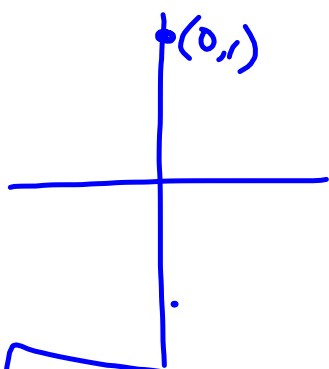
$$\theta = 0^\circ + 360k, k \in \mathbb{I}$$

Determine the general solution for $\sin^2 x - 1 = 0$ over the real numbers if x is measured in radians.

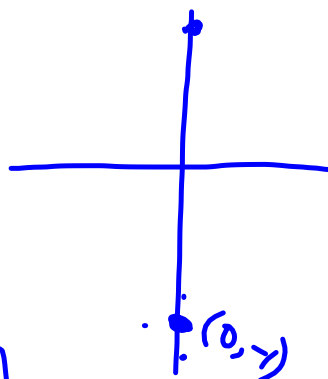
$$\begin{aligned} \sin^2 x - 1 &= 0 \\ (\sin x - 1)(\sin x + 1) &= 0 \\ \sin x = 1 \text{ or } \sin x = -1 \end{aligned}$$

$$\left. \begin{aligned} \sqrt{\sin^2 x} &= \sqrt{1} \\ \sin x &= \pm 1 \end{aligned} \right\}$$

Did You Know?
 $2n$, where $n \in \mathbb{I}$, represents all even integers.
 $2n + 1$, where $n \in \mathbb{I}$, is an expression for all odd integers.



$$x = \frac{\pi}{2} + 2\pi k, k \in \mathbb{I}$$



$$x = \frac{3\pi}{2} + 2\pi k, k \in \mathbb{I}$$

$$x = \frac{\pi}{2} + 2\pi n, \text{ where } n \in \mathbb{I}$$

$$x = \frac{3\pi}{2} + 2\pi n, \text{ where } n \in \mathbb{I}$$

or

$$x = \frac{\pi}{2} + \pi n, \text{ where } n \in \mathbb{I}$$

or

$$(2n + 1)\left(\frac{\pi}{2}\right), n \in \mathbb{I}$$

ex. 2

$$-5.8 = 7 \sin(t + 3.8) - 4.5$$

$$\frac{-5.8 + 4.5}{7} = \frac{7 \sin(t + 3.8)}{7}$$

$$-\frac{1.3}{7} = \sin(t + 3.8)$$

$$\sin^{-1}\left(-\frac{1.3}{7}\right) = \sin^{-1}(\sin(t + 3.8))$$

$$\sin^{-1}\left(\frac{1.3}{7}\right) = t + 3.8$$

(Ref $\times 0.19, 2.34$)

Q3: $\pi + 0.19 = 3.33$

$$3.33 = t + 3.8$$

$$t = -0.47 \text{ sec}$$

$$t = 5.81 \text{ sec}$$

$+2\pi$

- Radians

- 1st 3 times

$$t = 2.29 \text{ s}, 5.81 \text{ sec}, 8.57 \text{ sec}$$

$$\sin(40^\circ + 50^\circ)$$

$$\sin 40^\circ + \sin 50^\circ$$

Q4: $2\pi - 0.19 = 6.09$

$$6.09 = t + 3.8$$

$$t = 2.29 \text{ sec}$$

$$t = 8.57$$

$+2\pi$

Practice Problems:

Pages 212 - 214

#11 - 23

Check-Up problem...

Solve: $\sin x \sec x + 2 \sin x = 0, x \in R$ (x is measured in radians)

Find 2 times

$$(2) \quad 3.8 = 8.6 \cos \left[\frac{\pi}{5}(t+3) \right] - 2.3$$

$$3.8 + 2.3 = 8.6 \cos \left(\frac{\pi}{5}(t+3) \right)$$

$$\frac{6.1}{8.6} = \cos \left(\frac{\pi}{5}(t+3) \right)$$

$$\cos^{-1} \left(\frac{6.1}{8.6} \right) = \frac{\pi}{5}(t+3) \quad \cos \theta = \frac{6.1}{8.6}$$

(Ref $\rightarrow 0.78, 0.14$)
 $\theta = 0.78$ or $2\pi - 0.78 = 5.50$

Q1

Q4

$$\left(\frac{5}{\pi} \right) 0.78 = \frac{\pi}{5}(t+3) \quad \left. \begin{array}{l} 0 \\ \pi \end{array} \right\} \quad 5.50 = \frac{\pi}{5}(t+3)$$

$$\frac{5}{\pi}(0.78) - 3 = t$$

$$\frac{5}{\pi}(5.5) - 3 = t$$

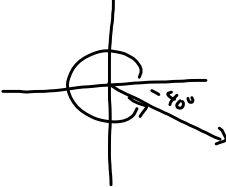
$$\underline{t = -1.76}$$

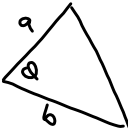
$$\underline{t = 5.75}$$


Unit Review...

What topics have we covered??

→ Radians ↔ Degrees Must be
 → Calculations: $\theta = \frac{a}{r}$ Radians

→ Principal Angles
 → Co-terminal Angles 

→ Formula:
 Triangle: $A = \frac{1}{2} ab \sin \theta$ 

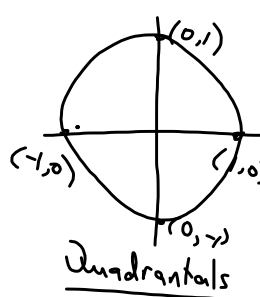
Sector: Degrees Radians
 $A = \left(\frac{\theta}{360}\right) \pi r^2$ or $A = \frac{\theta r^2}{2}$ 

Segment: $A_{\text{seg.}} = A_{\text{Sector}} - A_{\text{Triangle}}$

Angular Velocity $V_{\theta} = \frac{\theta}{t}$

Trigonometry of Rotation Angles

⇒ Special Angles in Radians

 $\left(\frac{\pi}{6}\right) 30^\circ \Rightarrow \left(\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$
 $\left(\frac{\pi}{3}\right) 60^\circ \Rightarrow \left(\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$
 $\left(\frac{\pi}{4}\right) 45^\circ \Rightarrow \left(\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}\right)$

Trig. Equations

- Linear
- Quadratic
- Ugly Linear!!

Review:

Pg. 215

1, 2, 3, 4, 5, 6, 12, 13, 14, 15, 16, 18, 20, 21, 23

Pg. 218

1, 2, 3, 5, 6, 12, 13, 15, 16

Attachments

Worksheet - Sketching Angles in Radians.doc