

$(-3x^4 - 2y^7)^5$  ← Expand & Simplify



$$\begin{array}{l}
 \begin{array}{l}
 -243 \\
 1(-3x^4)^5(-2y^7)^0
 \end{array}
 + \begin{array}{l}
 5x^8 1x^{-2} \\
 5(-3x^4)^4(-2y^7)^1
 \end{array}
 + \begin{array}{l}
 10x^{-2} 27x^4 \\
 10(-3x^4)^3(-2y^7)^2
 \end{array}
 + \begin{array}{l}
 10x^4 9x^{-8} \\
 10(-3x^4)^2(-2y^7)^3
 \end{array}
 + \begin{array}{l}
 5x^{-3} 3x^{16} \\
 5(-3x^4)^1(-2y^7)^4
 \end{array}
 + \begin{array}{l}
 -32 \\
 1(-3x^4)^0(-2y^7)^5
 \end{array}
 \end{array}$$

$$\begin{aligned}
 &= -243x^{20} - 810x^{16}y^7 - 1080x^{12}y^{14} - 720x^8y^{21} \\
 &\quad - 240x^4y^{28} - 32y^{35}
 \end{aligned}$$

# Return to the Binomial Theorem...

Binomial	Pascal's Triangle in Binomial Expansion	Row
$(x + y)^0$	1	1
$(x + y)^1$	1x + 1y	2
$(x + y)^2$	1x <sup>2</sup> + 2xy + 1y <sup>2</sup>	3
$(x + y)^3$	1x <sup>3</sup> + 3x <sup>2</sup> y + 3xy <sup>2</sup> + 1y <sup>3</sup>	4
$(x + y)^4$	1x <sup>4</sup> + 4x <sup>3</sup> y + 6x <sup>2</sup> y <sup>2</sup> + 4xy <sup>3</sup> + 1y <sup>4</sup>	5

Have a look at this neat connection...

Pascal's Triangle	Combinations
1	${}^0C_0$
1 1	${}^1C_0$ ${}^1C_1$
1 2 1	${}^2C_0$ ${}^2C_1$ ${}^2C_2$
1 3 3 1	${}^3C_0$ ${}^3C_1$ ${}^3C_2$ ${}^3C_3$
1 4 6 4 1	${}^4C_0$ ${}^4C_1$ ${}^4C_2$ ${}^4C_3$ ${}^4C_4$
1 5 10 10 5 1	${}^5C_0$ ${}^5C_1$ ${}^5C_2$ ${}^5C_3$ ${}^5C_4$ ${}^5C_5$

6  $\leftarrow$  3  
Combinations

$$\binom{n}{r}$$

You can use the **binomial theorem** to expand any power of a binomial expression.

$$(x + y)^n = {}_nC_0(x)^n(y)^0 + {}_nC_1(x)^{n-1}(y)^1 + {}_nC_2(x)^{n-2}(y)^2 + \dots + {}_nC_{n-1}(x)^1(y)^{n-1} + {}_nC_n(x)^0(y)^n$$

$$(x + y)^8$$

$${}^8C_0(x)^8(y)^0 + {}^8C_1(x)^7(y)^1 + {}^8C_2(x)^6(y)^2 + {}^8C_3(x)^5(y)^3 + {}^8C_4(x)^4(y)^4 + {}^8C_5(x)^3(y)^5 + {}^8C_6(x)^2(y)^6 + {}^8C_7(x)^1(y)^7 + {}^8C_8(x)^0(y)^8$$

Given the binomial expansion  $(2x - y^2)^{13}$

Determine the numerical coefficient of the term that has the variable parts...

(a)  $x^4 y^{18}$

(b)  $x^7 y^{12}$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \underline{{}^{13}C_9} (2x)^4 (-y^2)^9 \\
 & 715 (16x^4) (-y^{18}) \\
 & = \underline{-11440 x^4 y^{18}}
 \end{aligned} \right\} \begin{aligned}
 & \underline{{}^{13}C_6} (2x)^7 (-y^2)^6 \\
 & = 1716 (128x^7) (y^{12}) \\
 & = \underline{219648 x^7 y^{12}}
 \end{aligned}
 \end{aligned}$$

## Sum & Difference of Cubes

$$\left. \begin{array}{l} a^3 + b^3 \\ (a+b)(a^2 - ab + b^2) \end{array} \right\} \begin{array}{l} x^3 - y^3 \\ (x-y)(x^2 + xy + y^2) \end{array}$$

ex. 1)  $w^3 + 27$   
 $(w+3)(w^2 - 3w + 9)$

cube Root:  
 $\sqrt[3]{x^{27}}$   
 $(x^{27})^{1/3}$

2)  $x^{27} - 1$

$$(x^9 - 1)(x^{18} + x^9 + 1)$$

$$(x^3 - 1)(x^6 + x^3 + 1)(x^{18} + x^9 + 1)$$

$$(x-1)(x^2 + x + 1)(x^6 + x^3 + 1)(x^{18} + x^9 + 1)$$

3)  $8x^6 - 64$

$$8(x^6 - 8)$$

$$8(x^2 - 2)(x^4 + 2x^2 + 4)$$

4)  $w^{30} - y^{12}$

$$(w^{10} - y^4)(w^{20} + w^{10}y^4 + y^8)$$

$$(w^5 - y^2)(w^5 + y^2)(w^{20} + w^{10}y^4 + y^8)$$


---


$$(w^{15} - y^6)(w^{15} + y^6)$$

$$(w^5 - y^2)(w^{10} + w^5y^2 + y^4)(w^5 + y^2)(w^{10} - w^5y^2 + y^4)$$

Find the polynomial  $p(x)$   
such that its zeros are  $x = -1, 4$  and  $-2$

$$(x+1)(x-4)(x+2) = 0$$

$$(x^2 - 3x - 4)(x+2) = 0$$

$$x^3 + 2x^2 - 3x^2 - 6x - 4x - 8 = 0$$

$$x^3 - x^2 - 10x - 8 = 0$$

ex. 2)  $x = \frac{3}{4}, x = -2, x = \frac{1}{3}$

$$4x = \frac{3}{4} \quad x = -2 \quad x = \frac{1}{3}$$

$$4x = 3 \quad x + 2 = 0 \quad 3x = 1$$

$$4x - 3 = 0 \quad 3x - 1 = 0$$

$$(4x-3)(x+2)(3x-1) = 0$$

$$(4x^2 + 8x - 3x - 6)(3x-1)$$

$$(4x^2 + 5x - 6)(3x-1)$$

$$12x^3 - 4x^2 + 15x^2 - 5x - 18x + 6$$

$$12x^3 + 11x^2 - 23x + 6 = 0$$

# Polynomials Review

---

- Factoring Techniques
- Dividing Polynomials
- Remainder Theorem
- Factor Theorem
- Sum and Difference of Cubes
- Solving Polynomial Equations
- Permutations and Combinations
- Binomial Theorem

Review-Polynomials.pdf

